



# Imprints of cosmic reionization as a probe of dark matter nature in the post-reionization era

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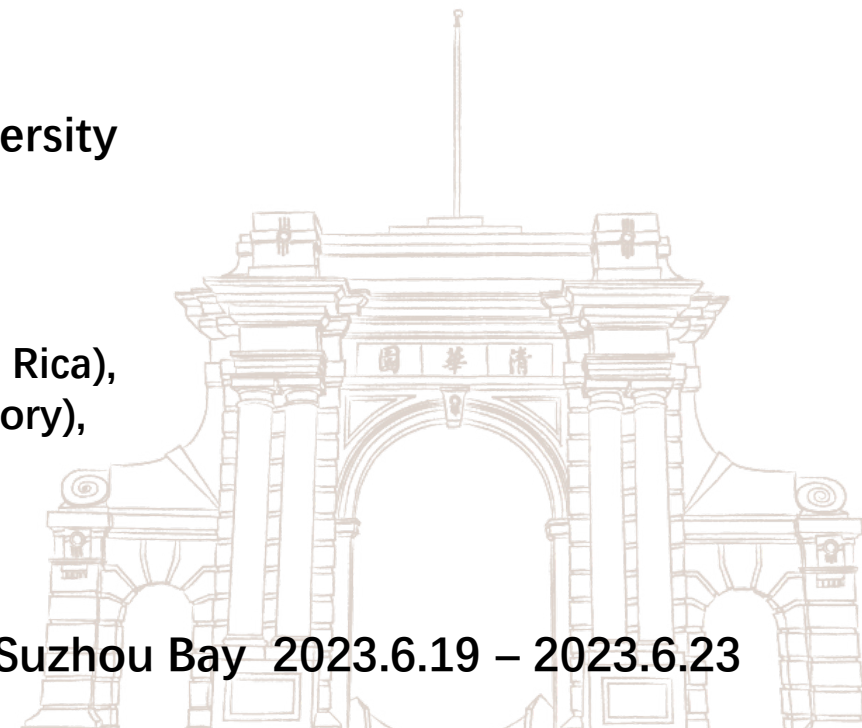
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Heyang Long (The Ohio State University),

Christopher Hirata (The Ohio State University).

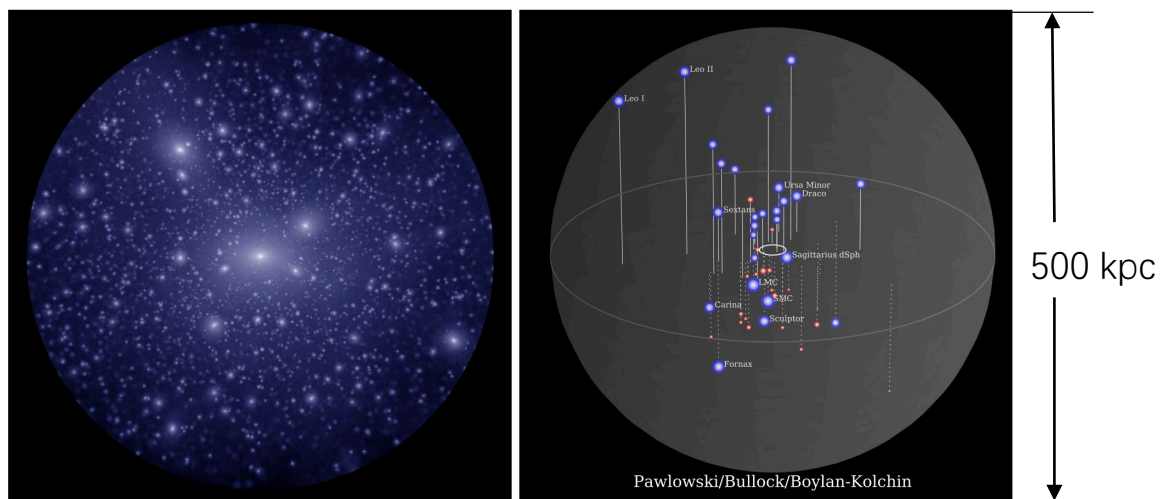




# Small-scale challenges to the $\Lambda$ CDM model



## Missing Satellites Problem

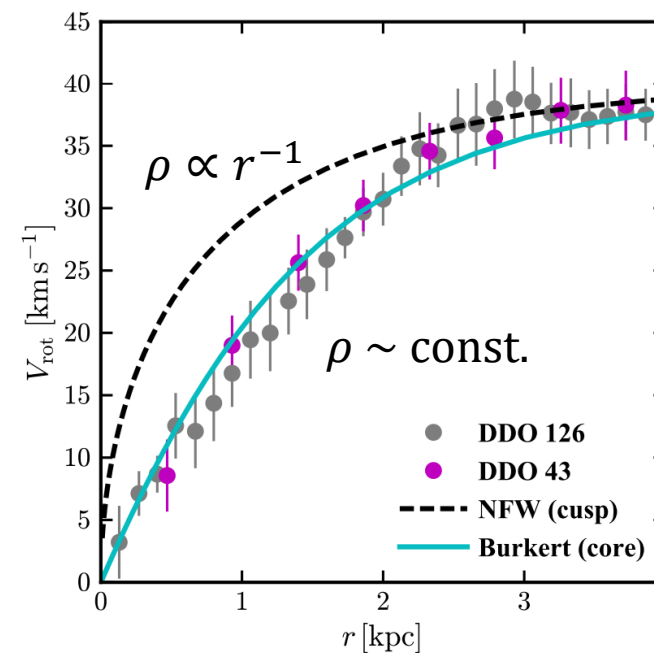


N-body simulation

observed satellite galaxies

(Bullock et al. 2017)

## Cusp-Core Problem



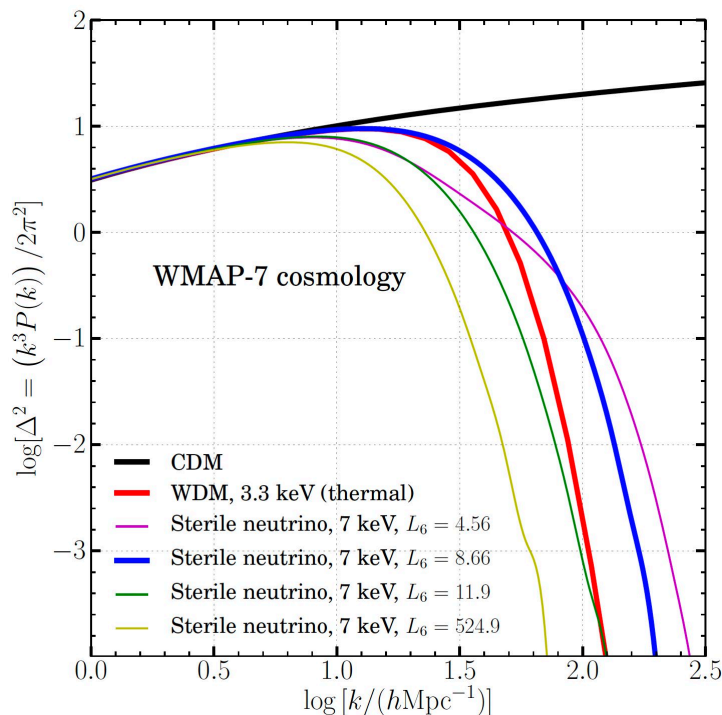
(Bullock et al. 2017)



# Other DM models: small-scale suppression

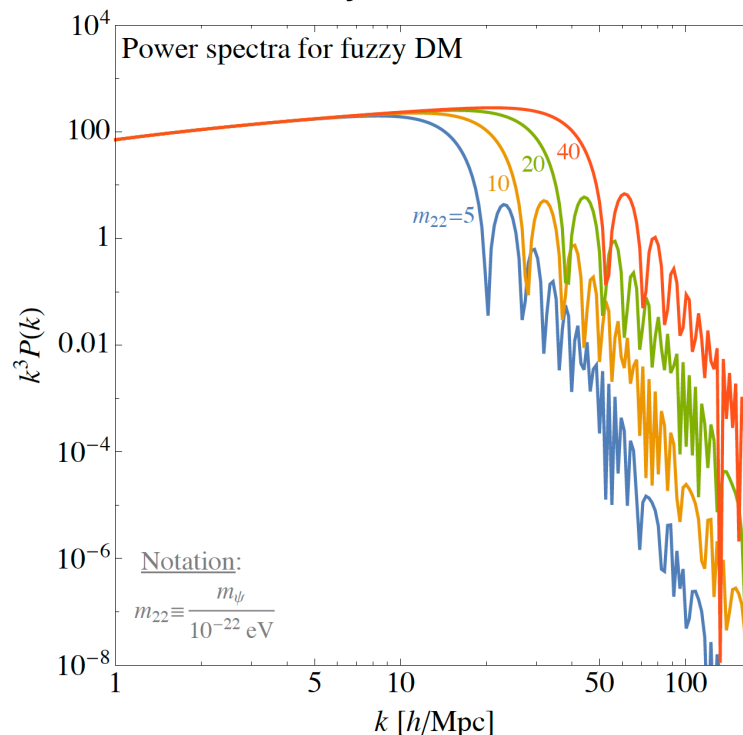


### Warm Dark Matter



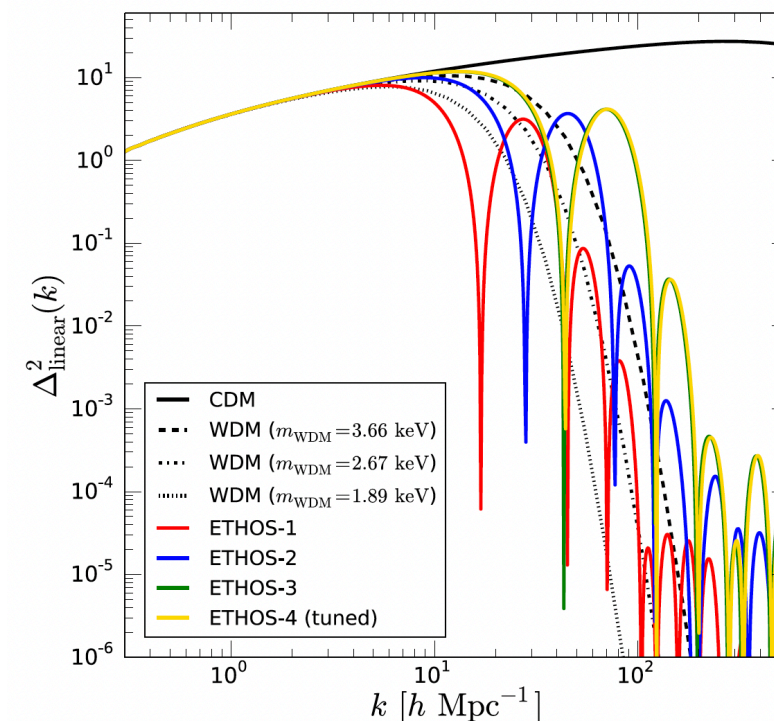
(Bose et al. 2016)

