



DES Y3 results: Measurement of BAO with projected three-dimensional clustering

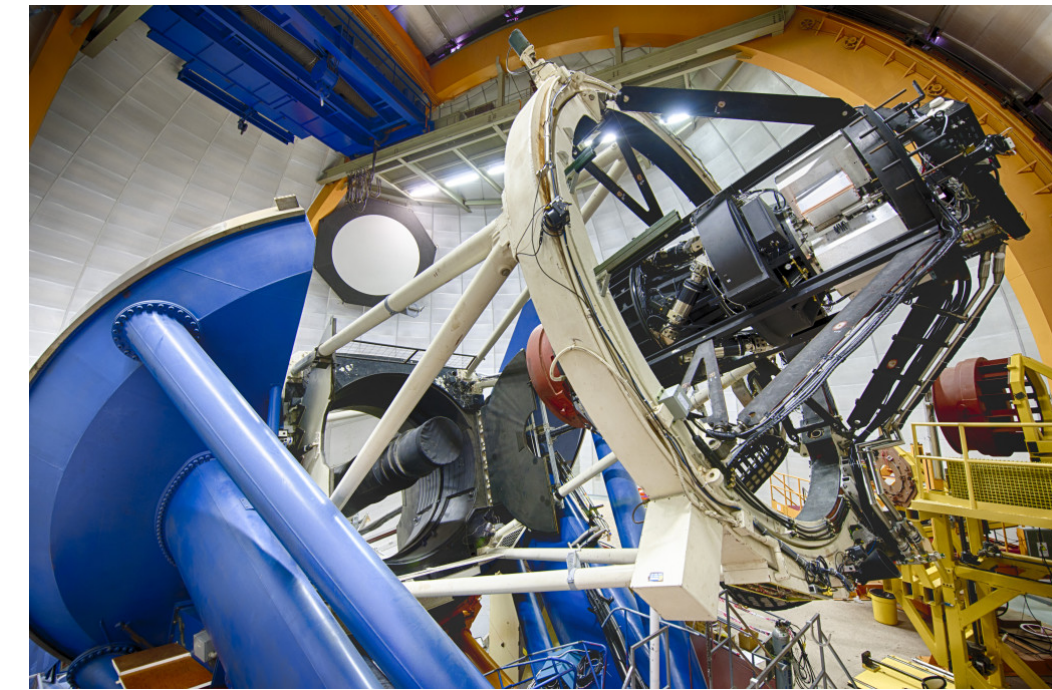
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In collaboration with Dark Energy Survey

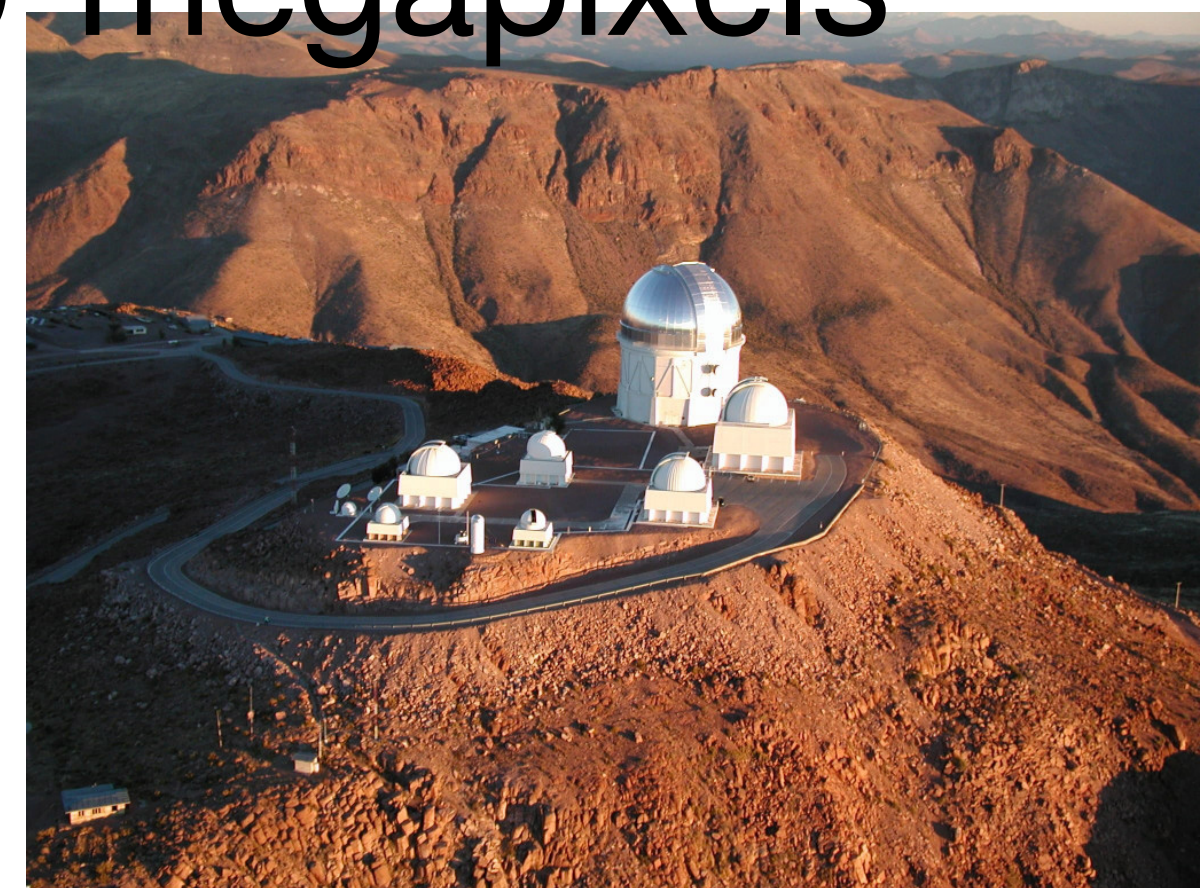
SJTU, 19 Jun 2023



Dark Energy Survey Year 3

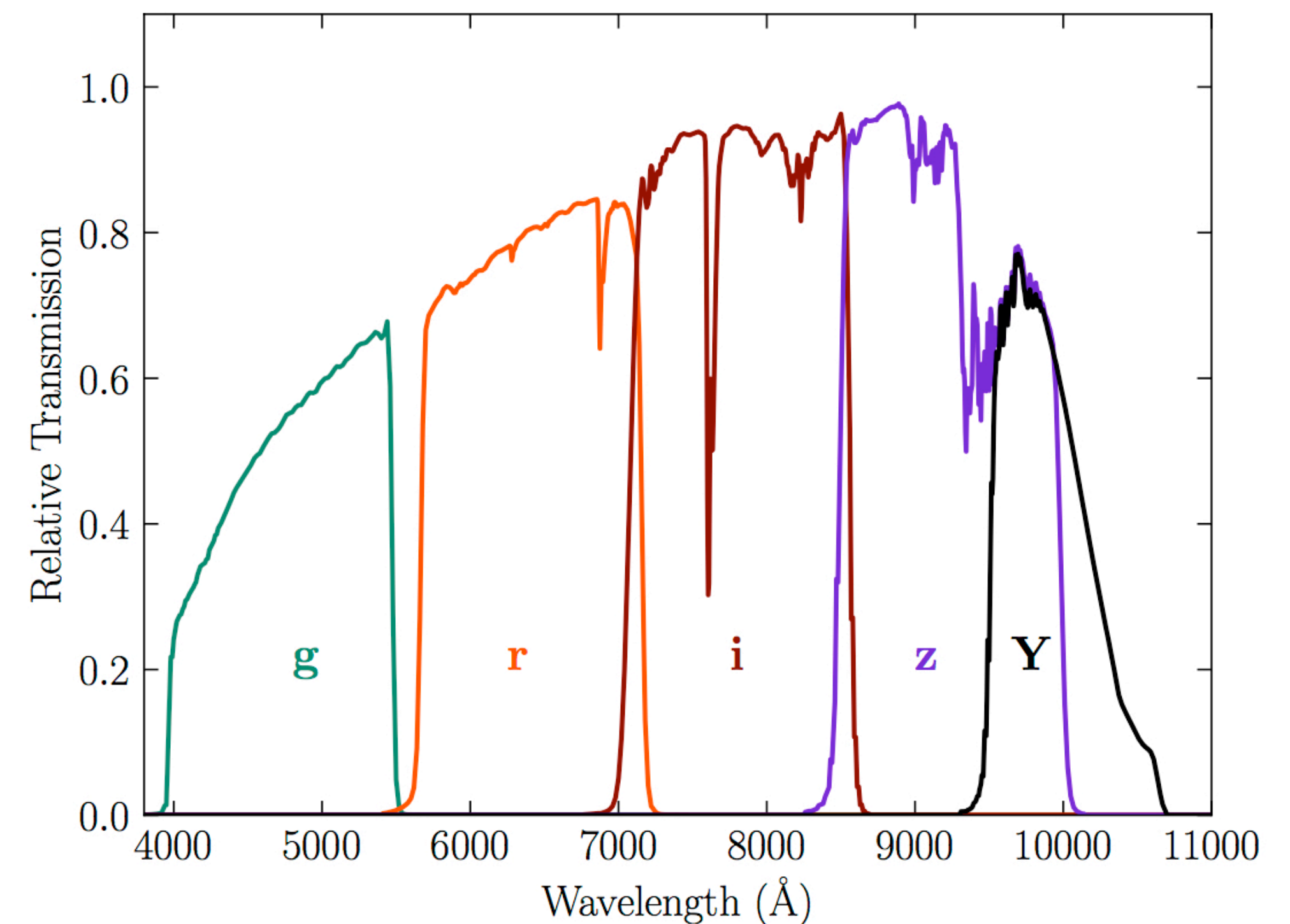
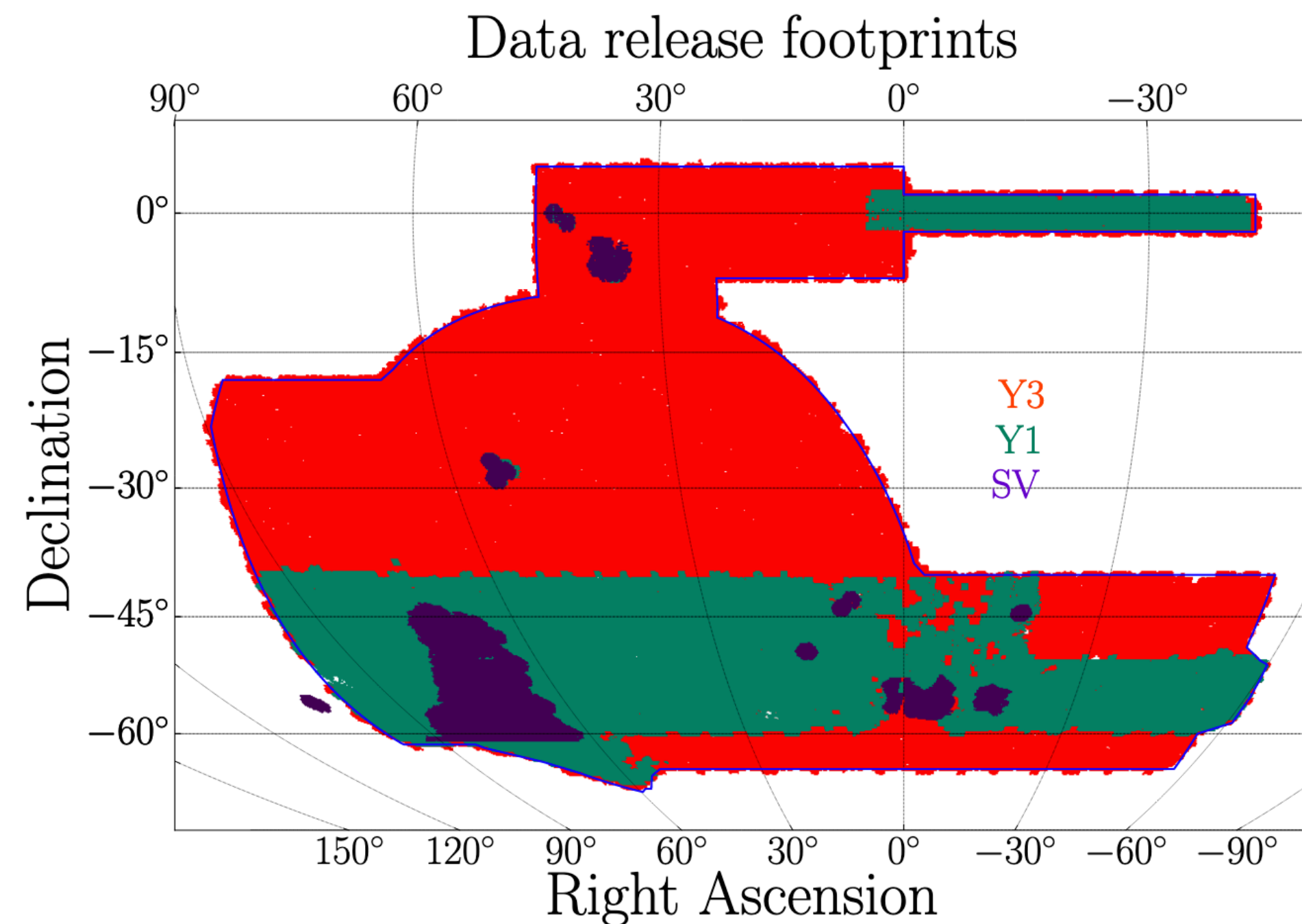


- Dark Energy Survey (DES) is an ongoing photometric survey, most well-known for weak lensing
- Blanco 4-meter telescope at Cerro Tololo Inter-American Observatory in Chile
- Dark Energy Camera, Field of view: 3 sq deg, 570-megapixels CCD
- Y3 observing time from 2013 to 2015