### Fuzzy Dark Matter



(Murgia et al. 2017)

### ETHOS

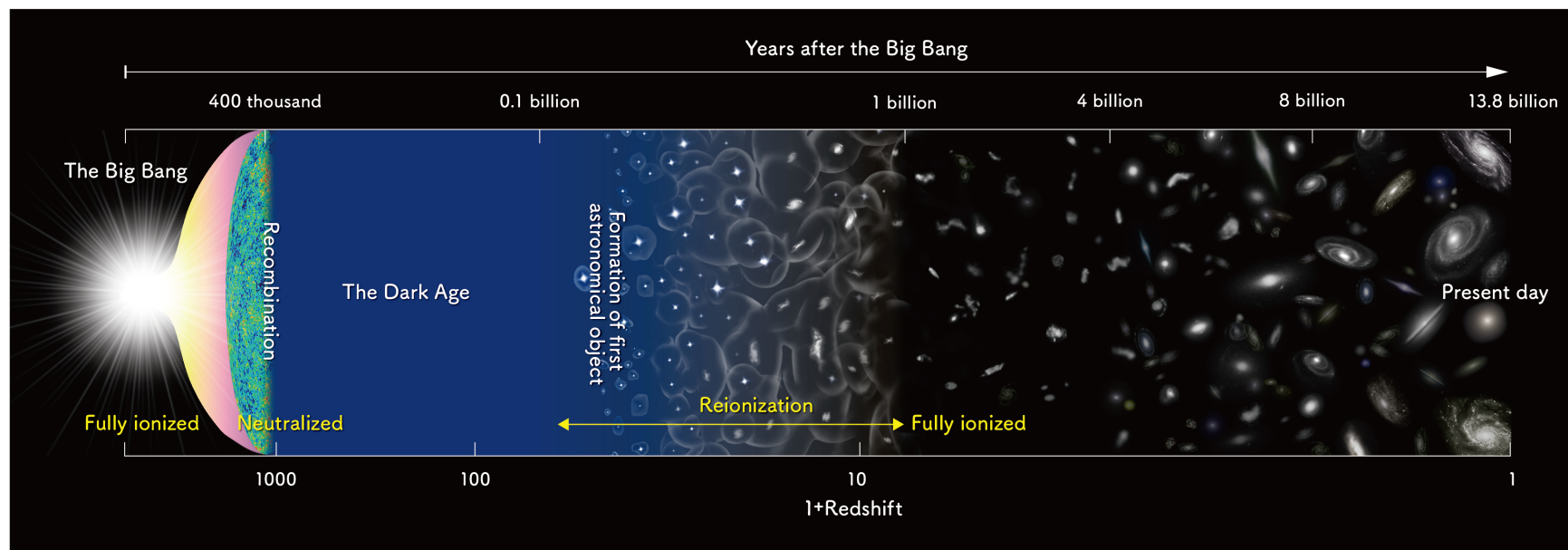


(Vogelsberger et al. 2015)

suppression on small scales: hard to observe



# Reionization



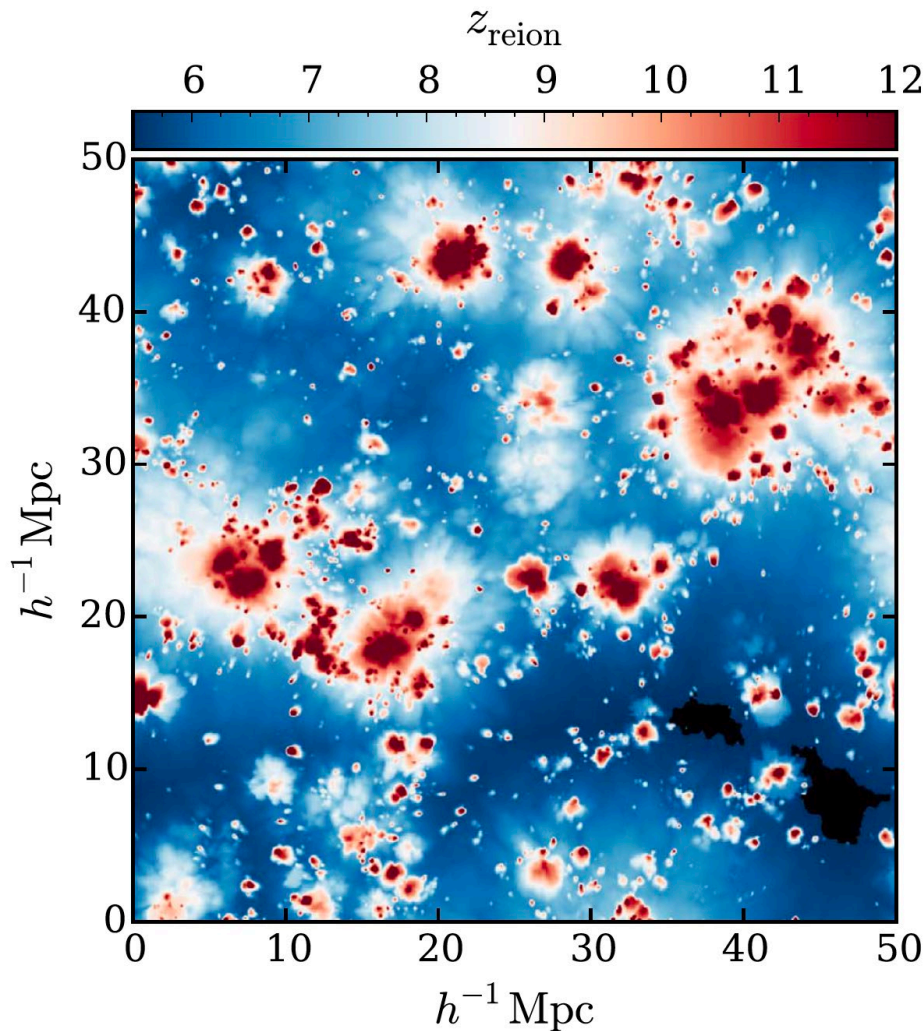
(NAOJ)

H I, He I  $\rightarrow$  H II, He II

photoionization heating: T of order  $10^4$  K



# Thermal imprints couple to reionization bubble

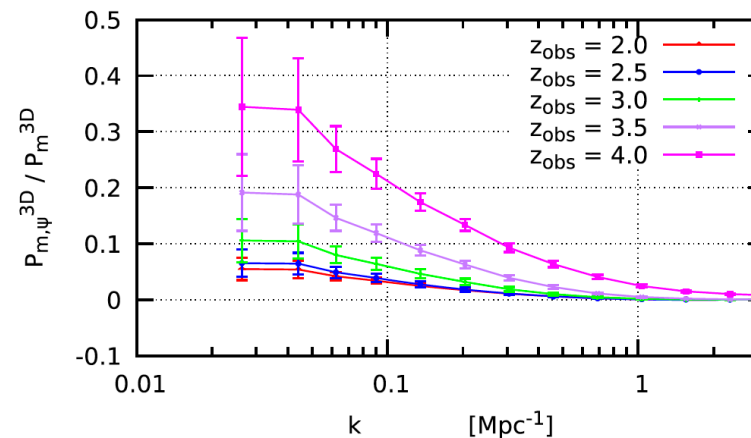
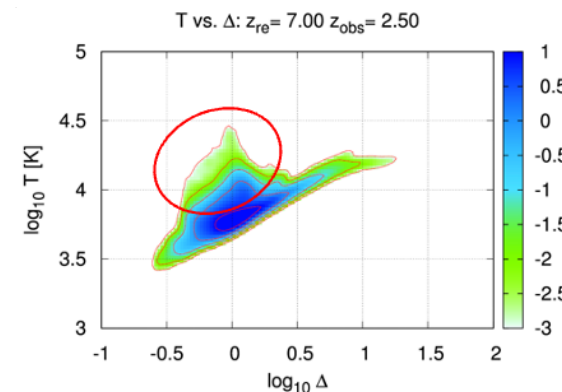


(D'Aloisio et al. 2019)

Different positions reionize at different redshifts.

Small scales: **high-entropy, mean-density gas** (Hirata 2018)  
memory: when reionization happens

couple  
bubbles scale

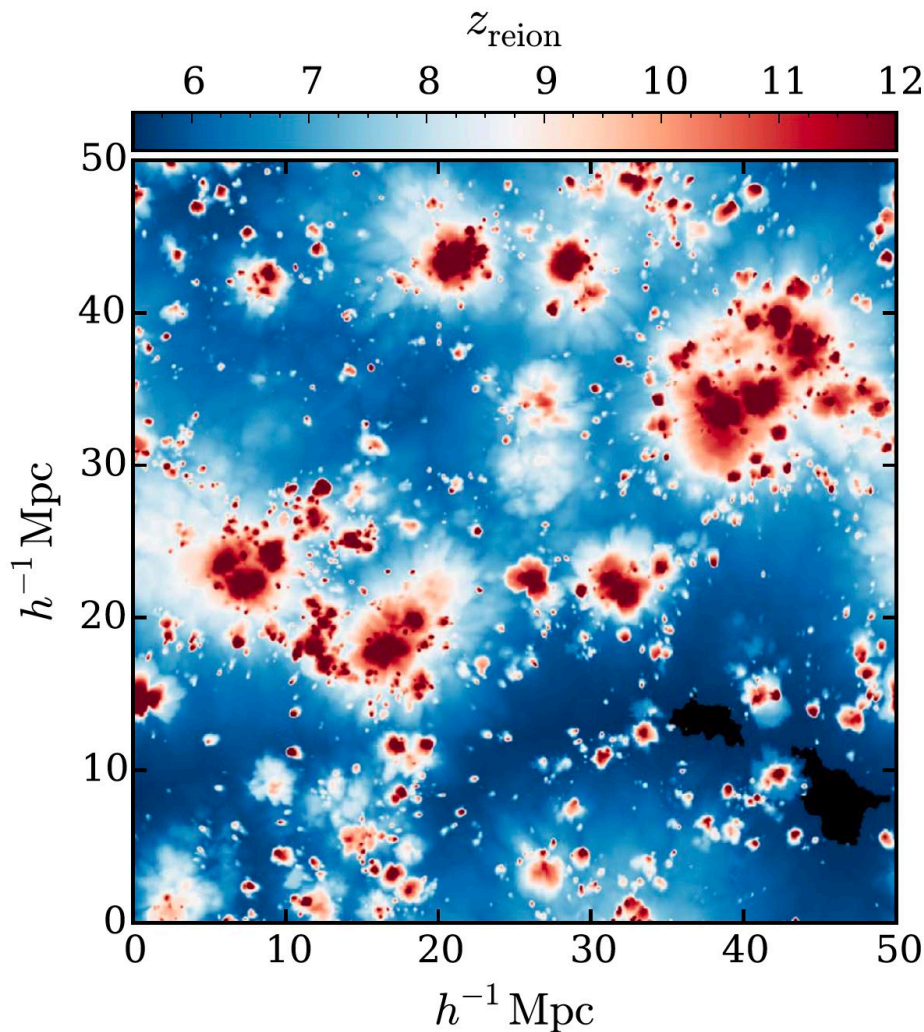


Impact of reionization on Ly $\alpha$  forest power spectrum:  
**enhancement on large scales**

(Montero-Camacho et al. 2019)



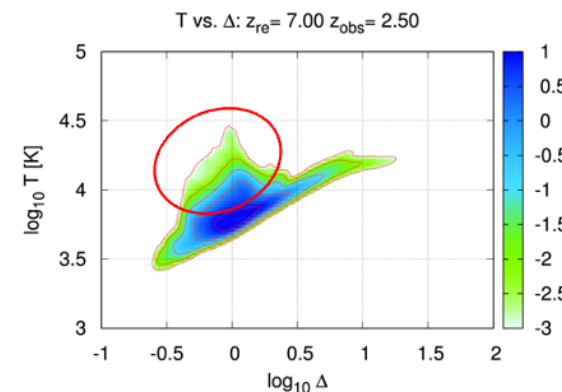
# Thermal imprints couple to reionization bubble



(D'Aloisio et al. 2019)

Small scales: **high-entropy, mean-density gas** (Hirata 2018)  
memory: when reionization happens

couple  
←→  
bubbles scale



**Small-scale suppression:**

evolution of IGM

+ process of reionization

Different positions reionize at different redshifts.



# Ly $\alpha$ forest 3D power spectrum in WDM model



**Thermal relics:** form in thermal equilibrium and decouple while being relativistic.  
e.g. gravitino

$$P_F^{3D}(k, \mu, z_{\text{obs}}) = b_F^2(1 + \beta_F \mu^2)^2 P_m(k, z_{\text{obs}}) + 2b_F b_\Gamma(1 + \beta_F \mu^2) P_{m,\psi}(k, z_{\text{obs}}) \quad (\text{Montero-Camacho et al. 2019})$$

conventional power spectrum

impact of inhomogeneous reionization

$$\psi(z_{\text{re}}) = \ln[\tau_1(z_{\text{re}})] - \ln[\tau_1(\bar{z}_{\text{re}})] \quad \text{how **transparency** of gas varies with } z_{\text{re}}$$

optical depth:  $\tau = \tau_1 \Delta^2 \alpha_A(T)$  **higher  $\tau_1$** : gas is more **transparent**

$$\langle F \rangle = \langle e^{-\tau} \rangle = \frac{1}{N} \sum_{i=1}^N \exp(-\tau_1 \Delta_i^2 \alpha_A(T_i)) \quad \langle F \rangle = \exp(-0.0023 a^{-3.65}) \quad (\text{Kim, Bolton \& Viel 2007})$$



# Hybrid method



impact of inhomogeneous reionization: 
$$P_{m,\psi}(k, z_{\text{obs}}) = - \int_{z_{\text{min}}}^{z_{\text{max}}} \frac{\partial \psi(z_{\text{obs}}, z_{\text{re}})}{\partial z_{\text{re}}} P_{m, \text{xHI}}(z_{\text{re}}, k) \frac{D(z_{\text{obs}})}{D(z_{\text{re}})} dz_{\text{re}}$$

Small scale: high-resolution hydrodynamical simulation

**Gadget-2** box size: 1275 kpc

Particle mass:  $9.72 \times 10^3 M_{\odot}$  (DM),  $1.81 \times 10^3 M_{\odot}$  (gas)

**redshift of reionization:  $z_{\text{re}} = 6, 7, 8, 9, 12$  calculate  $\psi(z_{\text{re}})$**

Large scale: semi-analytic model

**21CMFAST** box size: 400 Mpc

$256^3$  HI cells and  $768^3$  matter density cells

**Implement WDM:**  $m_{\text{x}} = \{3, 4, 6, 9\}$  keV

$P_{\text{WDM}}(k) = T_{\text{x}}(k)^2 P_{\text{CDM}}(k)$  as initial condition

transfer function:  $T_{\text{x}}(k) = [1 + (\alpha k)^{2\nu}]^{-5/\nu}$  (Bode et al. 2001)

suppression scale:  $\alpha = 0.049 \left(\frac{m_{\text{x}}}{1 \text{ keV}}\right)^{-1.11} \left(\frac{\Omega_{\text{x}}}{0.25}\right)^{0.11} \left(\frac{h}{0.7}\right)^{1.22} h^{-1} \text{Mpc}$

$\nu = 1.12$  (Viel et al. 2005)

**Implement WDM:**

transfer function

+

**effective Jeans mass**

a new minimum mass that enters the mean collapse fraction

$$M_{\text{J}} \approx 1.5 \times 10^{10} \left(\frac{\Omega_{\text{x}} h^2}{0.15}\right)^{\frac{1}{2}} \left(\frac{m_{\text{x}}}{1 \text{ keV}}\right)^{-4} M_{\odot}$$

(Sitwell et al. 2014)