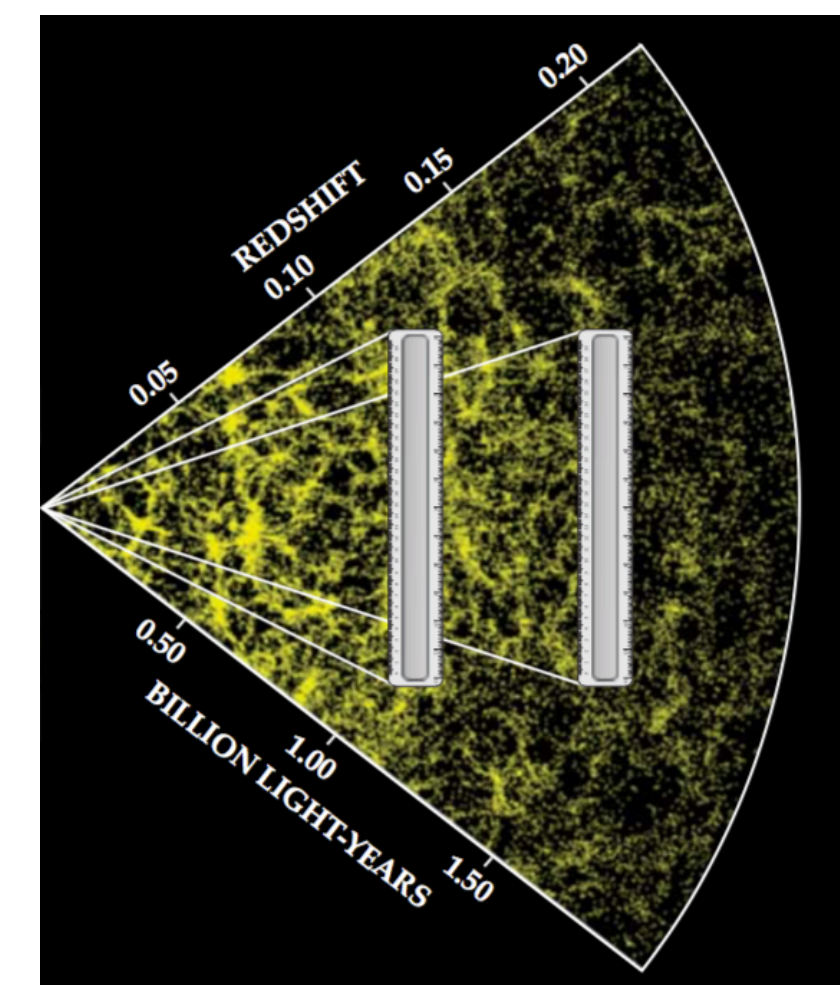
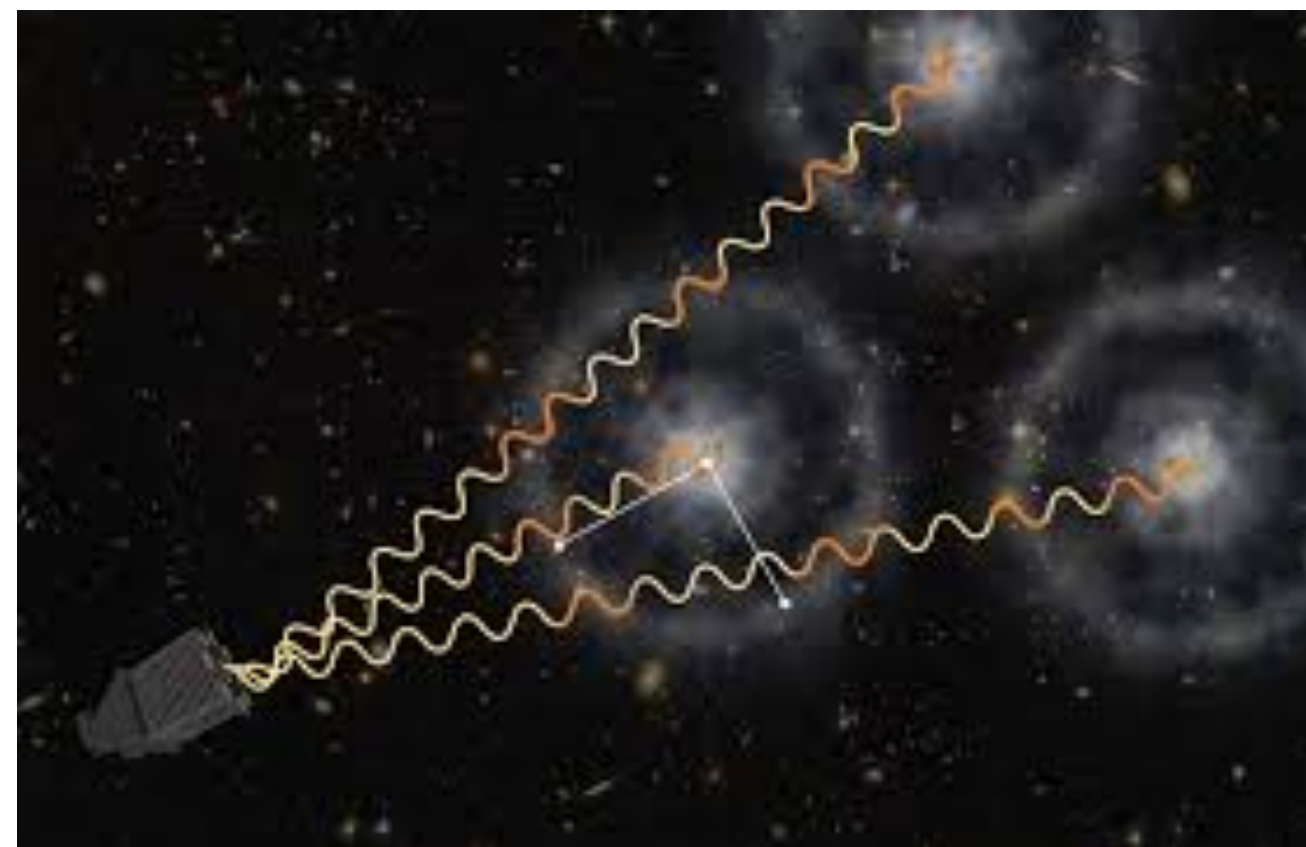
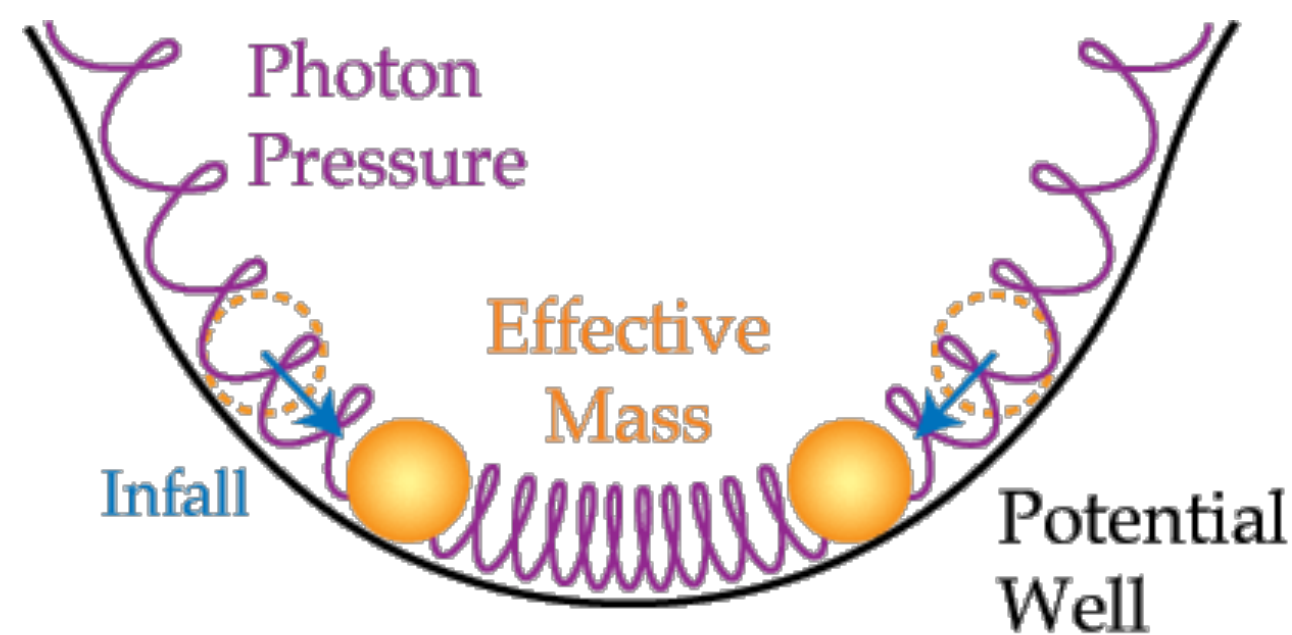
DES Y3

- DES Y3 gold sample covers about 5000 sq deg
- After masking, DES Y3 BAO sample covers about 4100 sq degree, with mean redshift of 0.83.



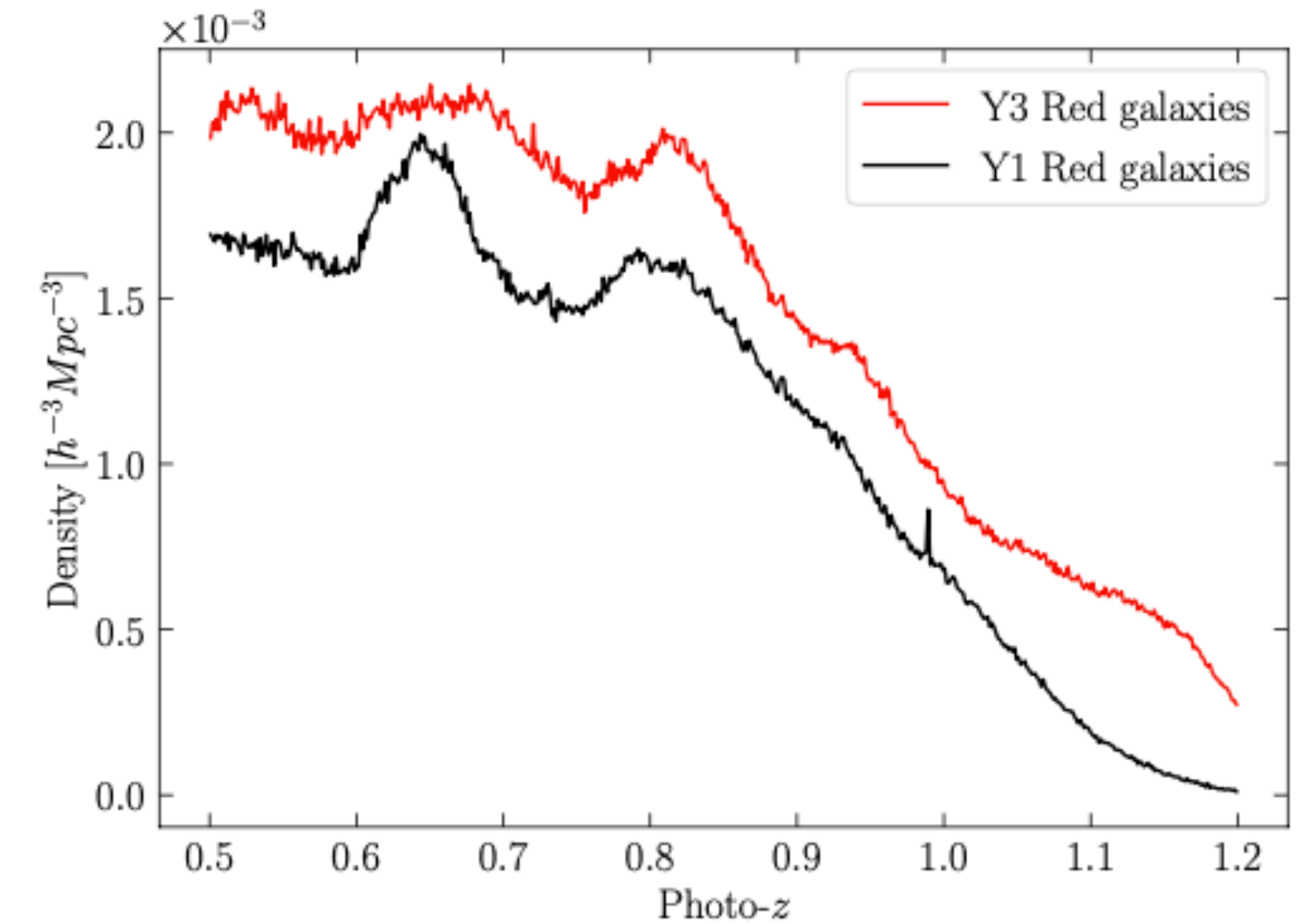
Baryonic Acoustic Oscillations (BAO)

- Acoustic oscillations during the early universe, imprinted in the distribution of the large-scale structure
- **Standard ruler** in the late universe
- Measured in numerous data analyses, mostly spec-z
- DES, lack of precise radial info, still preserve the **transverse** BAO.



Fiducial DES Y3 BAO analysis

- 7 million red galaxies $z=0.6$ to 1.1 , 5 tomographic bins
- 10σ depth of 22, 22, 22.3, and 21 for griz



Redshift limits	\bar{z}	W_{68}	σ_{68}	Number of galaxies	blind galaxy bias
$0.6 < z < 0.7$	0.648 ± 0.003	0.0455 ± 0.003	0.021 ± 0.001	1,478,178	1.79 ± 0.09
$0.7 < z < 0.8$	0.742 ± 0.003	0.0522 ± 0.002	0.025 ± 0.002	1,632,805	1.83 ± 0.10
$0.8 < z < 0.9$	0.843 ± 0.003	0.0629 ± 0.003	0.029 ± 0.002	1,727,646	2.02 ± 0.12
$0.9 < z < 1.0$	0.932 ± 0.004	0.0633 ± 0.003	0.030 ± 0.003	1,315,604	2.09 ± 0.14
$1.0 < z < 1.1$	1.020 ± 0.006	0.0808 ± 0.006	0.040 ± 0.005	877,760	2.4 ± 0.08

Angular clustering statistics

- The BAO is measured using angular correlation function w and angular power spectrum C_ℓ

$$w(\theta, z_p, z'_p) = \sum_{\ell} i^{\ell} \int dz \phi(z|z_p) \int dz' \phi(z'|z'_p) \mathcal{L}_{\ell}(\hat{\mathbf{s}} \cdot \hat{\mathbf{e}}) \int \frac{dk k^2}{2\pi^2} j_{\ell}(ks) P_{\ell}(k, z, z')$$

$$P(k, \mu) = (b + \mu^2 f)^2 \left[(P_{\text{lin}} - P_{\text{nw}}) e^{-k^2 \Sigma_{\text{tot}}^2} + P_{\text{nw}} \right]$$

$$C_{\ell} = 2\pi \int_{-1}^1 d(\cos \theta) w(\theta) \mathcal{L}_{\ell}(\cos \theta)$$