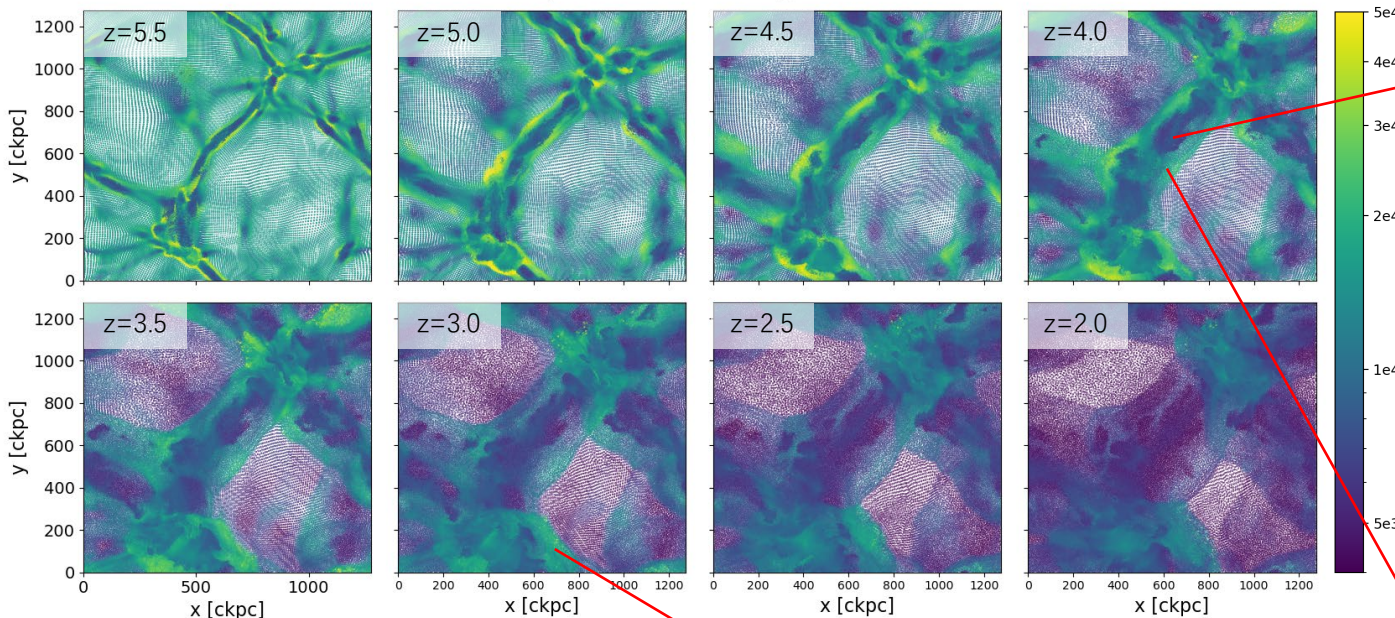




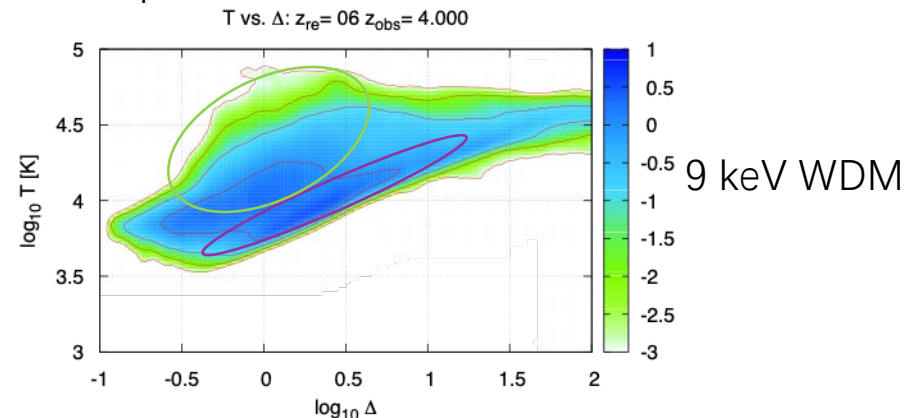
# Evolution of gas temperature



Temperature 9keV WDM  $z_{re} = 6$

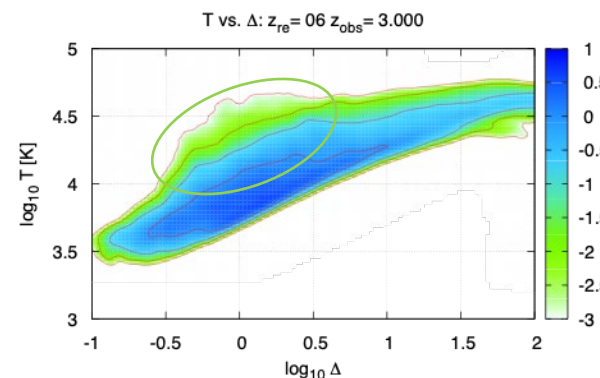


**Gas in dense structures (purple):**  
adiabatic expansion and photoionization heating  
->  $T - \Delta$  power-law relation



**Low and mean density gas around structures:**  
(yellow and green): compressed and heated

maintain relatively high temperature,  
deviate from power-law relation  
**high-entropy mean-density gas (Hirata, 2018)**

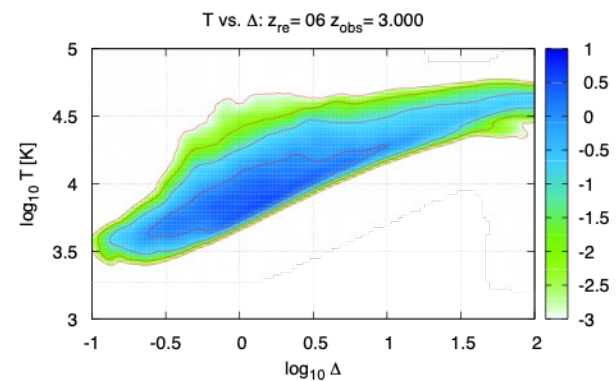
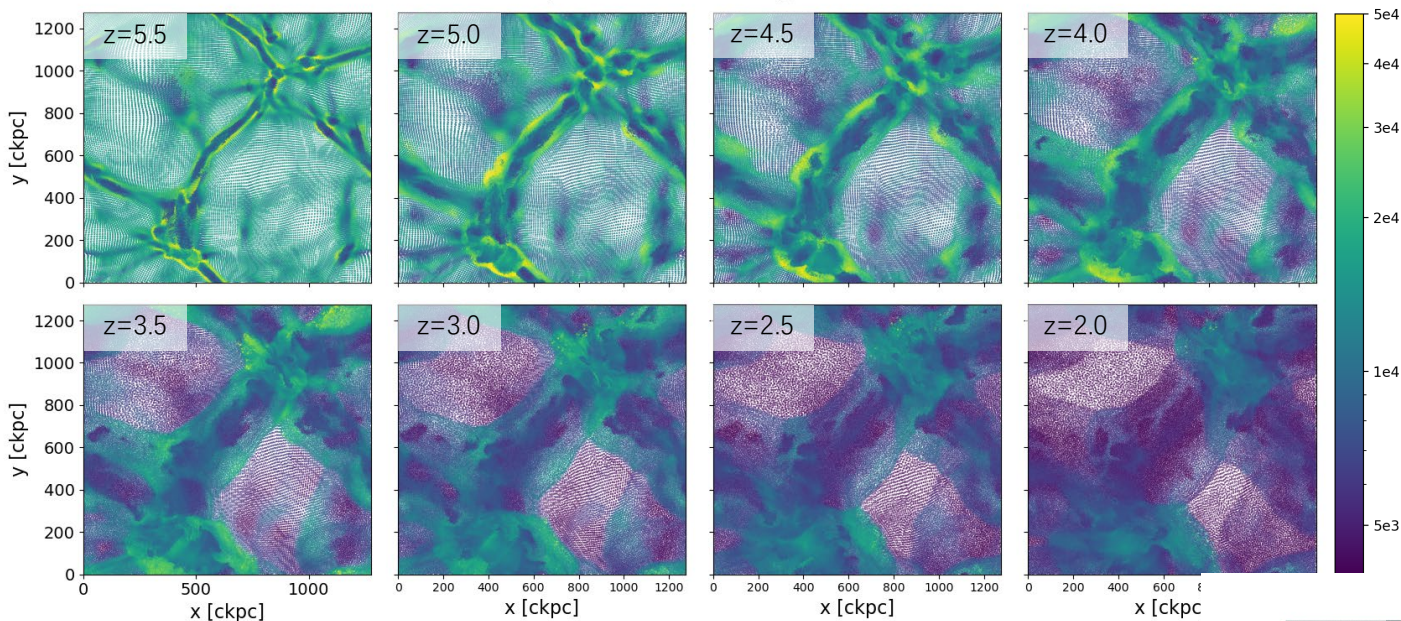




# Evolution of gas temperature

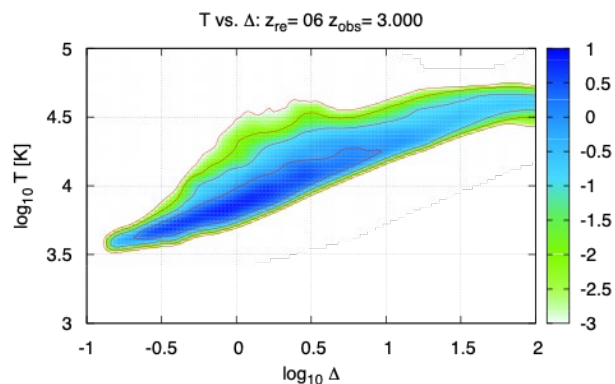


Temperature 9keV WDM  $z_{re} = 6$



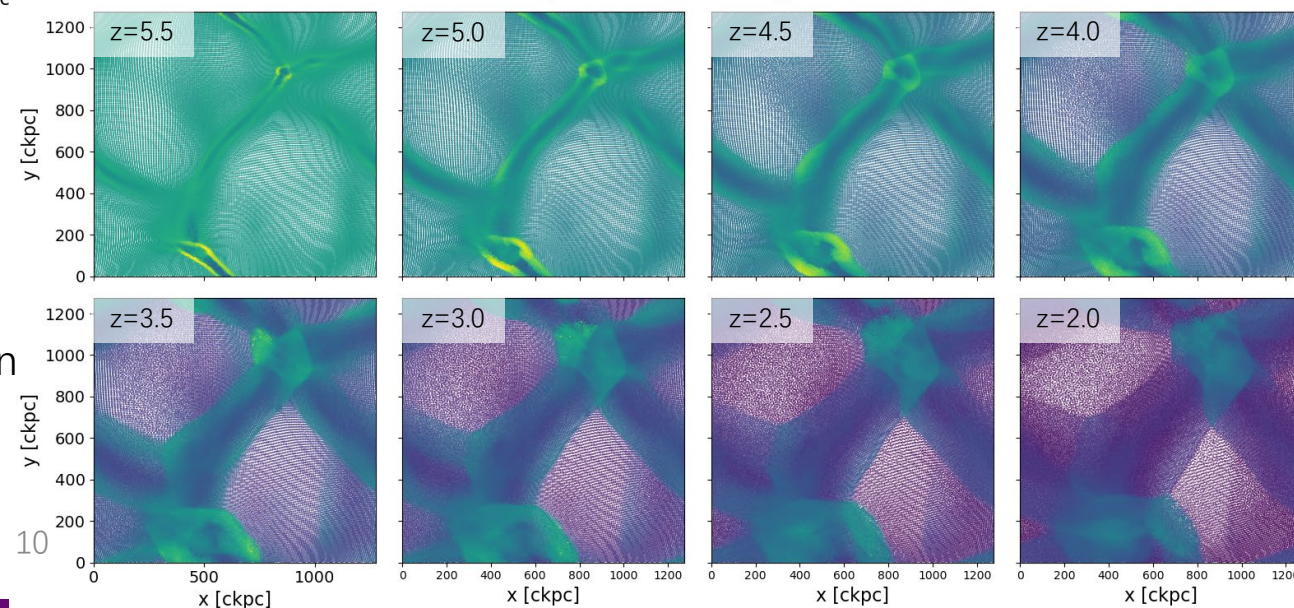
9 keV WDM

**Lighter** WDM model: expansion of dense gas and compression & heating of low density gas are **less violent**



3 keV WDM  
tighter power-law relation

Temperature 3keV WDM  $z_{re} = 6$

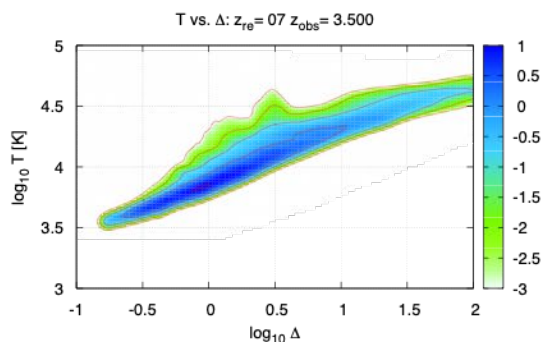




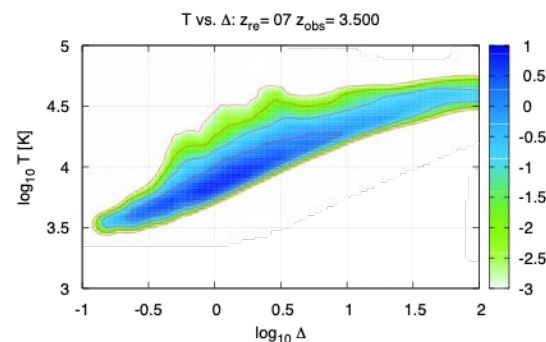
# Temperature-density relation



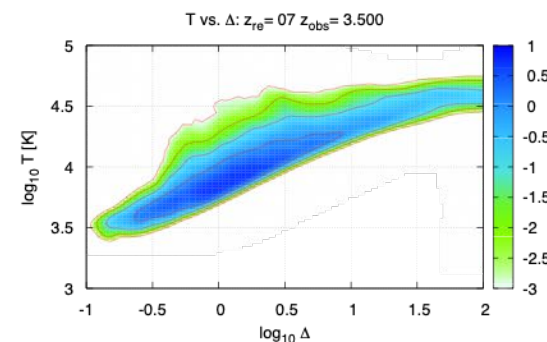
3 keV WDM



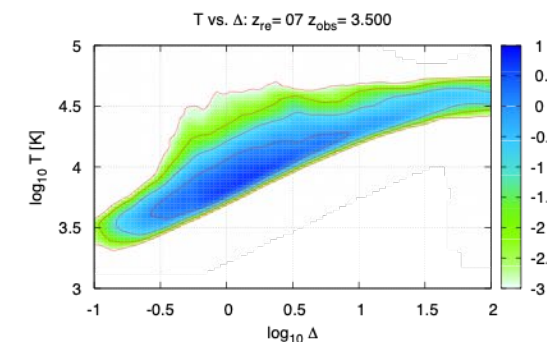
6 keV WDM



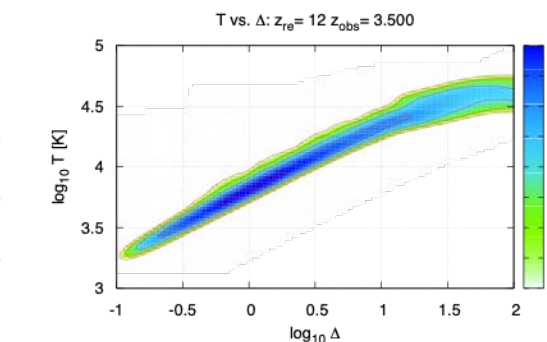
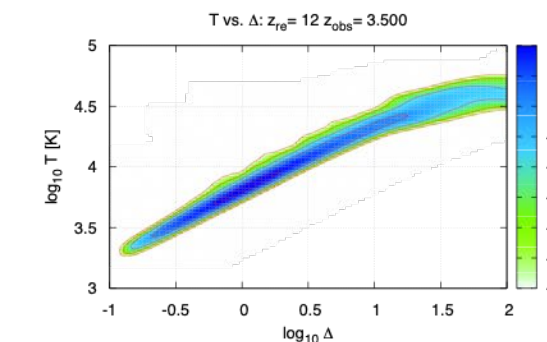
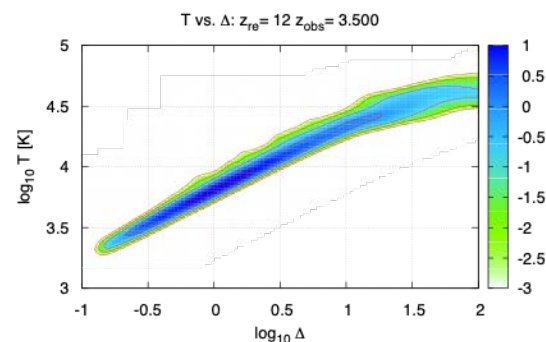
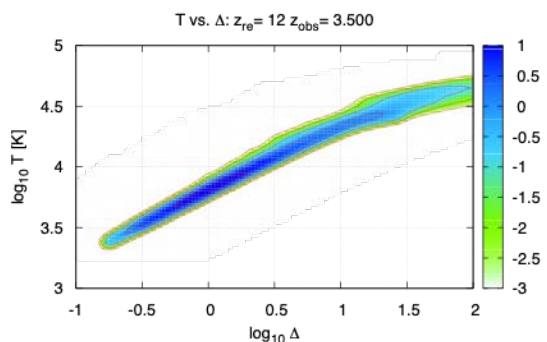
9 keV WDM



CDM



For late reionization ( $z_{re} \leq 8$ ), gas follows a tighter power-law relation in lighter WDM model.



For early reionization: gas has enough time to relax to power-law relation.

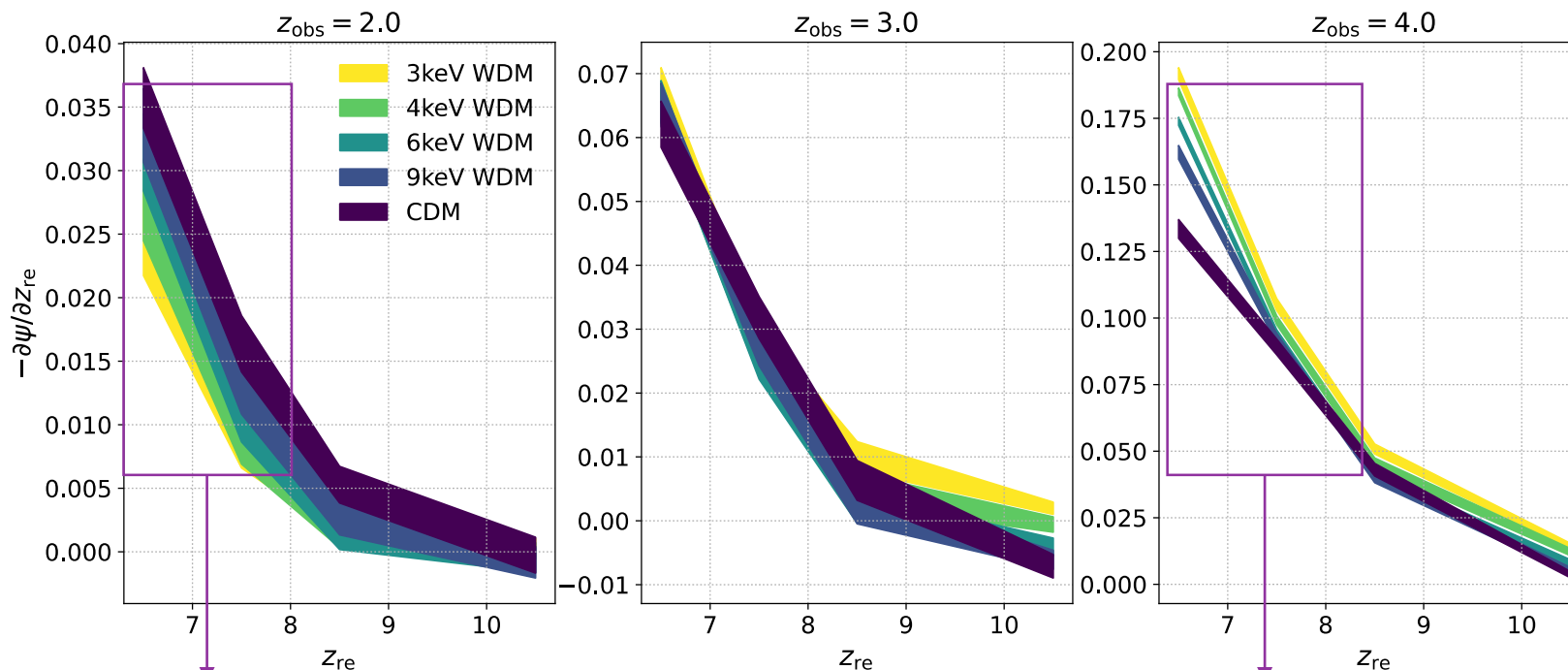


# Transparency: $\partial\psi(z_{\text{obs}}, z_{\text{re}}) / \partial z_{\text{re}}$



impact of inhomogeneous reionization: 
$$P_{m,\psi}(k, z_{\text{obs}}) = - \int_{z_{\text{min}}}^{z_{\text{max}}} \frac{\partial\psi(z_{\text{obs}}, z_{\text{re}})}{\partial z_{\text{re}}} P_{m,x_{\text{HI}}}(z_{\text{re}}, k) \frac{D(z_{\text{obs}})}{D(z_{\text{re}})} dz_{\text{re}}$$

small scale: thermal imprints



Band:  $\pm$  standard deviation of 4 realizations

Heavier DM,  
transparency varies faster.  
Effect of high-entropy mean-density gas  
is more prominent.