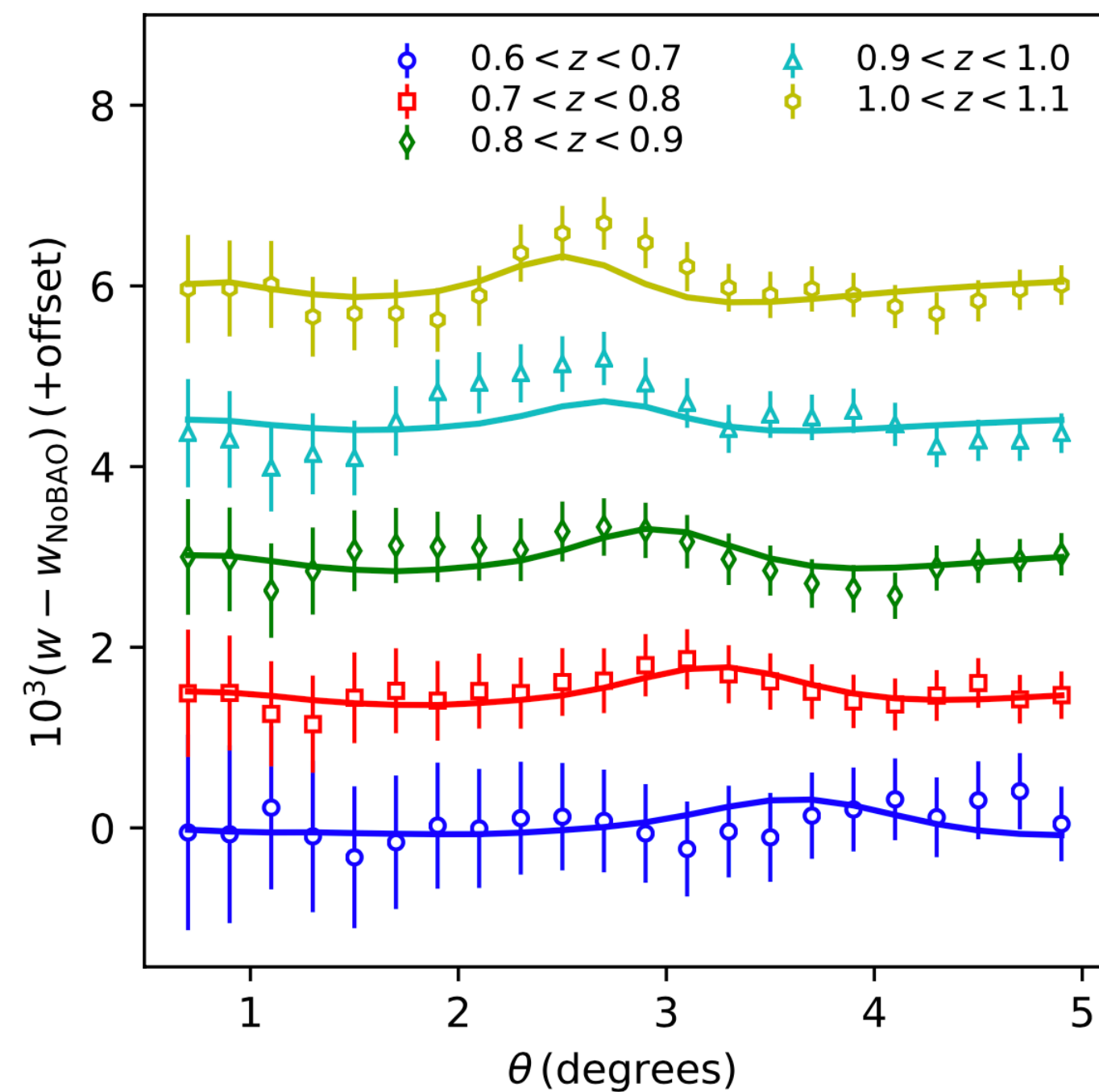
- BAO position in w or C_{ℓ} is extracted by fitting the full template to the data

$$M(x) = BT_{\text{BAO}, \alpha}(x') + A(x),$$

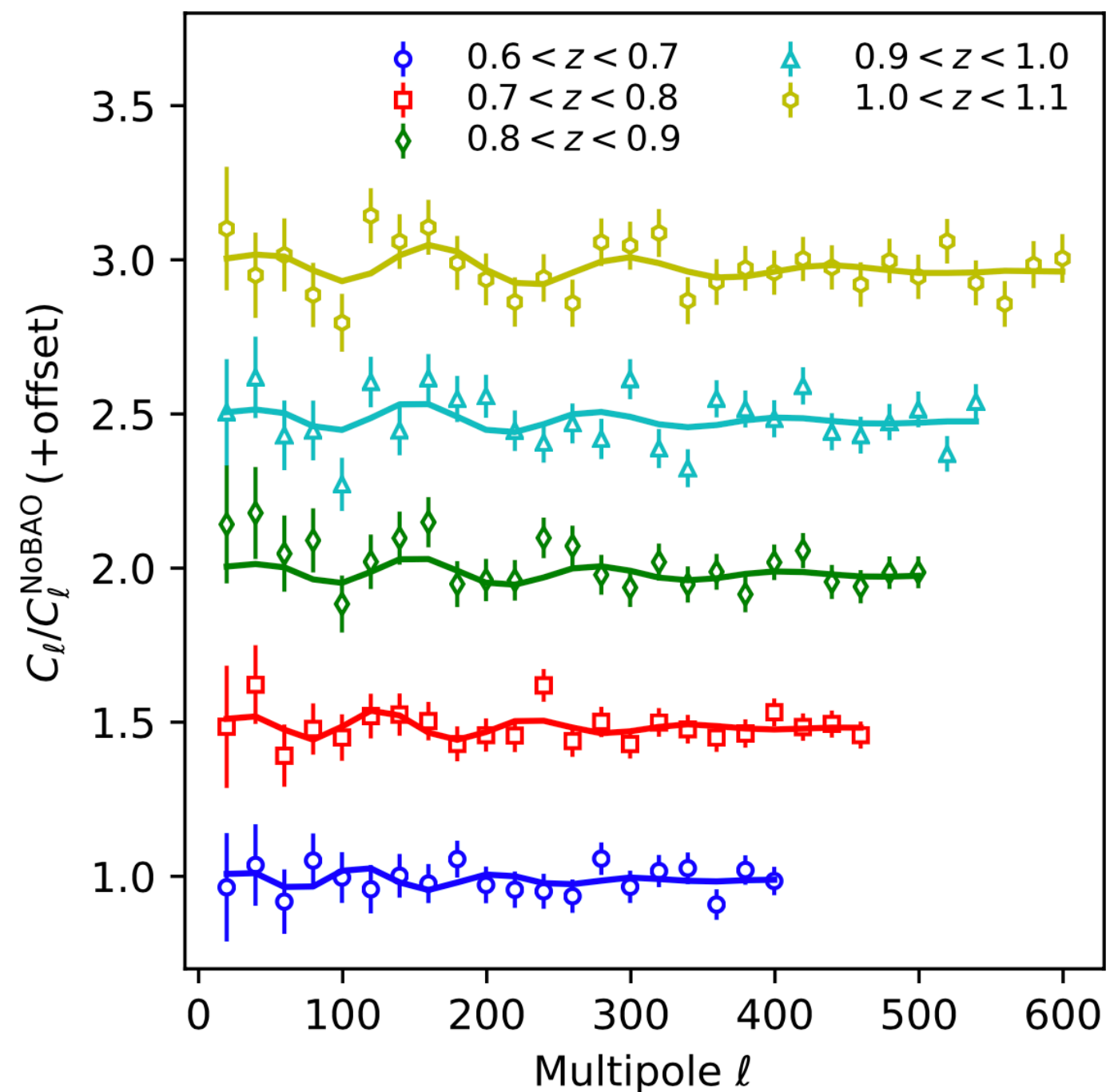
For w , $x = \theta$, $x' = \alpha\theta$, $T = w$, $A(\theta) = \sum_i \frac{a_i}{\theta^i}$ For C_{ℓ} , $x = \ell$, $x' = \frac{\ell}{\alpha}$, $T = C_{\ell}$, $A(\ell) = \sum_i a_i \ell^i$.

Angular BAO measurement

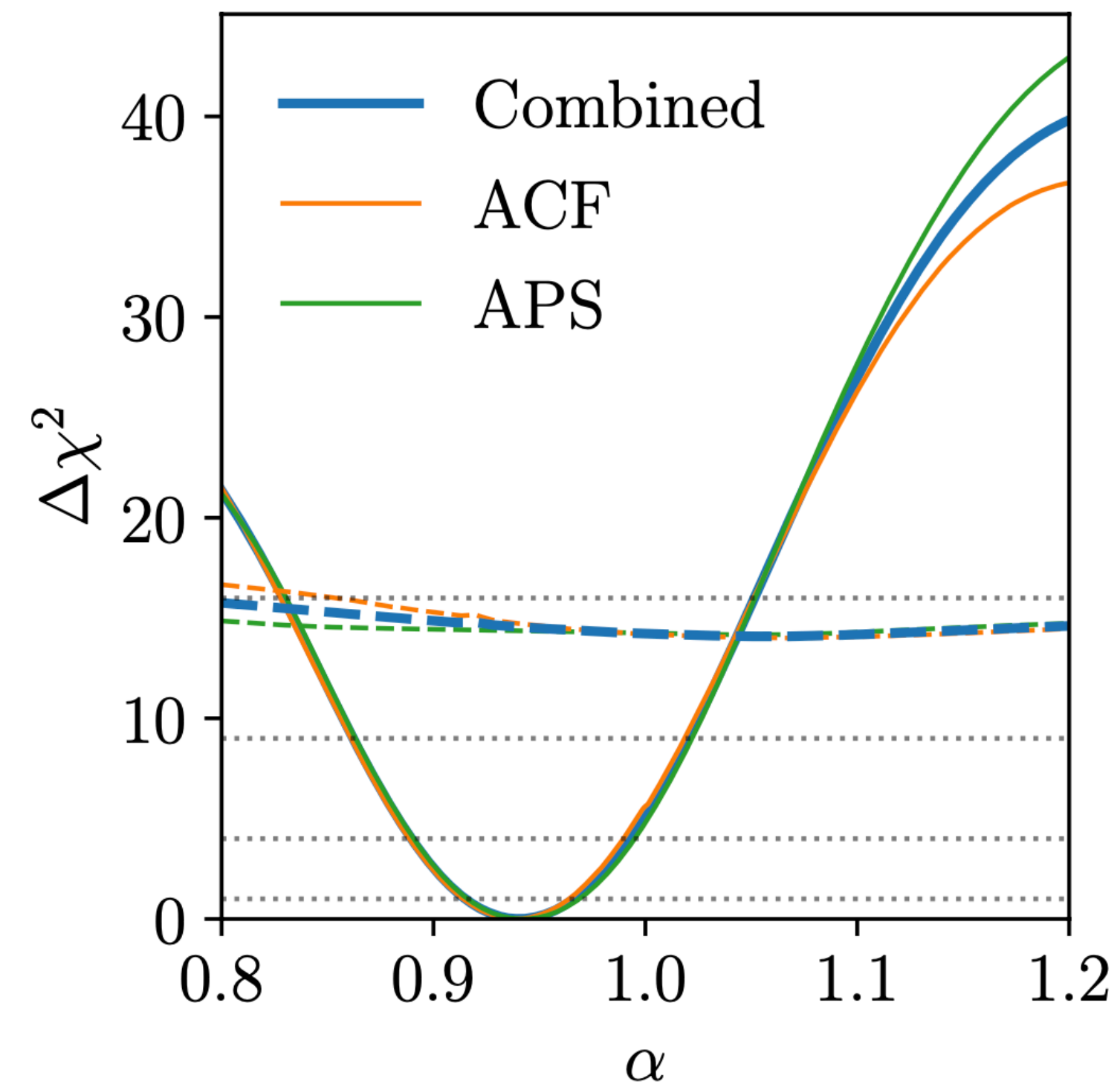
- w and C_ℓ results are consistent with each other



w



C_ℓ

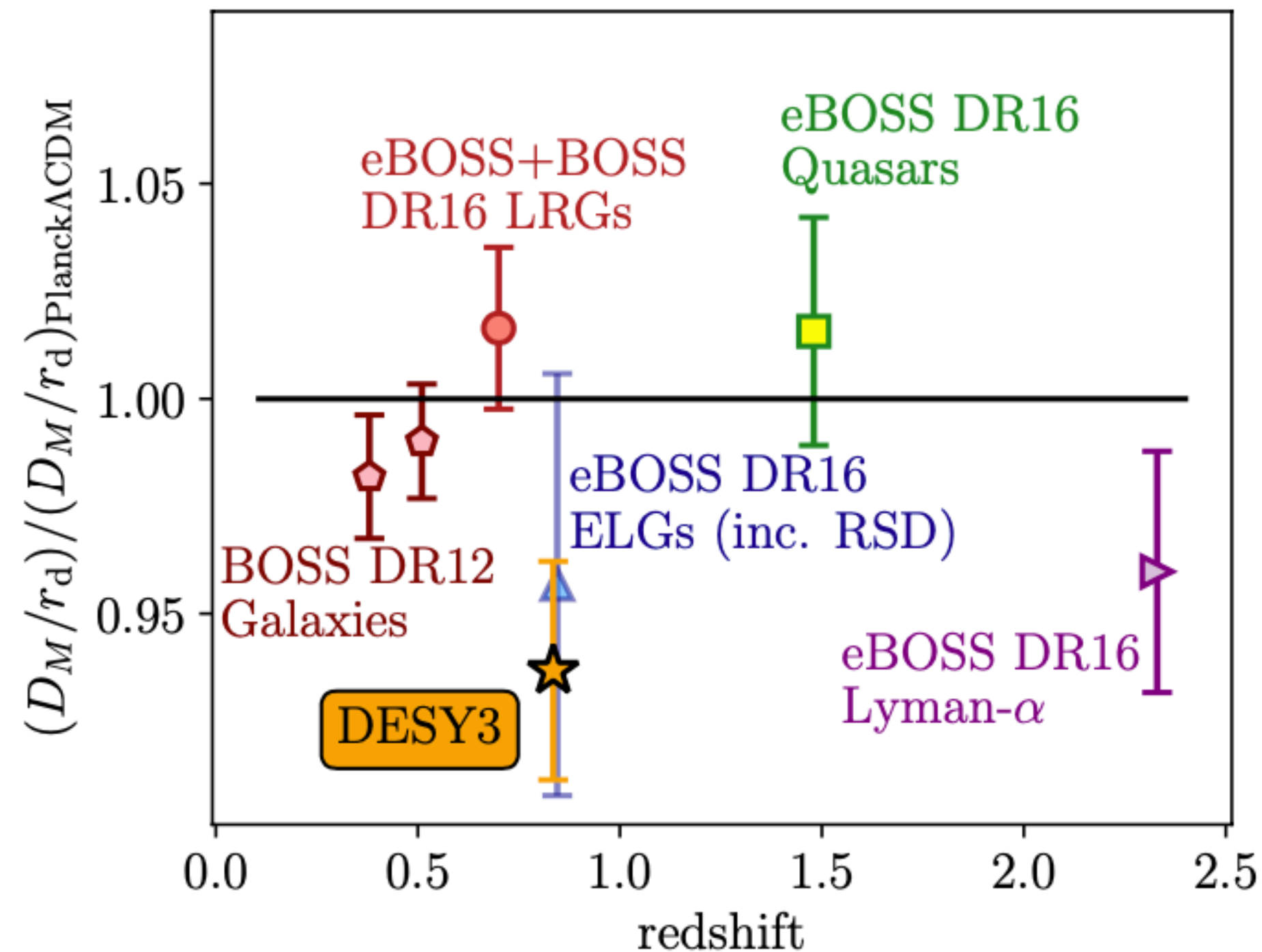


$$\alpha = \frac{\frac{D_M}{r_d} |_{\text{data}}}{\frac{D_M}{r_d} |_{\text{fid}}}$$