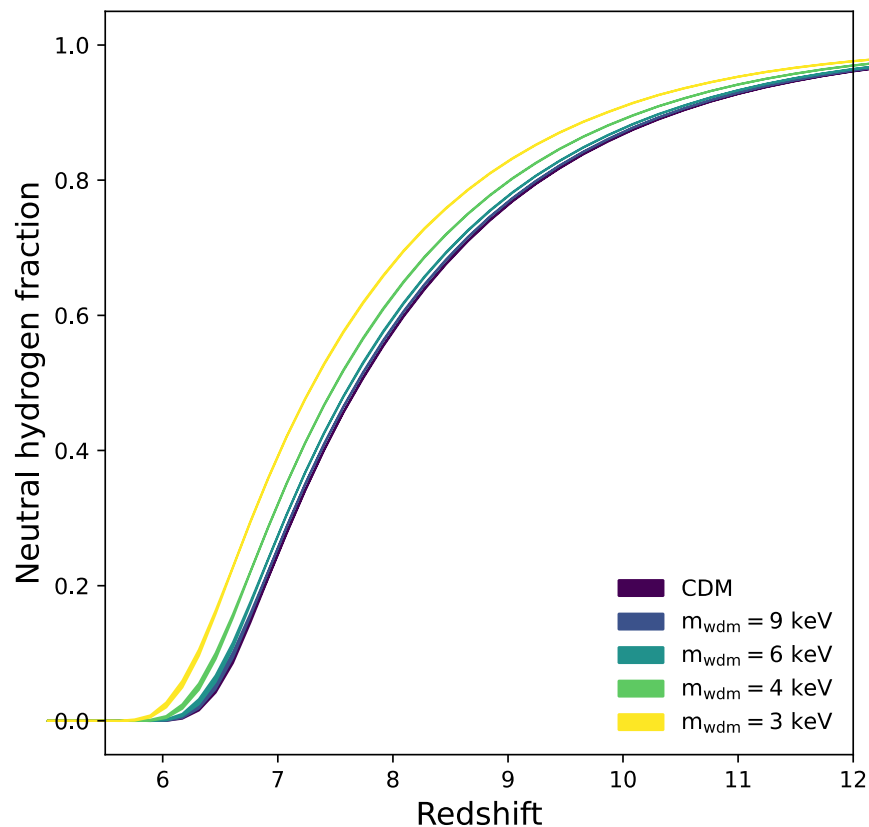
Lighter WDM,  
transparency varies faster.  
Cooling is more efficient.



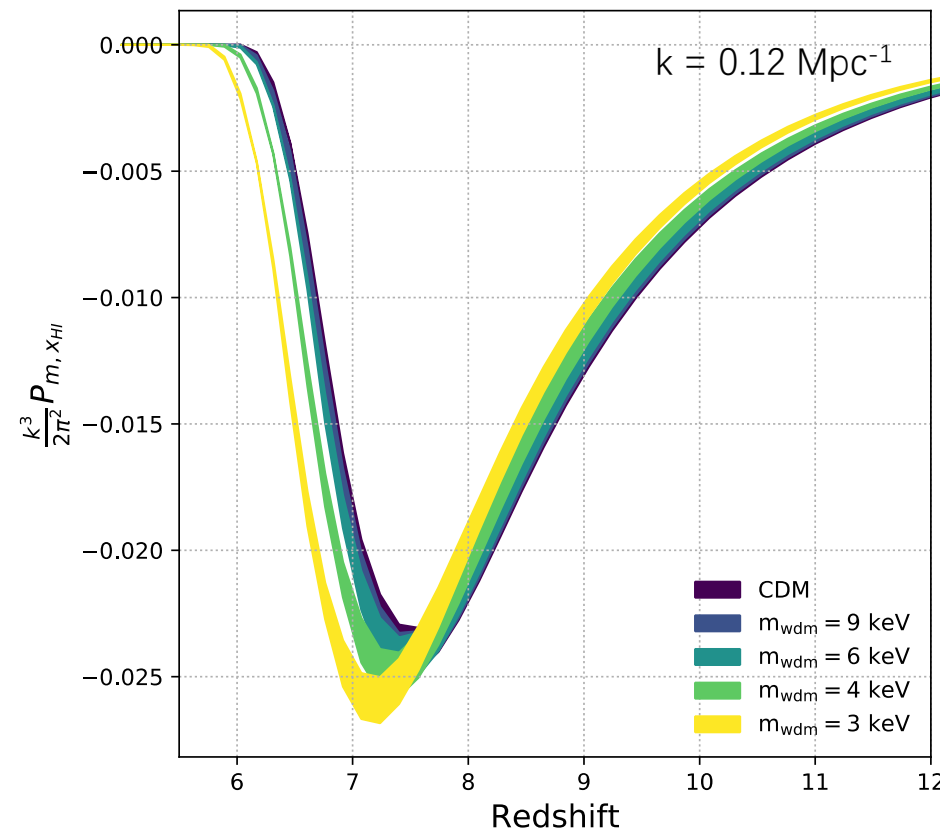
# $P_{m,x_{\text{HI}}}$ : patchy reionization



impact of inhomogeneous reionization: 
$$P_{m,\psi}(k, z_{\text{obs}}) = - \int_{z_{\text{min}}}^{z_{\text{max}}} \frac{\partial \psi(z_{\text{obs}}, z_{\text{re}})}{\partial z_{\text{re}}} P_{m,x_{\text{HI}}}(z_{\text{re}}, k) \frac{D(z_{\text{obs}})}{D(z_{\text{re}})} dz_{\text{re}}$$



Delay of reionization in WDM



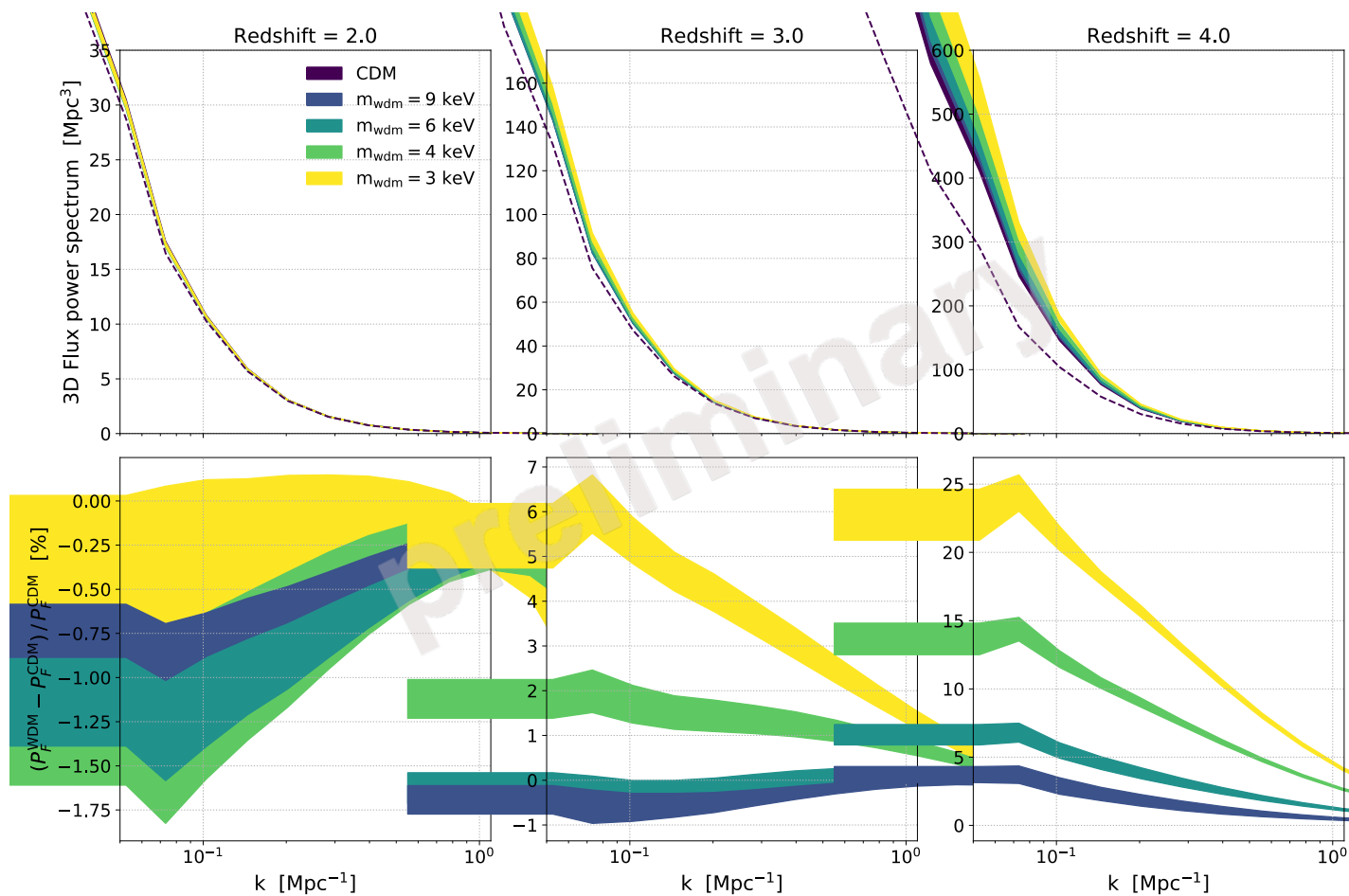
On large scales: enhancement of  $P_{m,x_{\text{HI}}}$  in WDM



# Ly $\alpha$ forest 3D power spectrum



$$P_F^{3D} = b_F^2 (1 + \beta_F \mu^2)^2 P_m + 2b_F b_\Gamma (1 + \beta_F \mu^2) P_{m,\psi}$$

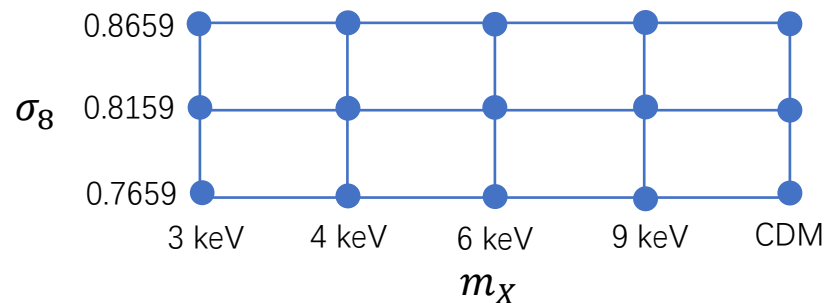


Impact of reionization:  
enhancement of power spectrum

At  $z_{\text{obs}} \geq 3.0$ , the enhancement is larger in lighter WDM.



# Forecast: constrain WDM mass by DESI Ly $\alpha$ surveys



**MCMC:** likelihood function:  $\mathcal{L} = \exp[-\frac{1}{2} \sum_{\text{bins}} (P_{\text{F}}^{3\text{D}}(z, \mathbf{k}) - P_{\text{F}}^{3\text{D,CDM}}(z, \mathbf{k}))^2 / \sigma_{\text{F}}^2(z, \mathbf{k})]$

$$\sigma_{\text{F}}^2(z, \mathbf{k}) = \frac{[P_{\text{tot}}^{3\text{D,CDM}}(z, \mathbf{k})]^2}{N_{\text{mode}}}$$

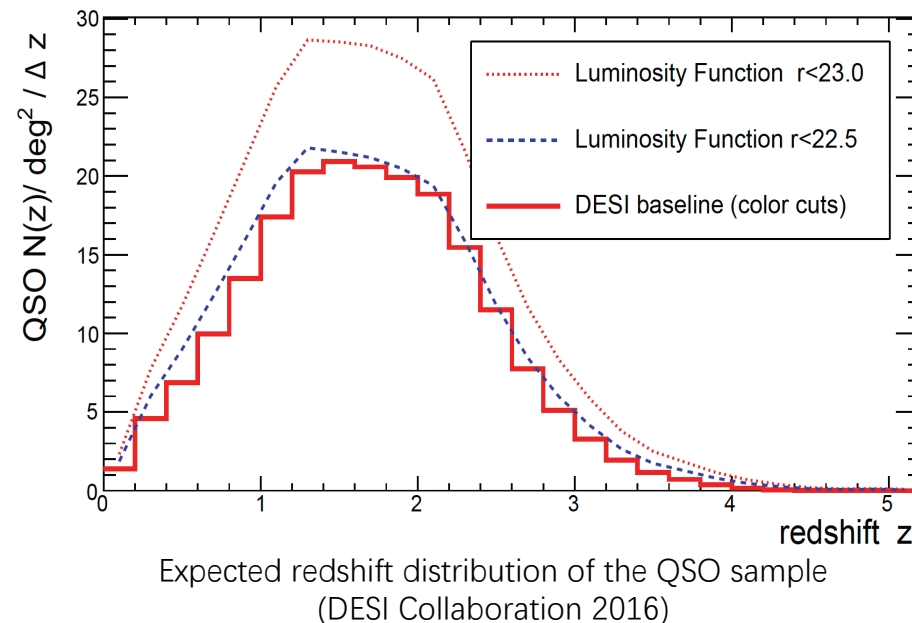
$$P_{\text{tot}}^{3\text{D,CDM}}(z, \mathbf{k}) = P_{\text{F}}^{3\text{D,CDM}}(z, \mathbf{k}) + P_{\text{F}}^{1\text{D}}(z, k_{\parallel})P_{\text{w}}^{2\text{D}}(z) + P_{\text{N}}^{\text{eff}}(z)$$

(McDonald & Eisenstein 2007) aliasing term for 2D quasar density

$P_{\text{w}}^{2\text{D}}$ : power spectrum of weighted quasar sampling function

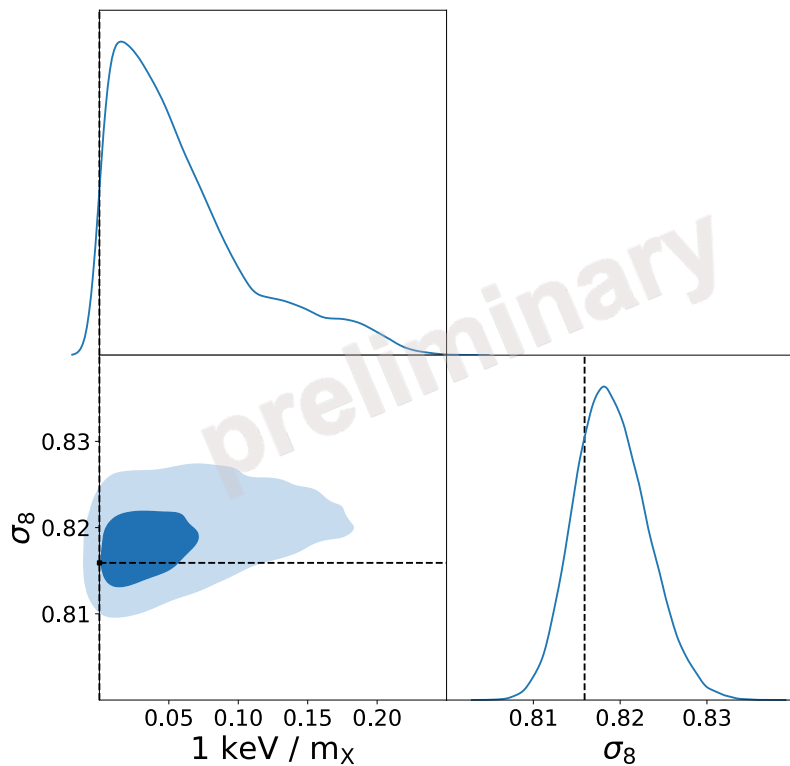
$P_{\text{N}}^{\text{eff}}$ : weighted pixel noise power

Quasar luminosity function and spectrograph performance of DESI  
(5 years, 14,000 square degrees)





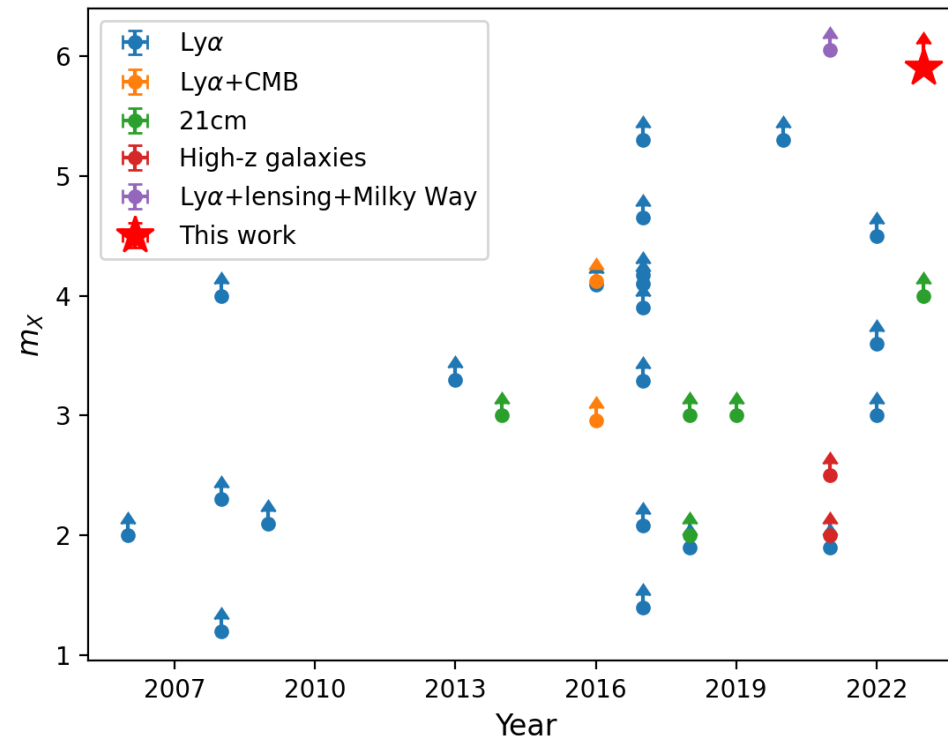
# Forecast: constrain WDM mass by DESI Ly $\alpha$ surveys



forecast:  $m_\chi > 5.9$  keV

$$\sigma_8 = 0.819^{+0.09}_{-0.07}$$

(95% Bayesian credible interval)







# Summary



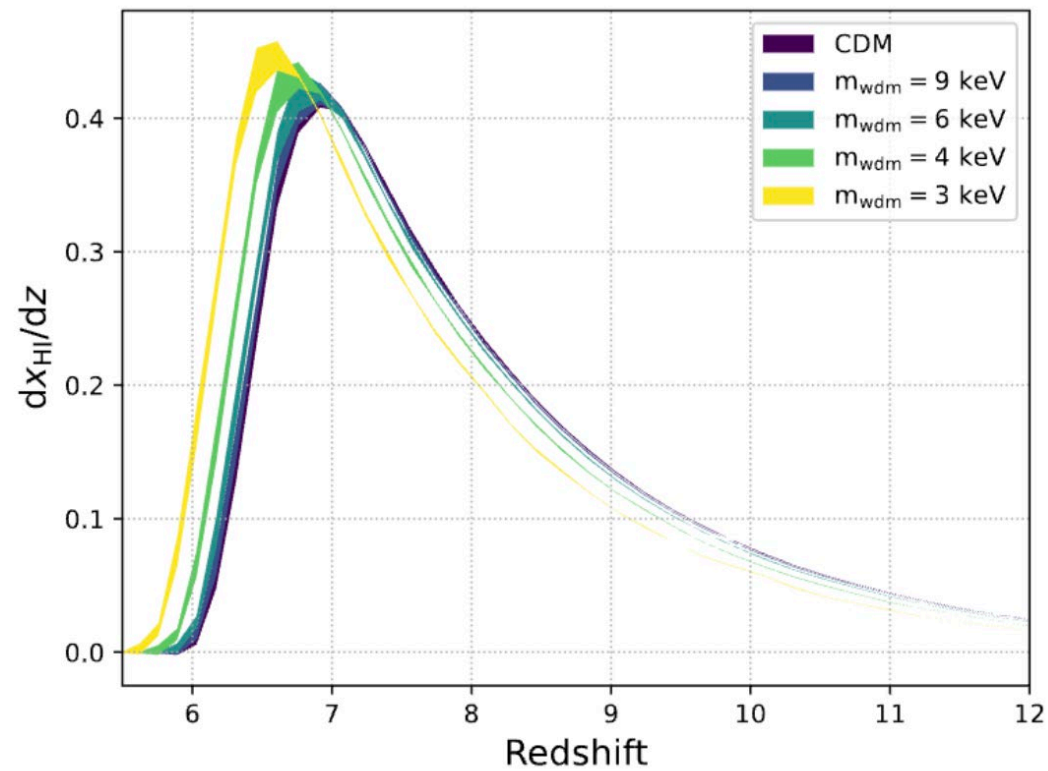
Impact of reionization:  $P_F^{3D} = b_F^2(1 + \beta_F \mu^2)^2 P_m + 2b_F b_\Gamma(1 + \beta_F \mu^2) P_{m,\psi}$