DES Y3 BAO constraints

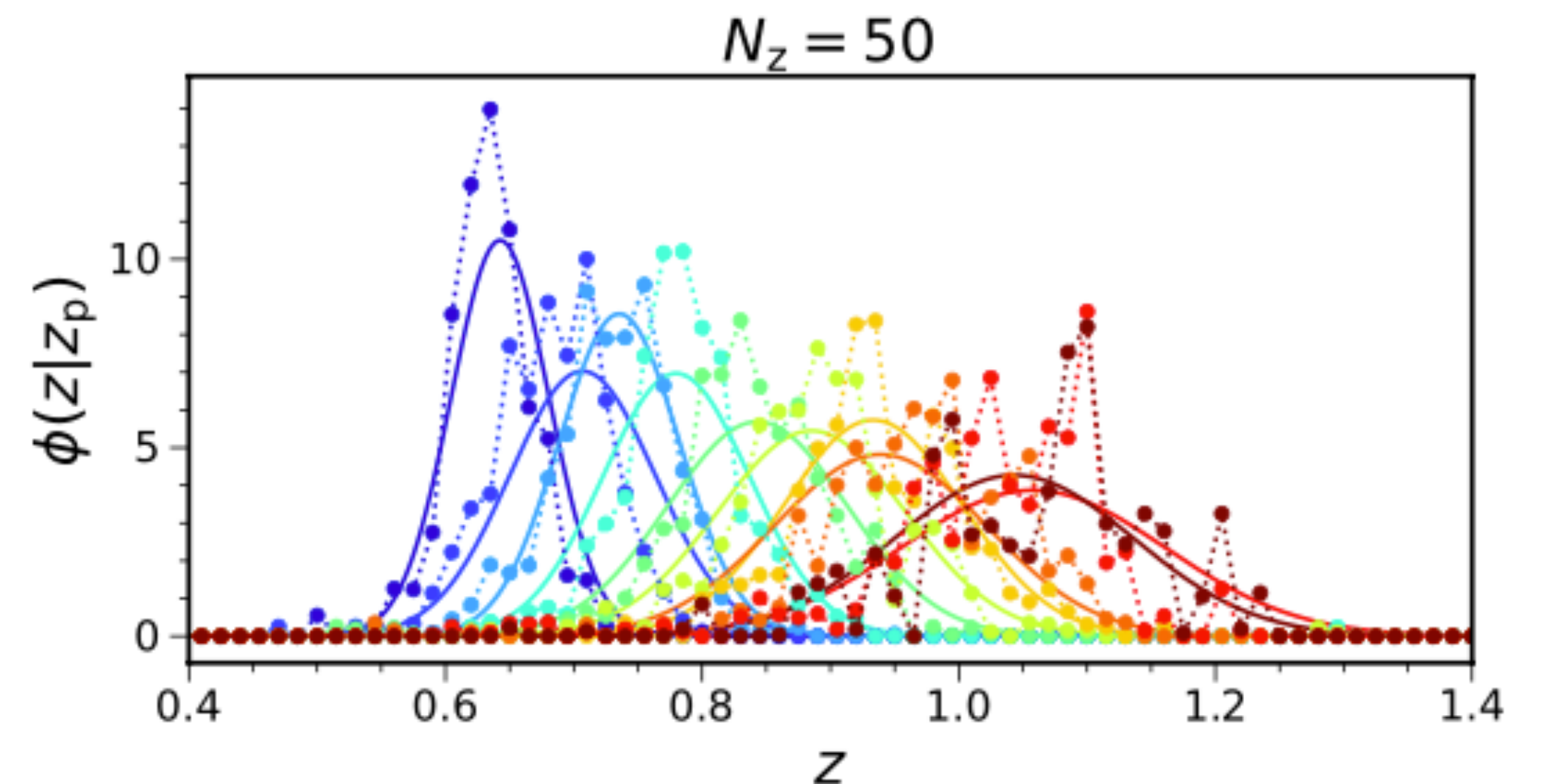
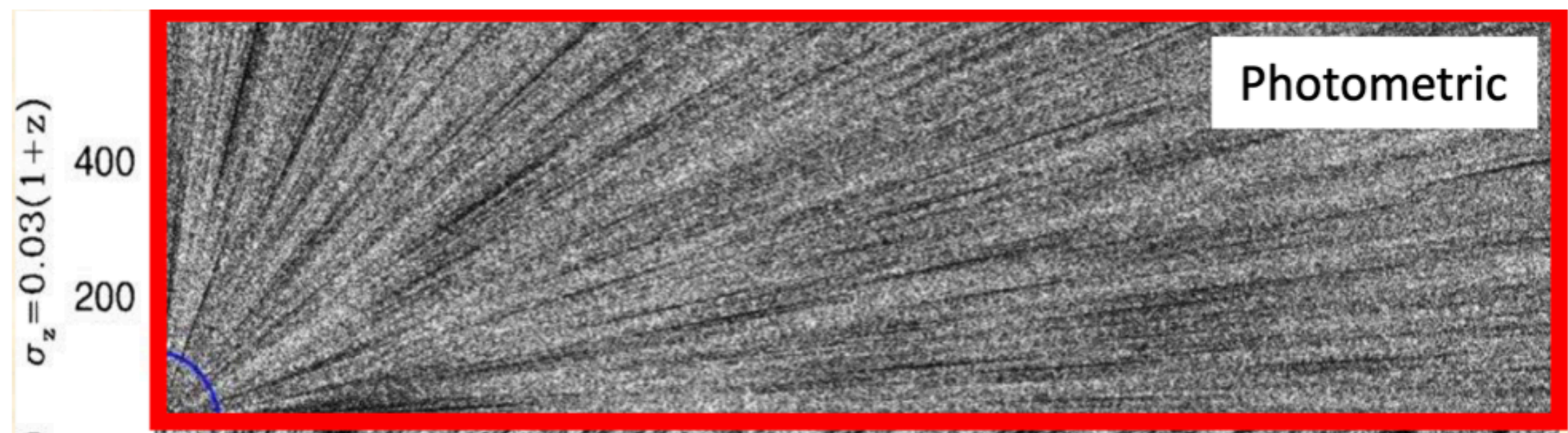
- $D_M/r_d = 18.92 \pm 0.51$, 2.5% measurement of the BAO at $z=0.83$
- Most precise BAO measurement from photometric surveys
- D_M/r_d is at 2.3σ deviation from the Planck results, need more data and alternative analyses to corroborate

$$\alpha = \frac{\frac{D_M}{r_d} |_{\text{data}}}{\frac{D_M}{r_d} |_{\text{fid}}}$$



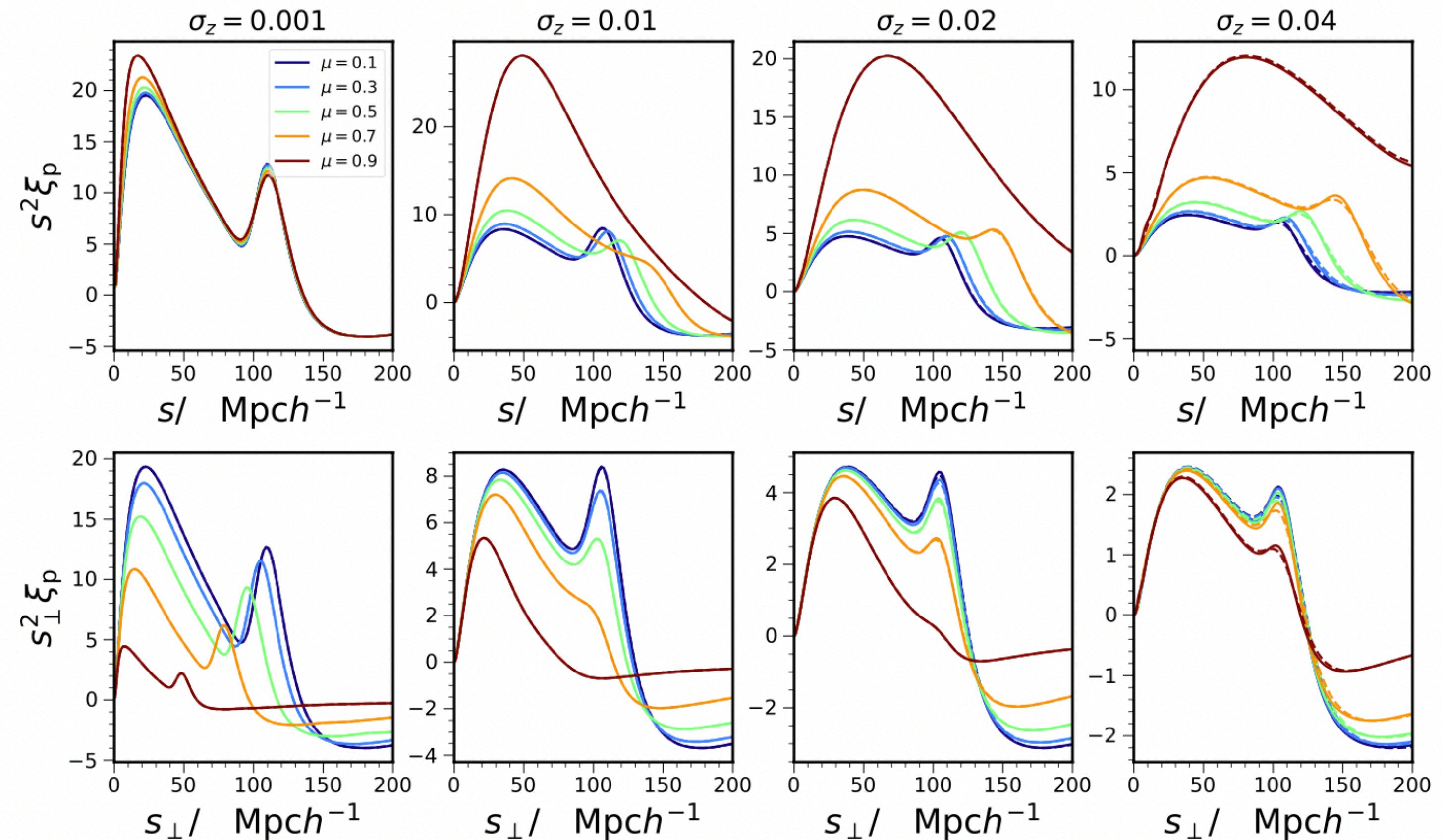
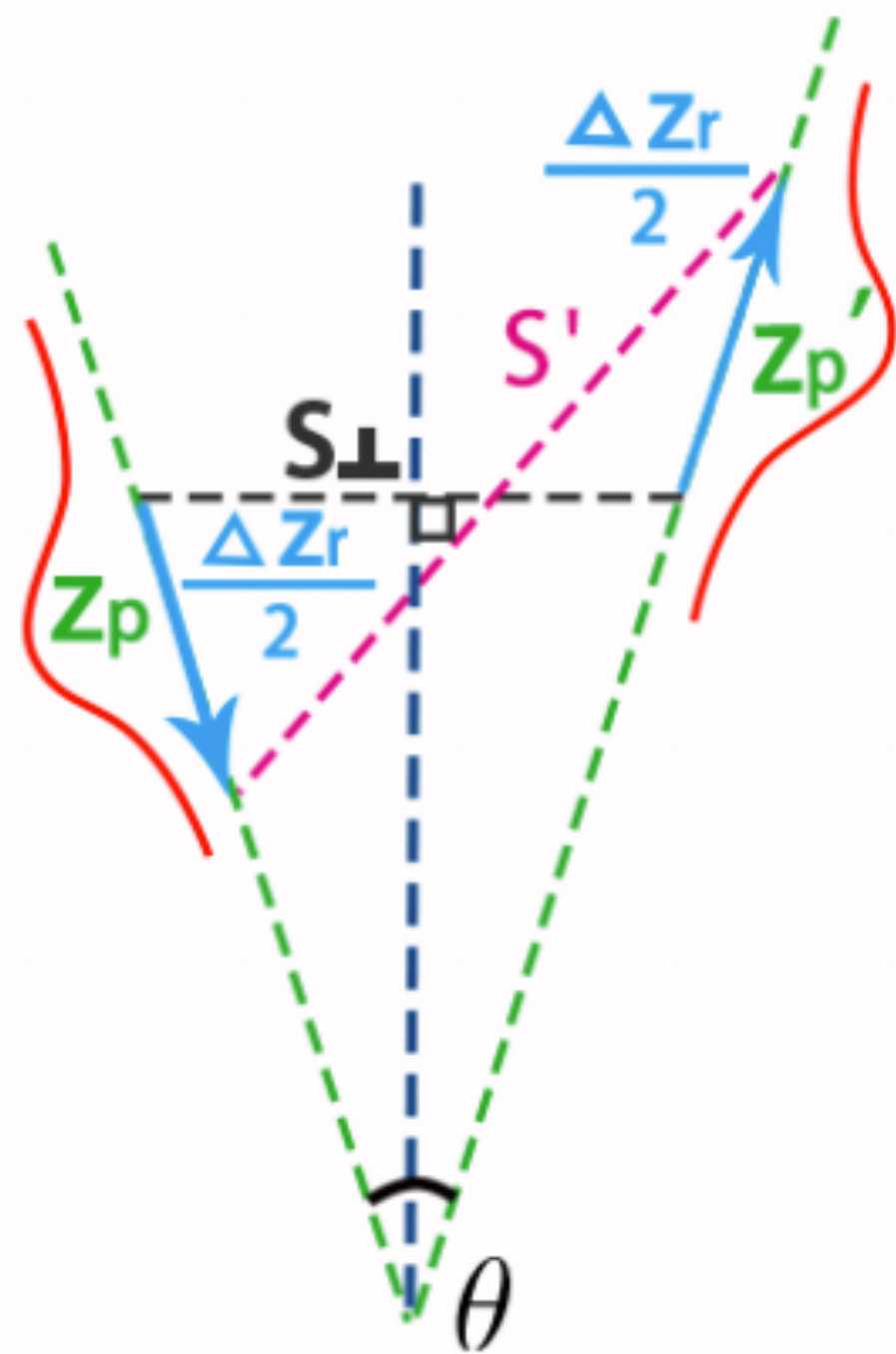
Three-dimensional correlation analysis

- Compute the 3D correlation function ξ akin to 3D analysis Ross +, 1705.05442
- Compress info in the whole redshift range into a single data vector. Include some radial info
- Need to take care of the evolving dn/dz
- Radial direction is smeared, need projection



3D correlation analysis for photometric data

- For $\sigma_z \geq 0.02$, only effectively probes the transverse information, the transverse BAO is preserved



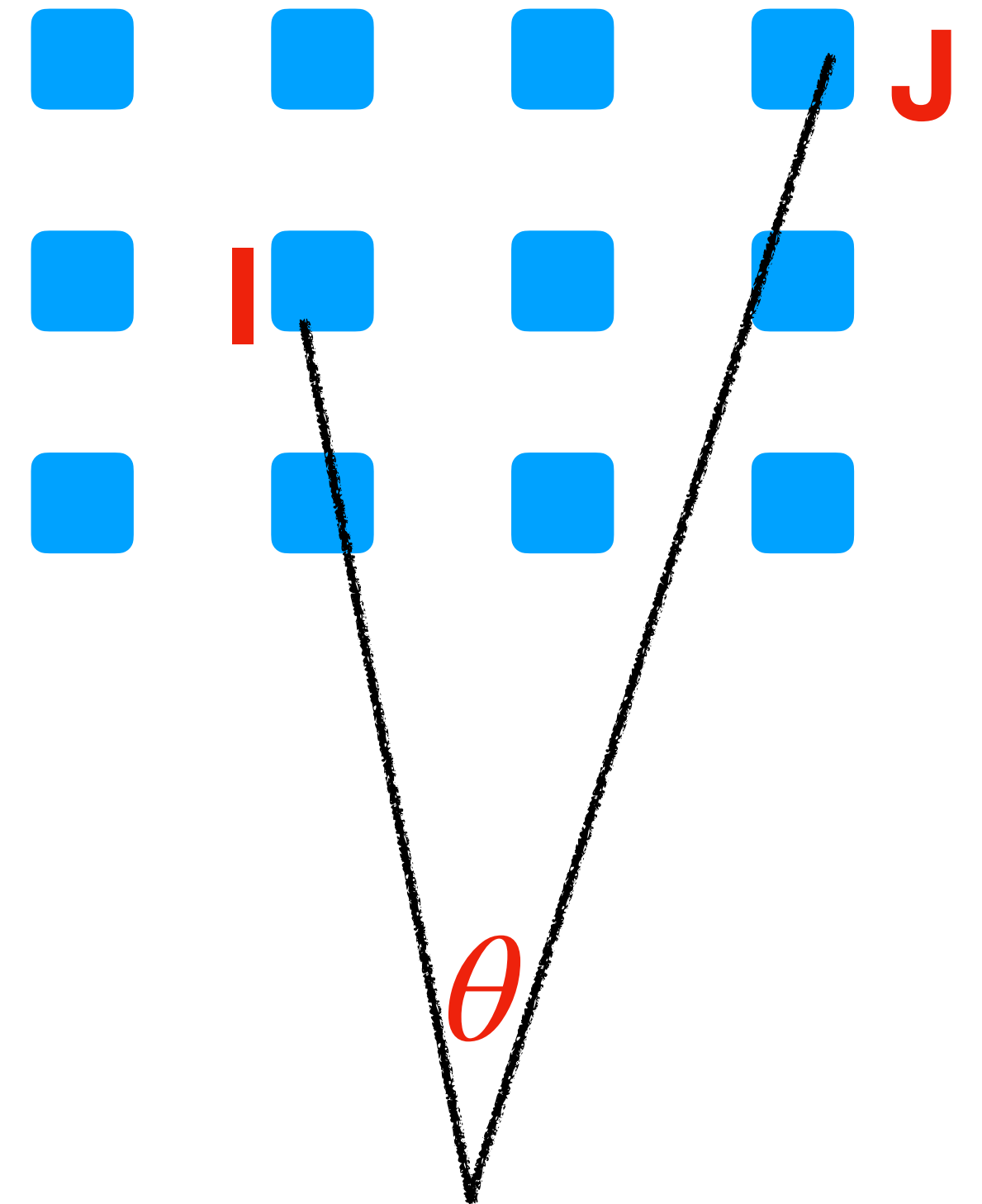
ξ_p template

- Obtained by mapping the general w template to ξ_p

$$w_{ij}(\theta) = \sum_{\ell=0,2,4} i^\ell \int dz \phi(z|z_p) \int dz' \phi(z'|z'_p) \\ \times \mathcal{L}_\ell(\hat{\mathbf{s}} \cdot \hat{\mathbf{e}}) \int \frac{dk k^2}{2\pi^2} j_\ell(ks) P_\ell(k, z, z'),$$