$$P_{m,\psi}(k, z_{\text{obs}}) = - \int_{z_{\text{min}}}^{z_{\text{max}}} \frac{\partial \psi(z_{\text{obs}}, z_{\text{re}})}{\partial z_{\text{re}}} P_{m,x_{\text{HI}}}(z_{\text{re}}, k) \frac{D(z_{\text{obs}})}{D(z_{\text{re}})} dz_{\text{re}}$$

small scales: thermal imprints    large scales: patchy reionization

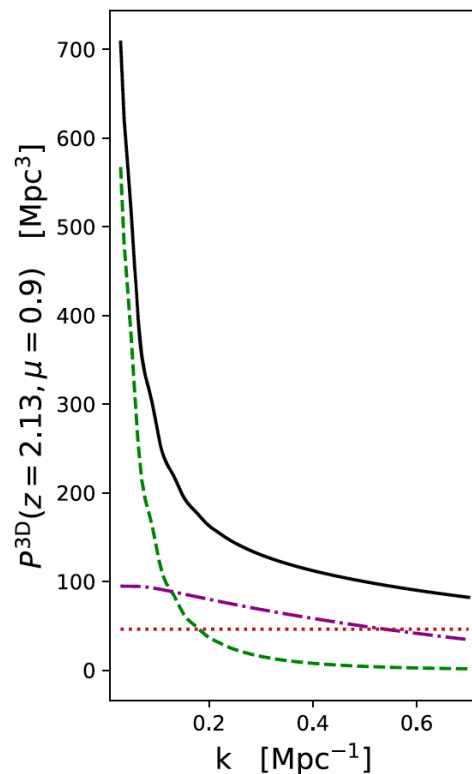
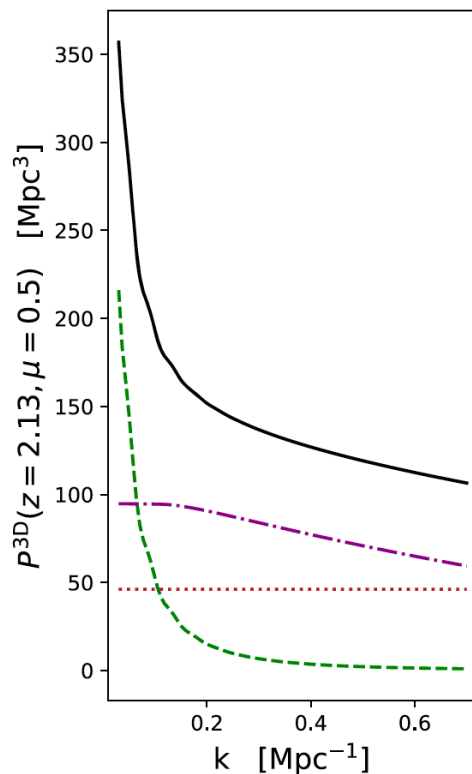
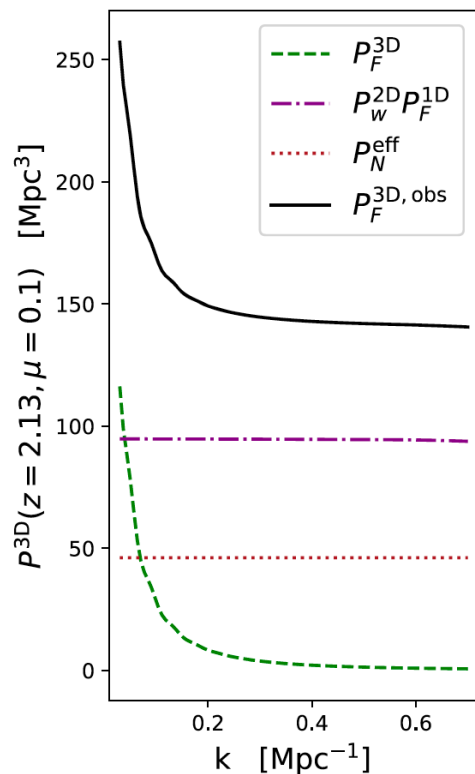
$P_F^{3D}$  can **differentiate** DM models on  $k < 1 \text{ Mpc}^{-1}$ .

Forecast DESI constraints:  $m_x > 5.9 \text{ keV}$  at 95% credible interval





# Notes



(Montero-Camacho & Mao 2020)

$$P_w^{\text{2D}} = \frac{I_2}{I_1^2 L_q},$$

$$P_N^{\text{eff}} = \frac{I_3 l_p}{I_1^2 L_q},$$

$$I_1 = \int dm \frac{dn_q}{dm} w(m),$$

$$I_2 = \int dm \frac{dn_q}{dm} w^2(m),$$

$$I_3 = \int dm \frac{dn_q}{dm} \sigma_N^2(m) w^2(m),$$

$$w(m) = \frac{P_S / P_N(m)}{1 + P_S / P_N(m)}$$



# Notes



Cosmological probe	Constraint	$m_X$ [keV]	Reference
Ly $\alpha$	Ly $\alpha$ FPS	$\gtrsim 2$	Viel et al. (2006)
	HIRES FPS	$\gtrsim 1.2$	Viel et al. (2008)
	SDSS FPS	$\gtrsim 2.3$	
	SDSS+HIRES FPS	$\gtrsim 4$	
	Ly $\alpha$ FPS	$\gtrsim 2.1$	Boyarsky et al. (2009)
	Ly $\alpha$ FPS	$\gtrsim 3.3$	Viel et al. (2013)
	SDSS-III FPS	$> 4.09$	Baur et al. (2016)
	XQ-100 FPS	$> 1.4$	Iršič et al. (2017)
	HIRES + MIKE FPS	$> 4.1$	
	XQ-100 + HIRES + MIKE FPS	$> 5.3$	
	HIRES + MIKE FPS <sup>1.1</sup>	$> 3.9$	
	XQ-100 FPS	$\gtrsim 2.08$	Yèche et al. (2017)
	SDSS-III + XQ-100 <sup>1.2</sup>	$\gtrsim 3.29$	
	SDSS-III + XQ-100	$\gtrsim 4.17$	
	SDSS-III + XQ-100 + HIRES/MIKE	$\gtrsim 4.65$	
	Ly $\alpha$ FPS <sup>1.3</sup>	$\gtrsim 1.9$	Garzilli et al. (2018)
	eBOSS ( $z < 4.5$ ) + XQ-100 FPS	$> 5.3$	Palanque-Delabrouille et al. (2020)
	HIRES FPS	$\geq 1.9$	Garzilli et al. (2021)
Keck + VLT FPS	$> 3.0$	Villasenor et al. (2022)	
Keck + VLT FPS best fit <sup>1.4</sup>	$> 3.6$		
Keck + VLT FPS + Increased Quasar Sightlines <sup>1.5</sup>	$> 4.5$		
Ly $\alpha$ + CMB	SDSS-III flux + Planck 2016 + SDSS-III BAO	$> 2.96$	Baur et al. (2016)
	SDSS-III flux + Planck 2016 + SDSS-III BAO + $\alpha_s$	$> 4.12$	
21cm	Atomic cooling haloes + $f_s$	$\geq 3$	Sitwell et al. (2014)
	Atomic cooling halos	$> 3$	Safarzadeh et al. (2018)
	H II cooling halos	$> 2$	
	EDGES + X-ray heating+ with and without excess radio background	$\gtrsim 3$	Chatterjee et al. (2019)
	EDGES + $f_s = 0.09$	$= 6$	Boyarsky et al. (2019)
	SKA1-LOW	$\gtrsim 4$	Mosbech et al. (2023)
High- $z$ galaxies	UV luminosity function	$\gtrsim 2$	Rudakovskiy et al. (2021)
	JWST Mock data	$\gtrsim 2.5$	
Ly $\alpha$ + lensing + Milky Way	HIRES + MIKE flux, SLACS and DES + SDSS	$\geq 6.048$	Enzi et al. (2021)



$$\begin{aligned}
 & (2\pi)^3 \delta^{(3)}(\mathbf{k} - \mathbf{k}') P_{m,\psi}(z_{\text{obs}}, k) \\
 &= \int_{\mathbb{R}^3} d^3 \mathbf{r}' e^{-i\mathbf{k}' \cdot \mathbf{r}'} \langle \tilde{\delta}_m^*(z_{\text{obs}}, \mathbf{k}) \psi(z_{\text{re}}(\mathbf{r}'), z_{\text{obs}}) \rangle \\
 &= - \int_{\mathbb{R}^3} d^3 \mathbf{r}' e^{-i\mathbf{k}' \cdot \mathbf{r}'} \int_{z_{\text{max}}}^{z_{\text{min}}} \left\langle \tilde{\delta}_m^*(z_{\text{obs}}, \mathbf{k}) \frac{\partial \psi(z', z_{\text{obs}})}{\partial z'} \right. \\
 &\quad \left. \times \Theta(z' - z_{\text{re}}(\mathbf{r}')) \right\rangle dz' \\
 &= - \int_{z_{\text{min}}}^{z_{\text{max}}} dz' \frac{\partial \psi}{\partial z'}(z', z_{\text{obs}}) \langle \tilde{\delta}_m^*(z', \mathbf{k}) \tilde{x}_{\text{HI}}(z', \mathbf{k}') \rangle \frac{D(z_{\text{obs}})}{D(z')}.
 \end{aligned}$$

(Montero-Camacho et al. 2019)