- Loop over ijk that satisfy the bin conditions, ensure the evolving dn/dz window is accounted for

$$\xi_p(s, \mu) = \frac{\sum_{ijk} f_{ijk} w_{ij}(\theta_k)}{\sum_{ijk} f_{ijk}}$$



ξ_p template

- Photo-z uncertainties, the radial info, especially the radial BAO is erased
- Project $\xi_p(s, \mu)$ to the transverse direction

KCC +, 2110.13332

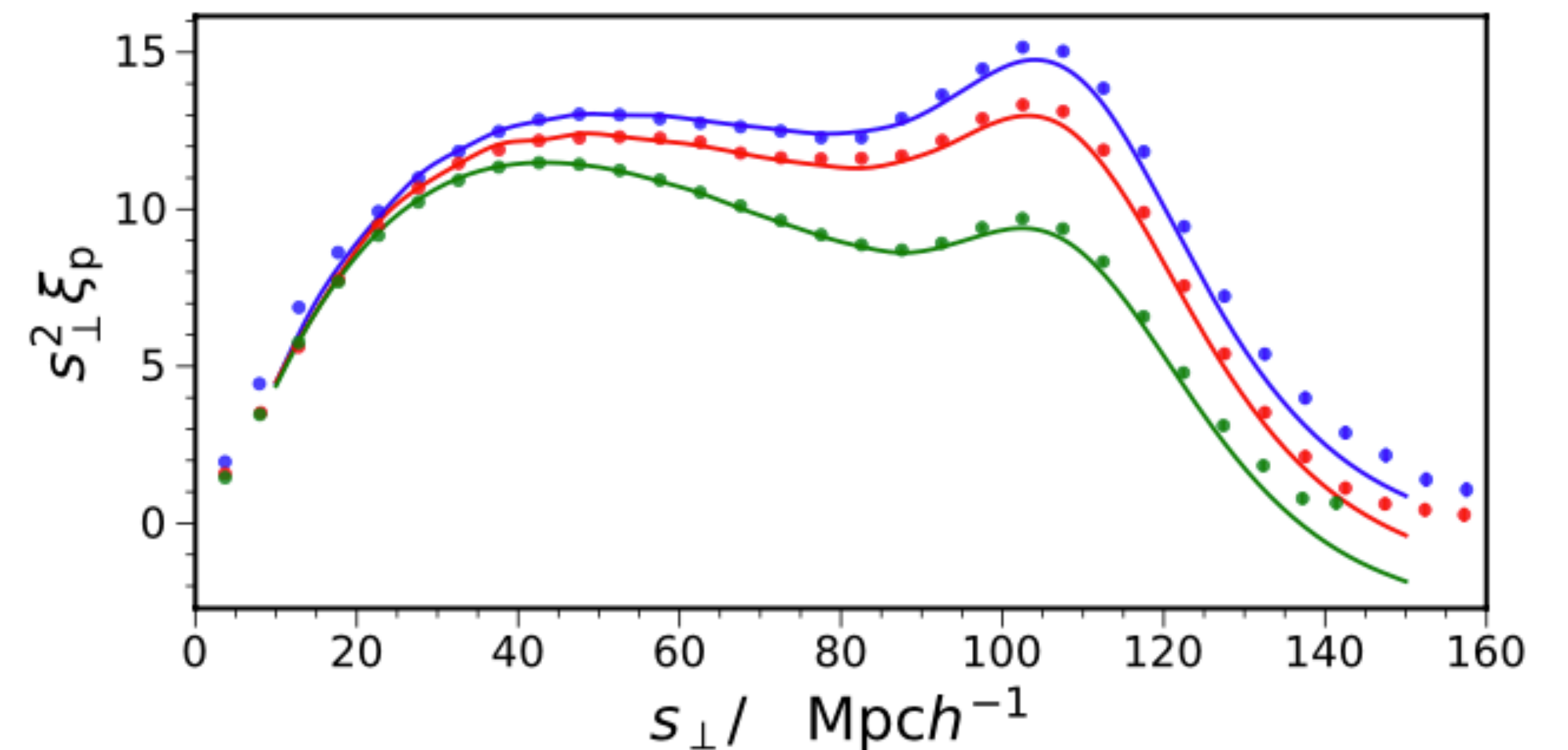
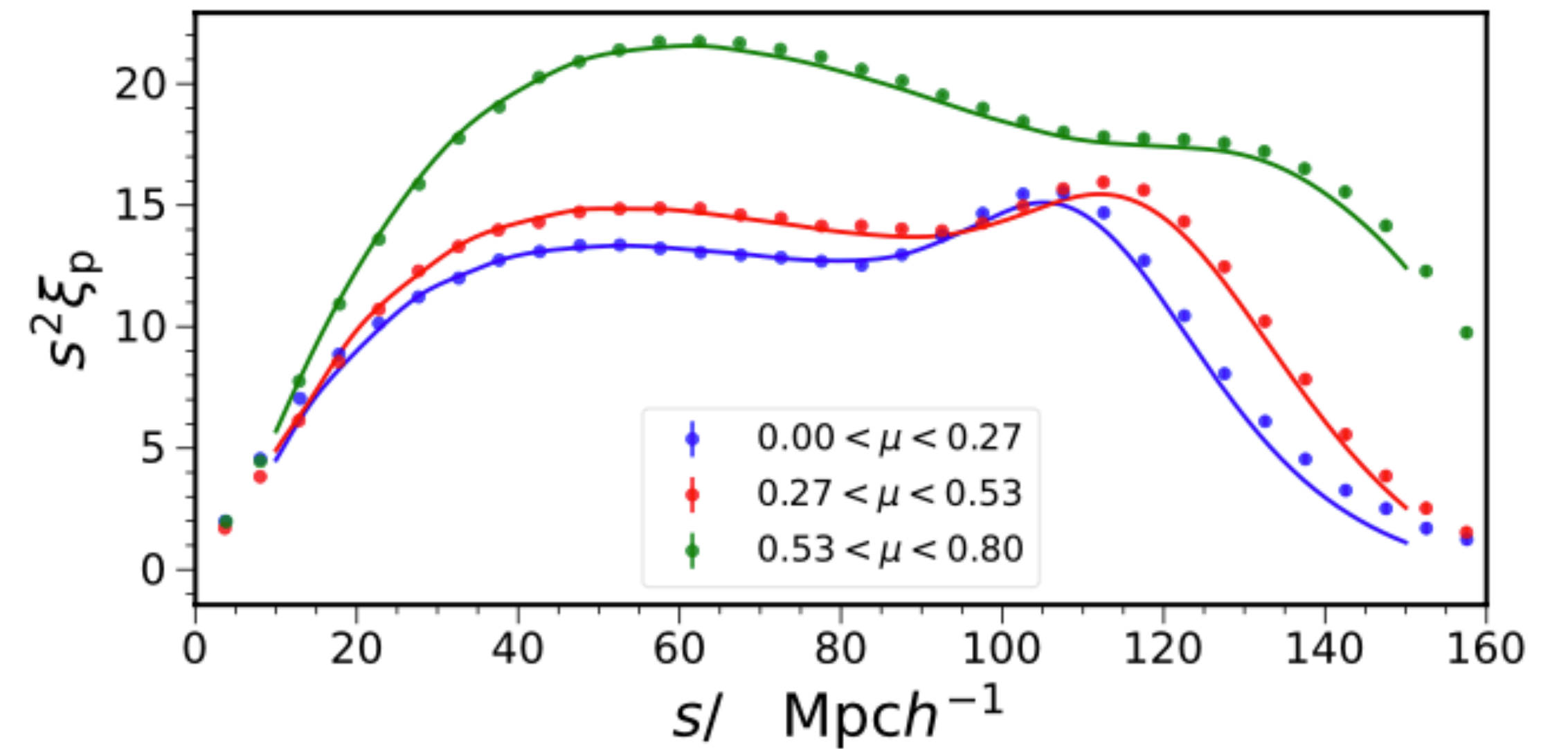
$$\xi_p(s_{\perp}) = \frac{\sum_i \xi_p(s, \mu_i) W(\mu_i)}{\sum_i W(\mu_i)}$$

Tophat: equal weighting, sub-optimal

Gaussian: suppress the pairs with low signal to noise

Theory vs mock measurement

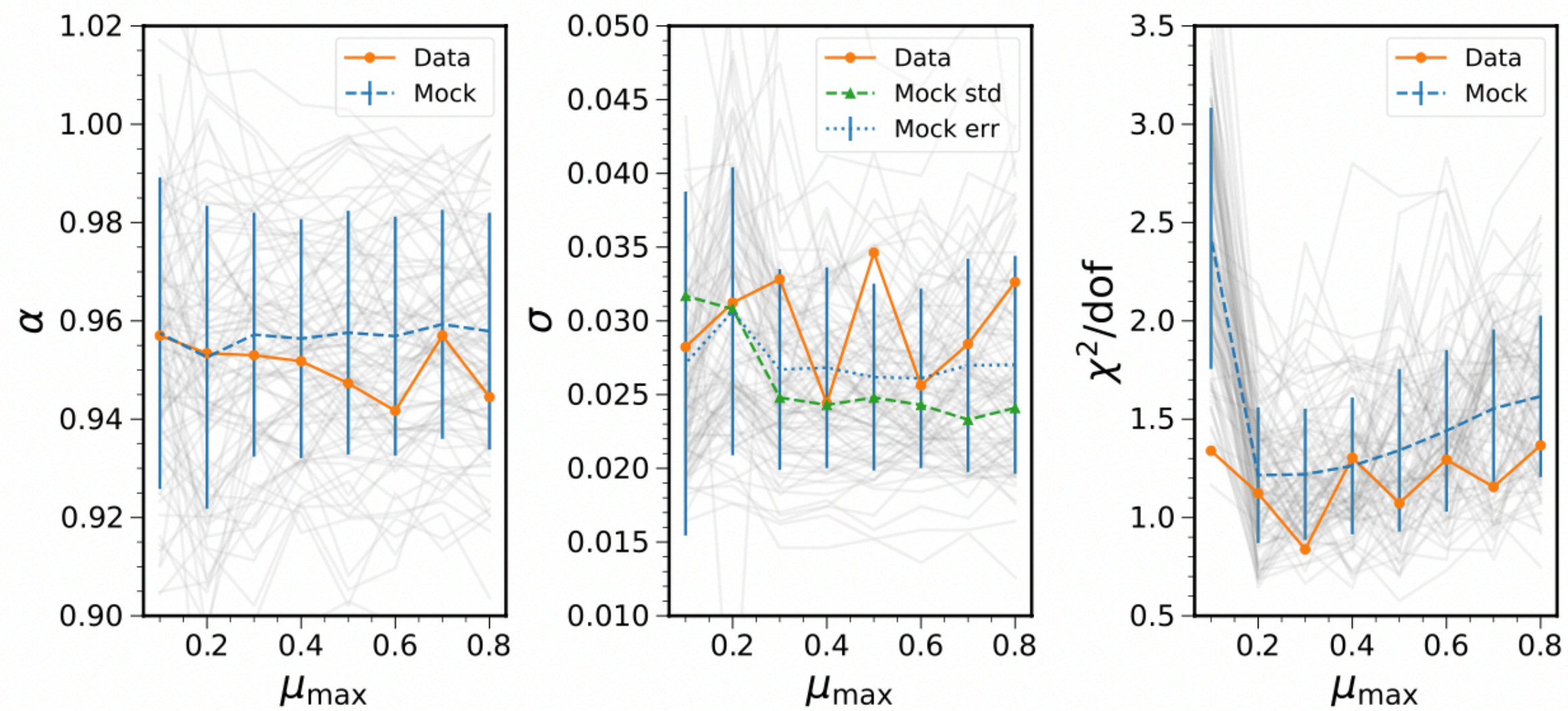
- ICE-COLA mocks, data include realistic photo-z uncertainties
- The theory template is in good agreement with the mock measurement



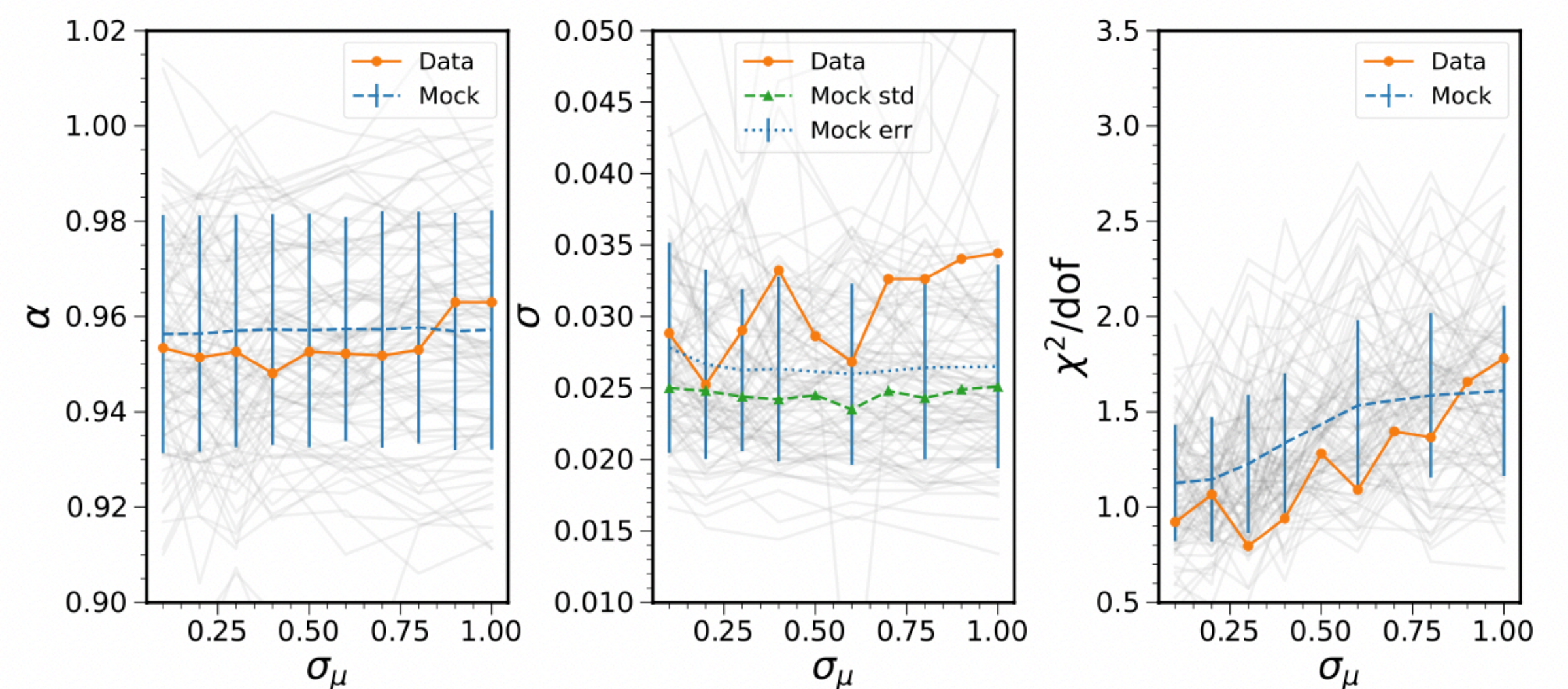
Testing the stacking window on mocks

- Gaussian window behaves more stably as the width of the window decreases b/c it gives more weight to the pairs with high S/N

Top-hat



Gaussian



**More stable mean and error bar estimates, more consistent χ^2/dof ,
Gaussian window is preferred**

ξ_p covariance

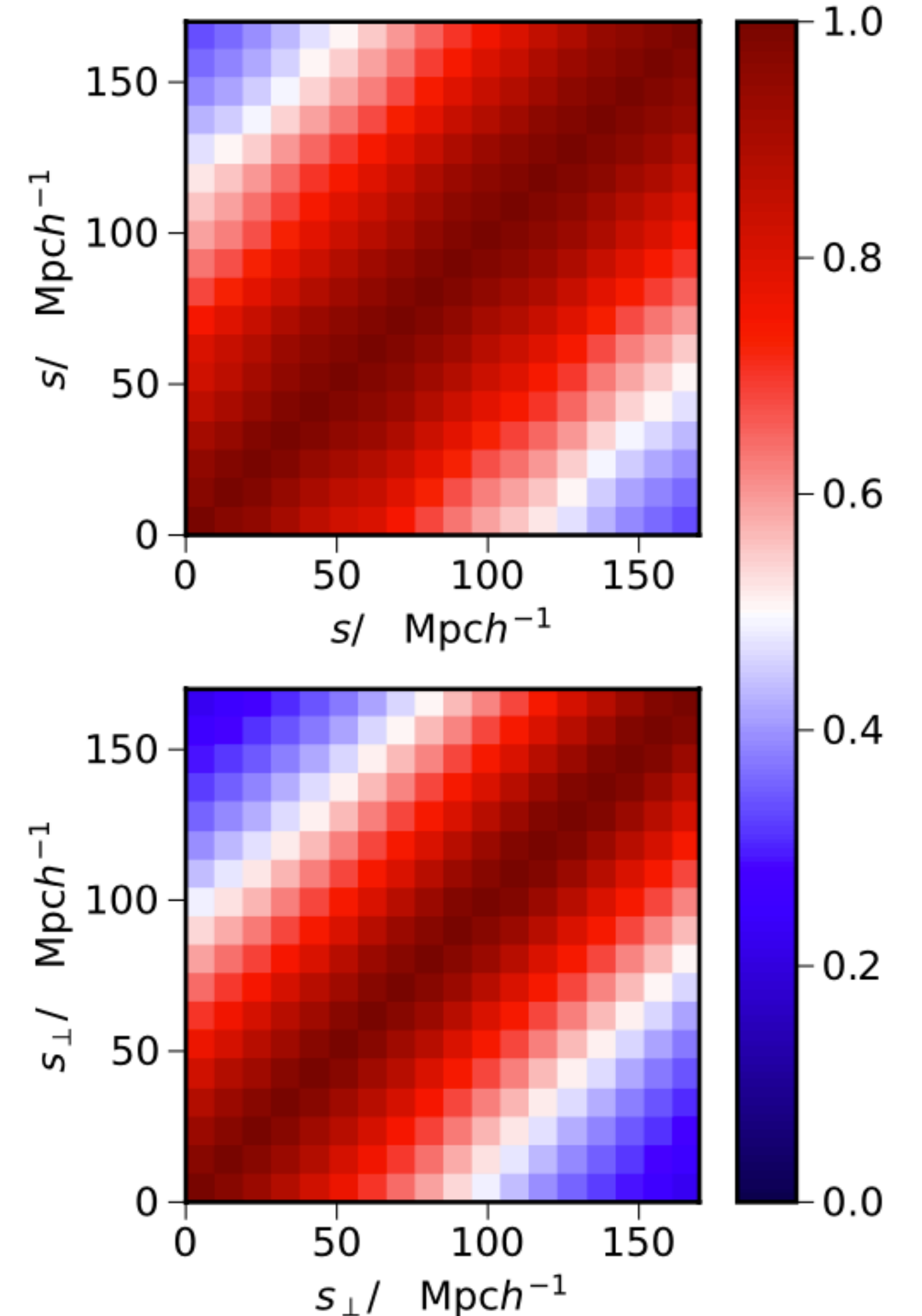
- Mapping the general w covariance to ξ_p one

$$\begin{aligned} & \text{Cov}[\xi_p(s_\perp), \xi_p(s'_\perp)] \\ = & \frac{\sum_i \sum_j W(\mu_i) W(\mu_j) \text{Cov}(\xi_p(s, \mu_i), \xi_p(s', \mu_j))}{\sum_i W(\mu_i) \sum_j W(\mu_j)} \end{aligned}$$

$$\text{Cov}[\hat{w}_{ij}(\theta), \hat{w}_{mn}(\theta')] = \sum_\ell \frac{(2\ell + 1)}{(4\pi)^2 f_{\text{sky}}} \bar{\mathcal{L}}_\ell(\cos \theta) \bar{\mathcal{L}}_\ell(\cos \theta')$$

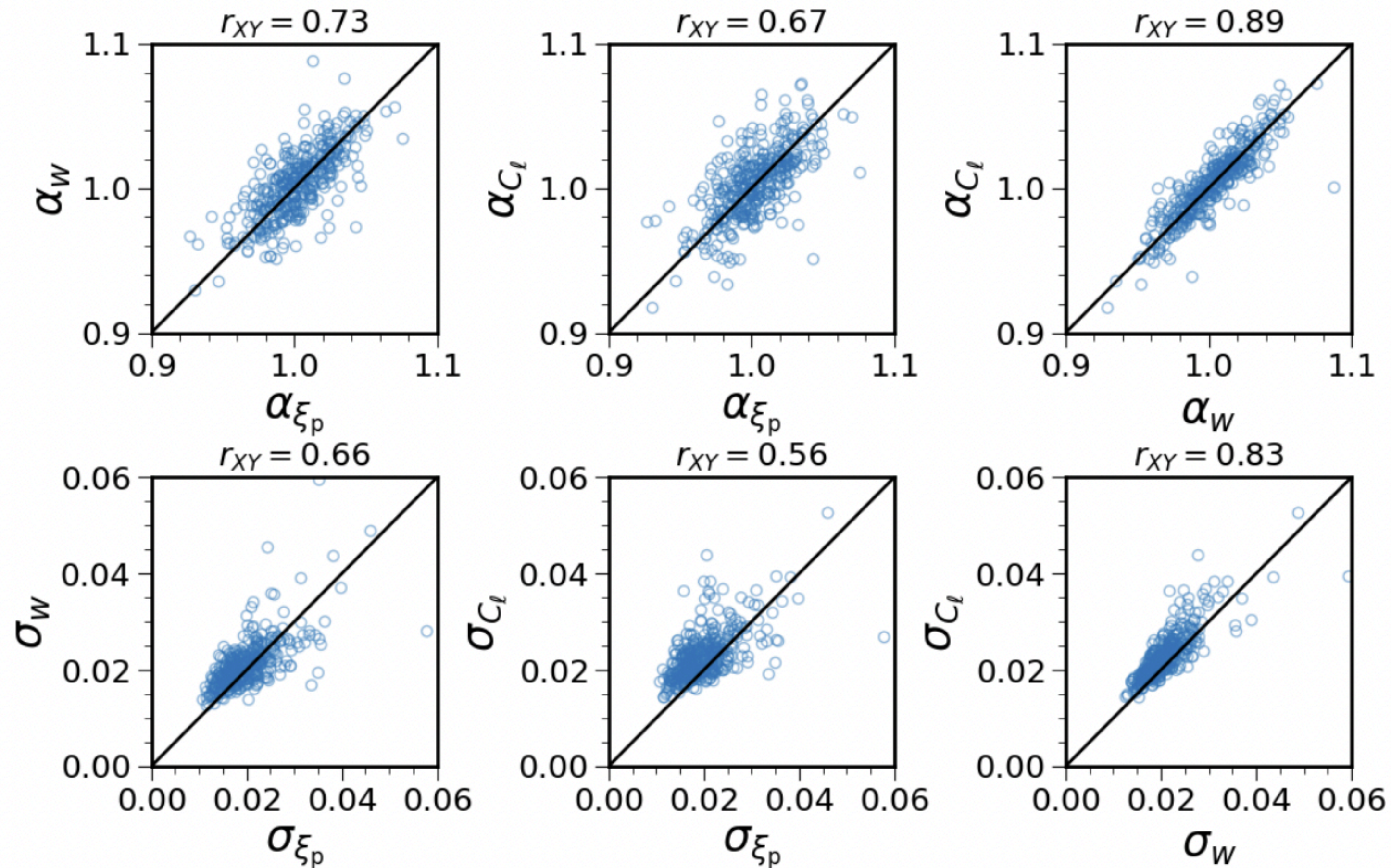
$$\left[\left(C_\ell^{im} + \frac{\delta_K^{im}}{\bar{n}_i} \right) \left(C_\ell^{jn} + \frac{\delta_K^{jn}}{\bar{n}_j} \right) + \left(C_\ell^{in} + \frac{\delta_K^{in}}{\bar{n}_i} \right) \left(C_\ell^{jm} + \frac{\delta_K^{jm}}{\bar{n}_j} \right) \right]$$

Finite bin width correction
Mask correction



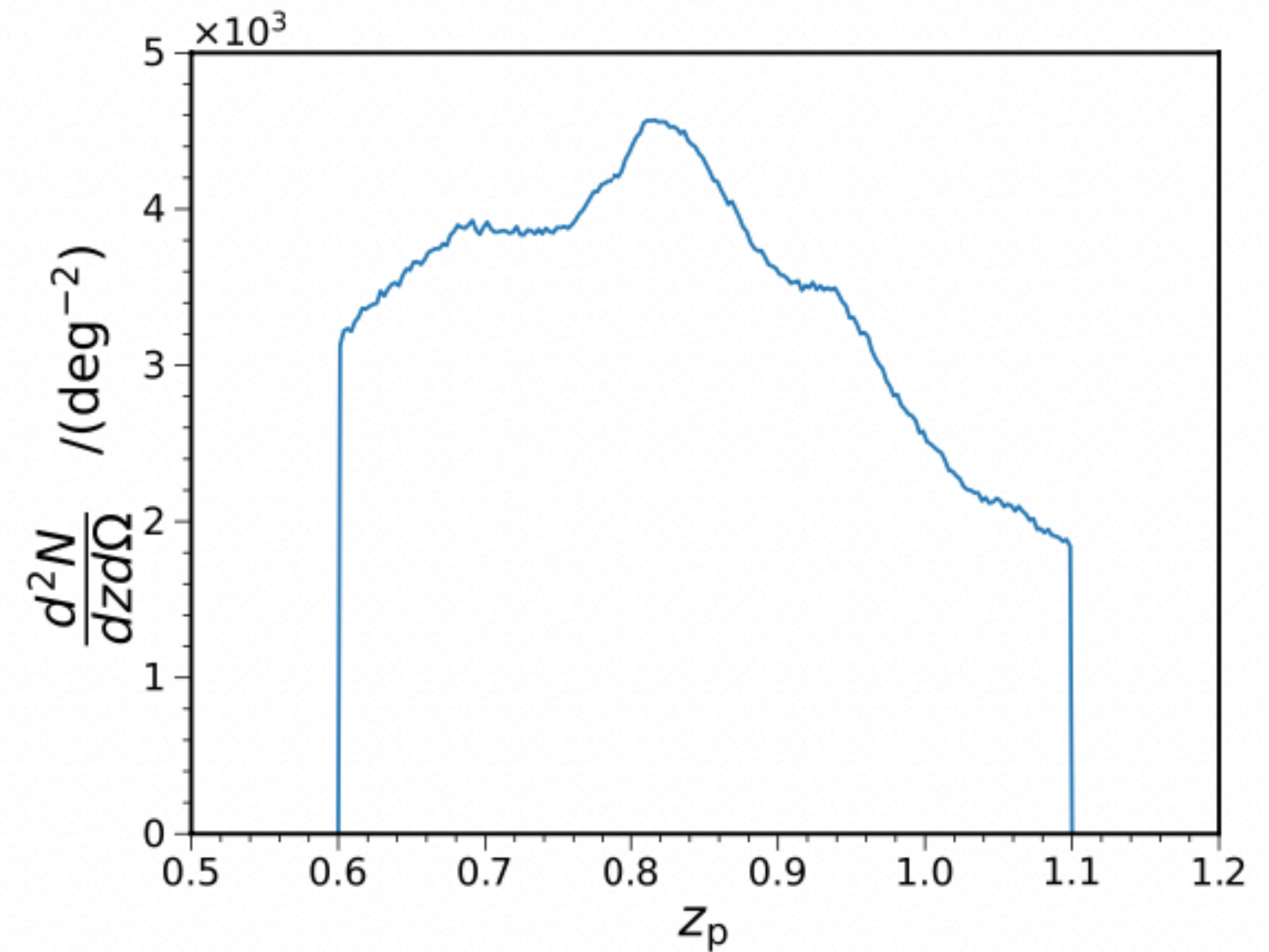
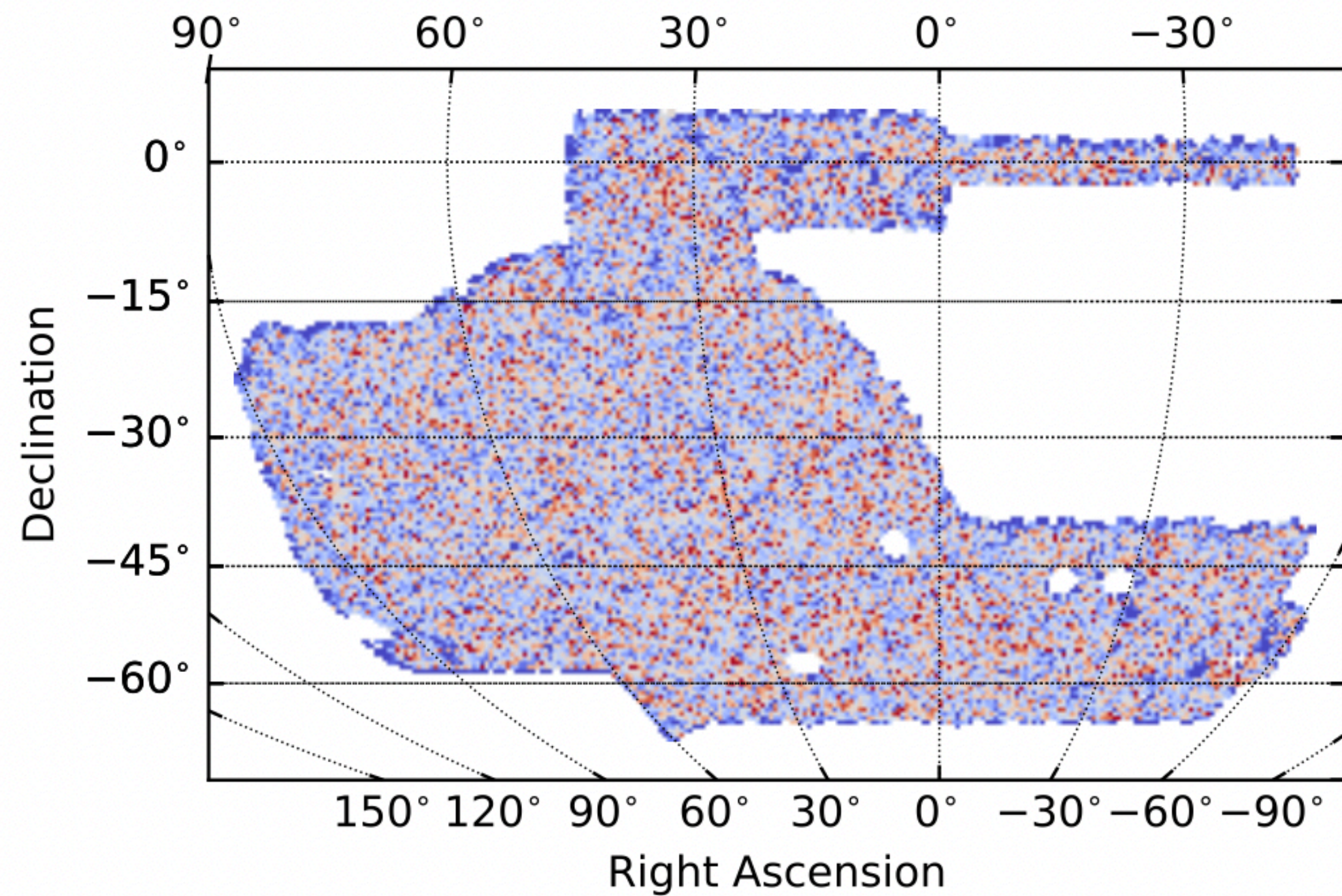
Correlation btw ξ_p and angular statistics

- The correlation btw ξ_p and angular statistics (w or C_ℓ) is low, serves as a more independent statistic



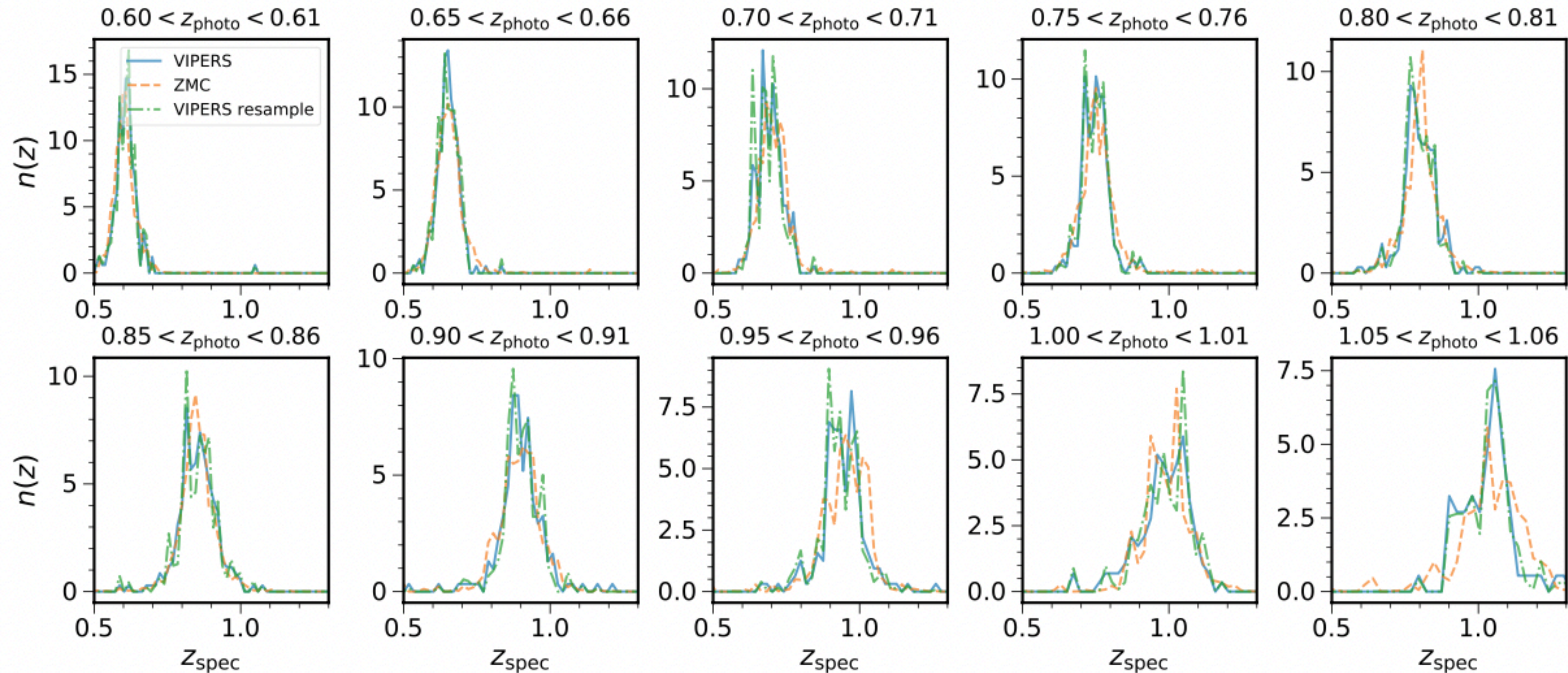
BAO sample

- BAO sample, 7.03 million red galaxies in the redshift range of [0.6,1.1] over a footprint of 4108 deg²



True-z distribution

- Photo-z derived from DNF, true redshift distribution estimated with the VIPERS spec-z sample

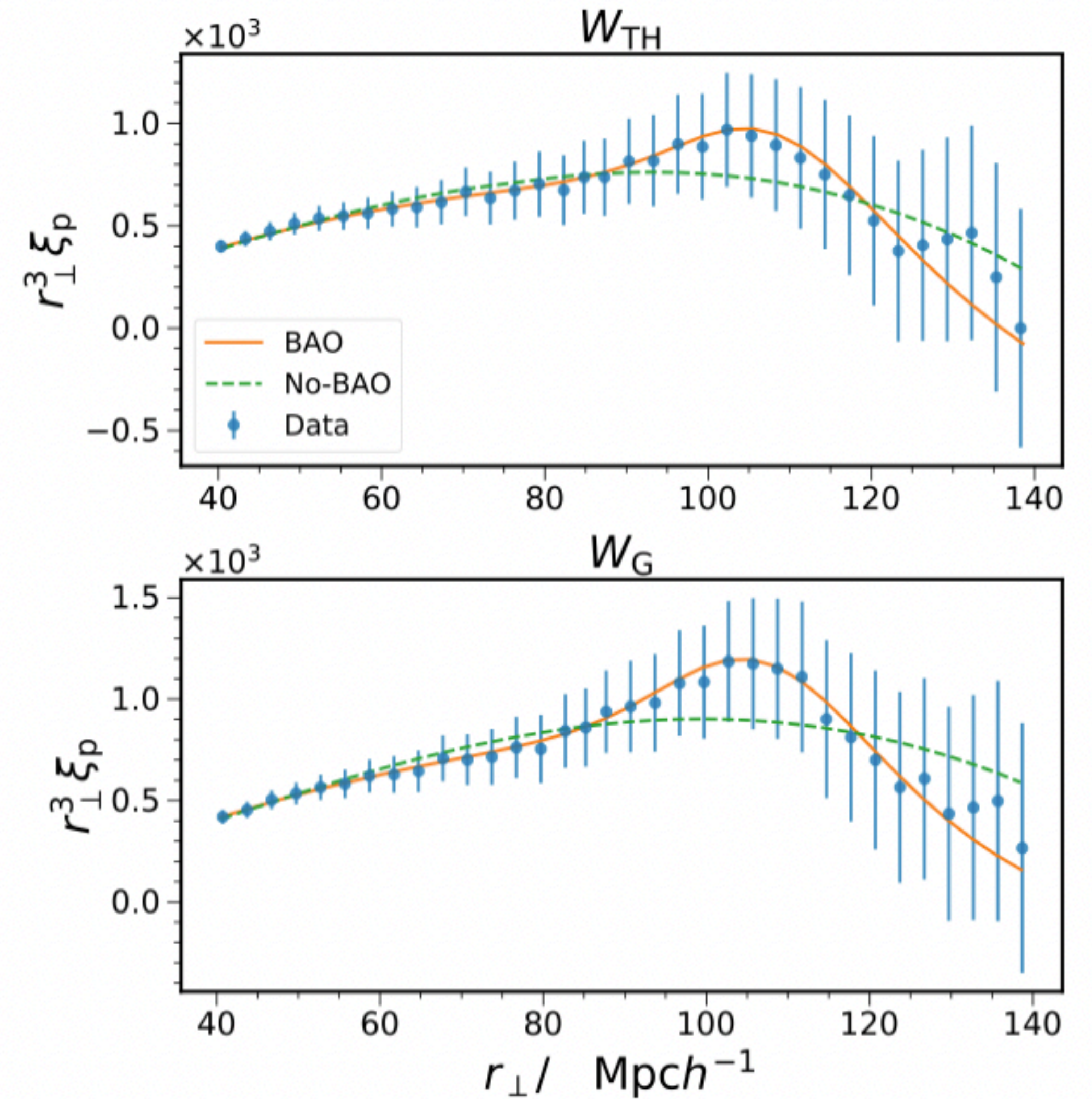


BAO measurements

- ξ_p constraint on α : 0.953 ± 0.029 (Gaussian) and 0.945 ± 0.033 (Top-hat)
- Consistent with w : 0.937 ± 0.025
- Deviation from Planck is reduced to 1.6σ

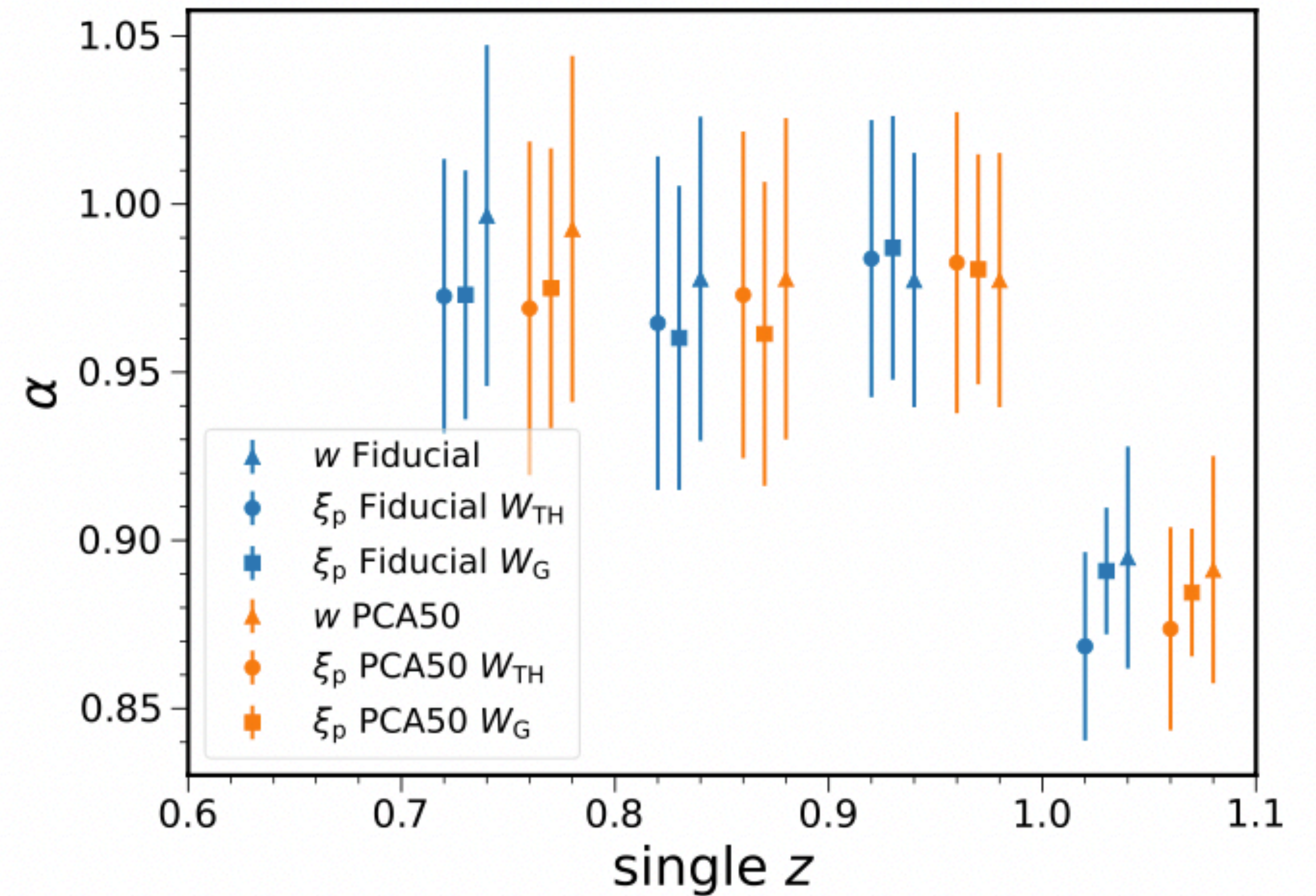
Planck fiducial cosmology, $\alpha = 1$

$$\alpha = \frac{\frac{D_M}{r_d} |_{\text{data}}}{\frac{D_M}{r_d} |_{\text{fid}}}$$



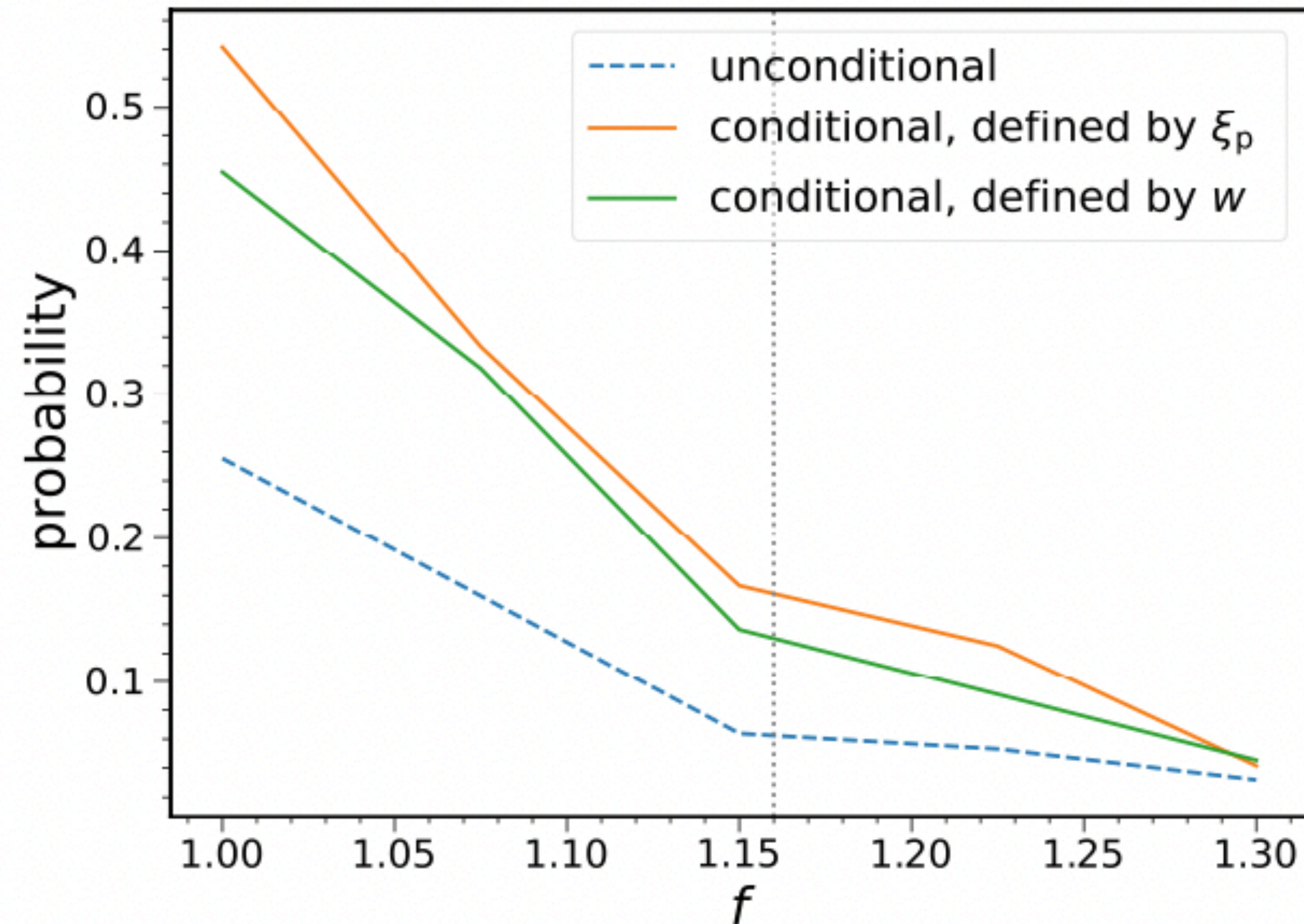
Individual bin fit results

- Individual tomographic bins, ξ_p gives comparable or even tighter constraint than w
- The BAO signals are heterogeneous across redshift, deviation from Planck mainly driven by the last bin



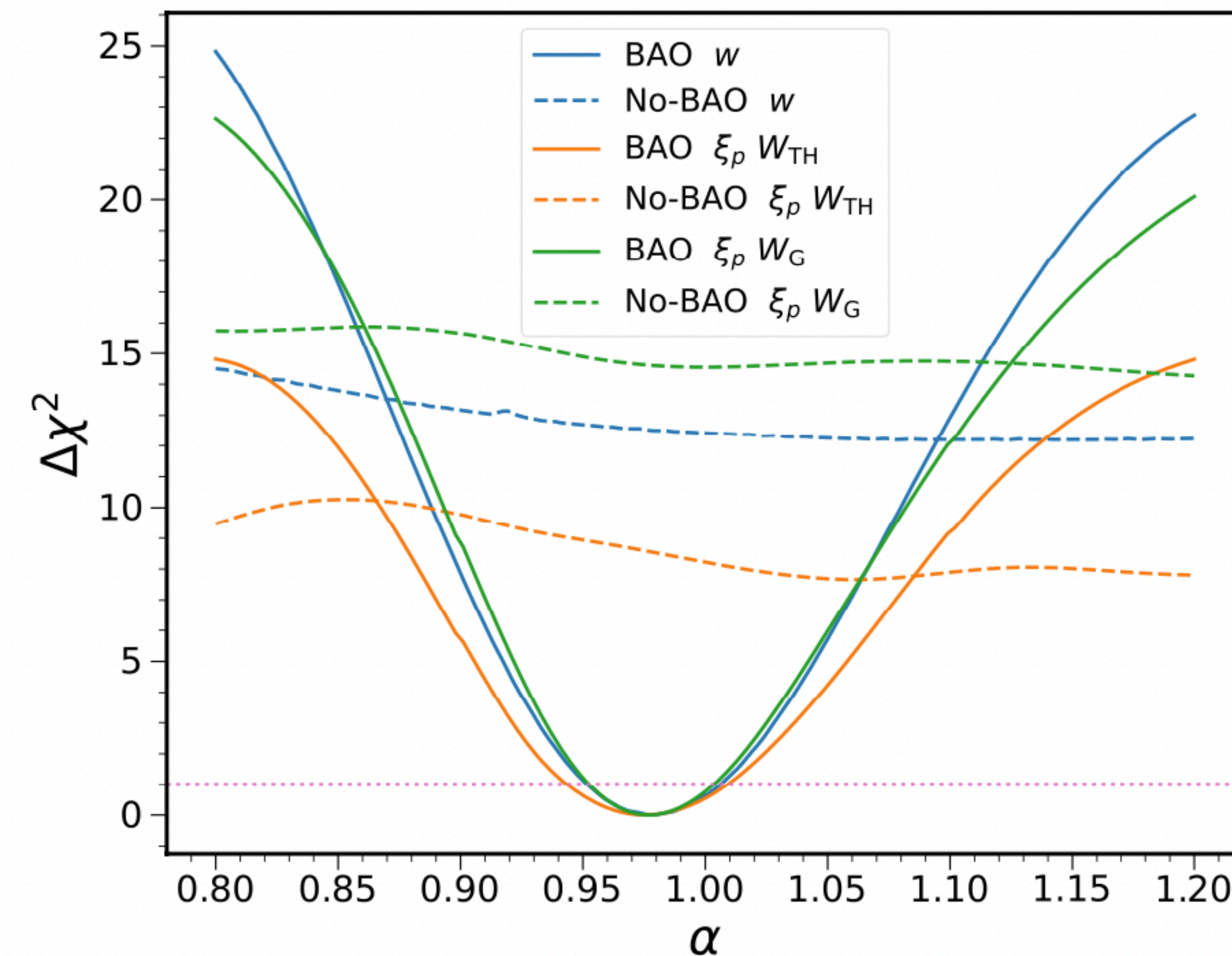
Error bars in heterogeneous mocks

- In heterogeneous mocks, the probability of getting ξ_p with error bar larger than w is enhanced



Measurements in homogeneous sample

- The combo 2-4 bins contains consistent BAO signals, the resultant constraint from 0.977 ± 0.026 (Gaussian) and 0.975 ± 0.033 (Top-hat) vs 0.978 ± 0.027 (w)
- ξ_p combines the signals at the level of data vector, while w effectively combines likelihood
- Caveat: combining likelihood always shrinks the error bar



Robustness tests

- ξ_p is generally more sensitive to photo-z noise than w b/c (1) it measures correlation after projection (2) it combines signals at the level of data vector
- Gaussian window is more stable than top-hat as it puts more weight to the transverse pairs

Case	$\xi_p: W_G$	$\xi_p: W_{TH}$	w
Default	0.953 ± 0.029 (21.5/29)	0.945 ± 0.033 (33.4/29)	0.937 ± 0.025 (95.2/89)
No sys. corr.	0.942 ± 0.029 (39.7/29)	* 0.938 ± 0.033 (46.4/29)	0.935 ± 0.026 (94.6/89)
sys – PCA50	0.945 ± 0.029 (22.8/29)	0.943 ± 0.028 (36.0/29)	0.937 ± 0.025 (94.9/89)
$n(z)$ Z_MC	0.948 ± 0.029 (21.6/29)	* 0.943 ± 0.034 (33.6/29)	0.935 ± 0.025 (95.6/89)
MICE template	0.989 ± 0.038 (53.5/29)	* 0.988 ± 0.032 (78.5/29)	0.980 ± 0.026 (95.1/89)
MICE cov.	0.956 ± 0.021 (23.7/29)	* 0.955 ± 0.025 (41.0/29)	0.936 ± 0.021 (125.8/89)
MICE cosmology	0.996 ± 0.026 (59.3/29)	0.995 ± 0.021 (90.7/29)	0.977 ± 0.022 (125.8/89)
Unmodified cov.	0.956 ± 0.030 (21.3/29)	0.953 ± 0.035 (32.7/29)	—
[70, 130] Mpc h^{-1}	0.955 ± 0.030 (11.7/16)	0.965 ± 0.031 (17.1/16)	—
$\Delta r = 5$ Mpc h^{-1}	0.953 ± 0.030 (19.1/15)	0.953 ± 0.036 (16.2/15)	—
$\Delta r = 2$ Mpc h^{-1}	0.949 ± 0.028 (38.1/44)	0.941 ± 0.031 (44.5/45)	—
No bin 1	0.976 ± 0.024 (29.5/29)	* 0.960 ± 0.030 (38.7/29)	0.948 ± 0.026 (67.8/71)
No bin 2	0.928 ± 0.034 (19.0/29)	* 0.931 ± 0.034 (32.4/29)	0.929 ± 0.026 (80.7/71)
No bin 3	0.938 ± 0.034 (27.0/29)	* 0.941 ± 0.038 (38.7/29)	0.935 ± 0.028 (78.4/71)
No bin 4	0.928 ± 0.033 (24.7/29)	* 0.943 ± 0.034 (38.8/29)	0.925 ± 0.028 (70.0/71)
No bin 5	0.950 ± 0.030 (21.5/29)	* 0.959 ± 0.029 (40.6/29)	0.967 ± 0.026 (82.3/71)

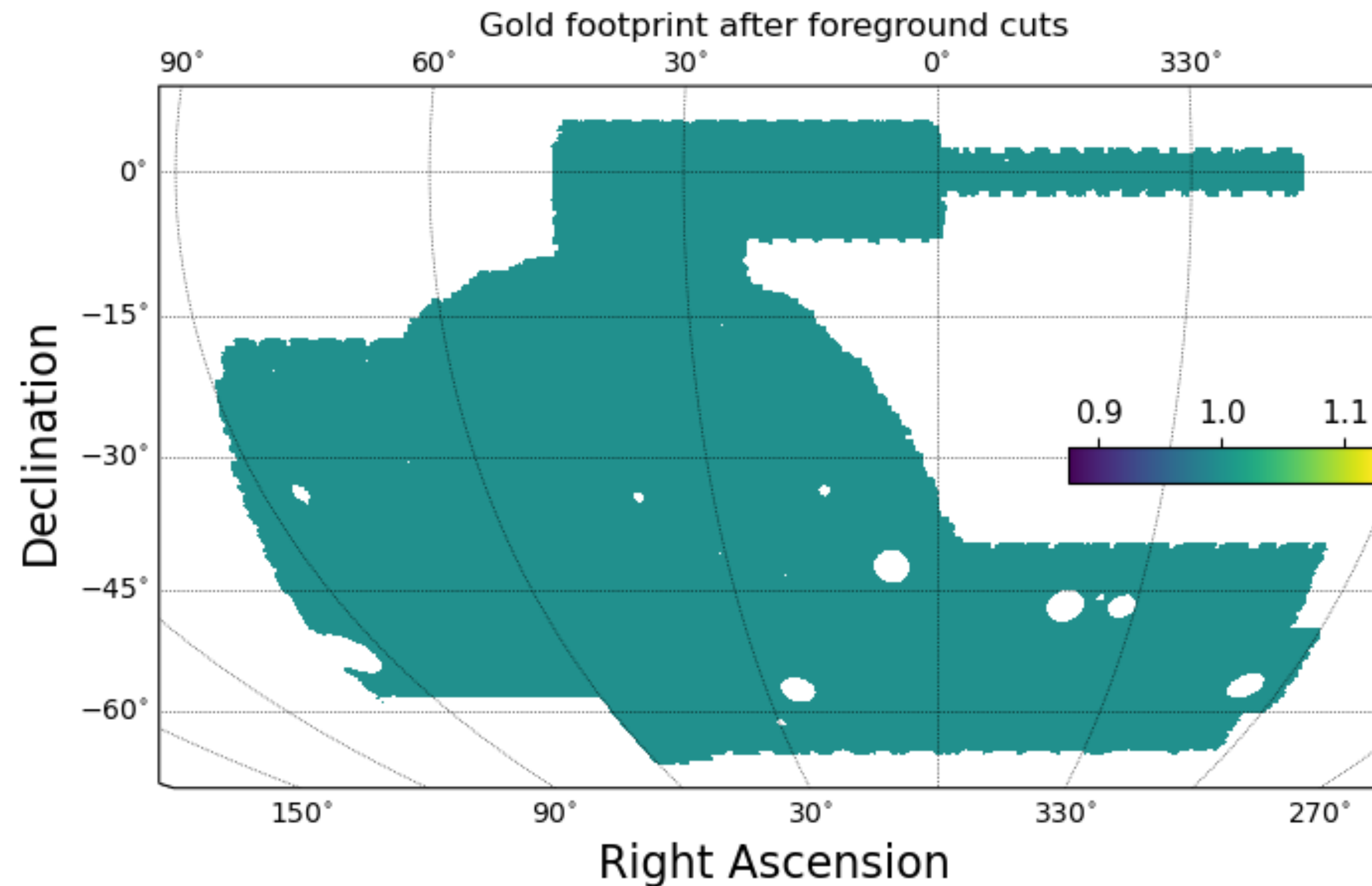
Angular vs Projected 3D

	Angular analysis Projection and then clustering measurement	Projected 3D Clustering measurement and then projection
Pros	Angle only, cosmology-independent	Effective to condense the data Include some radial info
Cons	Explicit bin division, loss of radial info	Need cosmology for distance computation More sensitive to noise

Both statistics offer important crosschecks on each other.

Y6 BAO analysis

- Same footprint, but deeper magnitude
- ξ_p , along with angular statistics, is adopted for fiducial Y6 BAO analysis



Conclusions

- Using DES Y3 data, we apply the 3D correlation function to measure the BAO on a red galaxy sample with 7 million galaxies in the redshift range of [0.6,1.1] over a field of 4180 deg².
- Modeling includes general photo-z distribution and more robust Gaussian window function is considered
- We find $D_M/r_d = 19.15 \pm 0.58$ (Gaussian) and $D_M/r_d = 19.00 \pm 0.67$ (Top-hat).
The constraint is weaker than w b/c the sample is heterogeneous in BAO signals and for the combo 2-4 bins, the constraint from ξ_p is indeed stronger
- The deviation from Planck is reduced from 2.5 sigma to 1.6 sigma.
- ξ_p is complementary to the angular statistics, serve as useful crosscheck, one of the fiducial statistics in Y6 BAO analysis