

DarkAI: Reconstructing the large-scale density field of dark matter using AI



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Reconstructing the mass distribution of the Universe

Well-understood



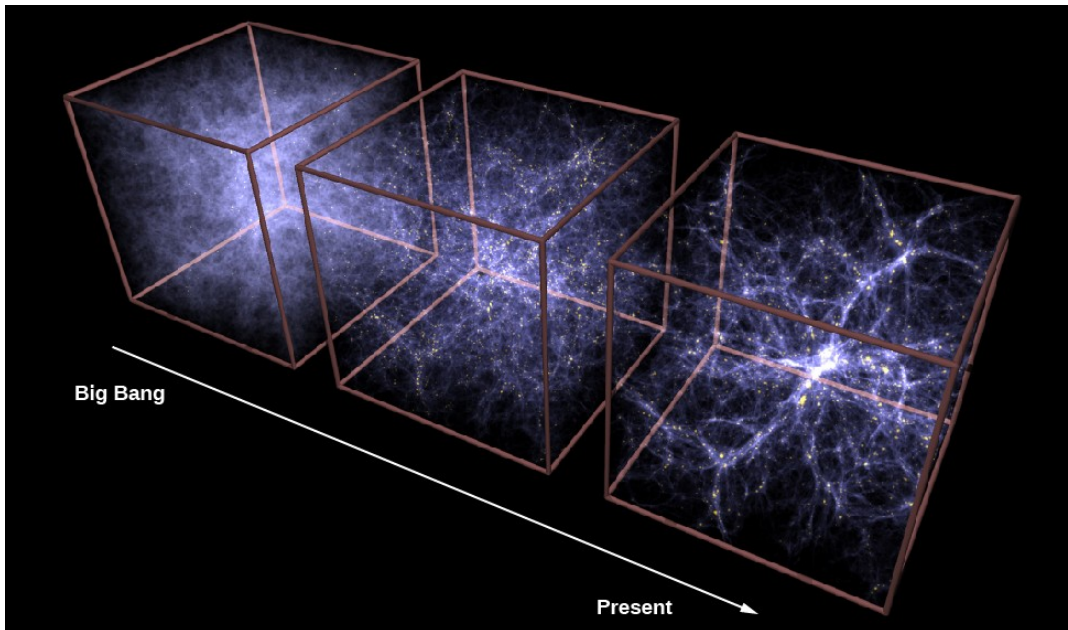
Initial conditions

Dark matter distribution

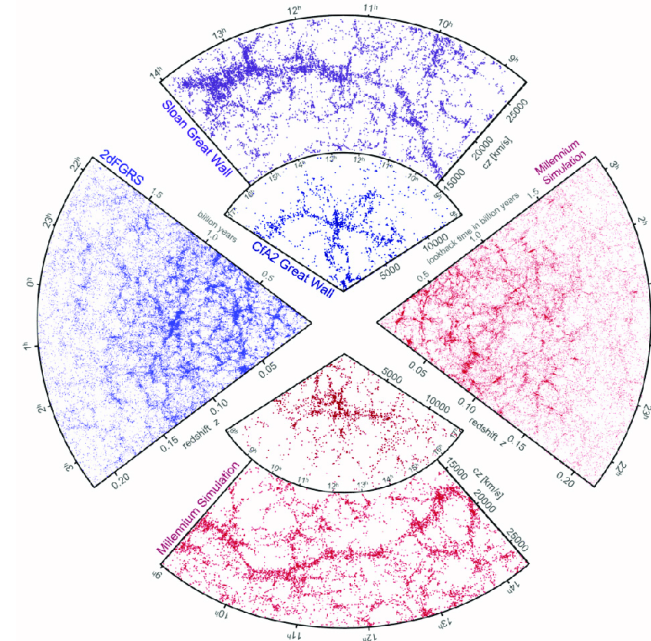
Dark matter halo

Galaxy distribution

Nbody simulations



Mock galaxy survey





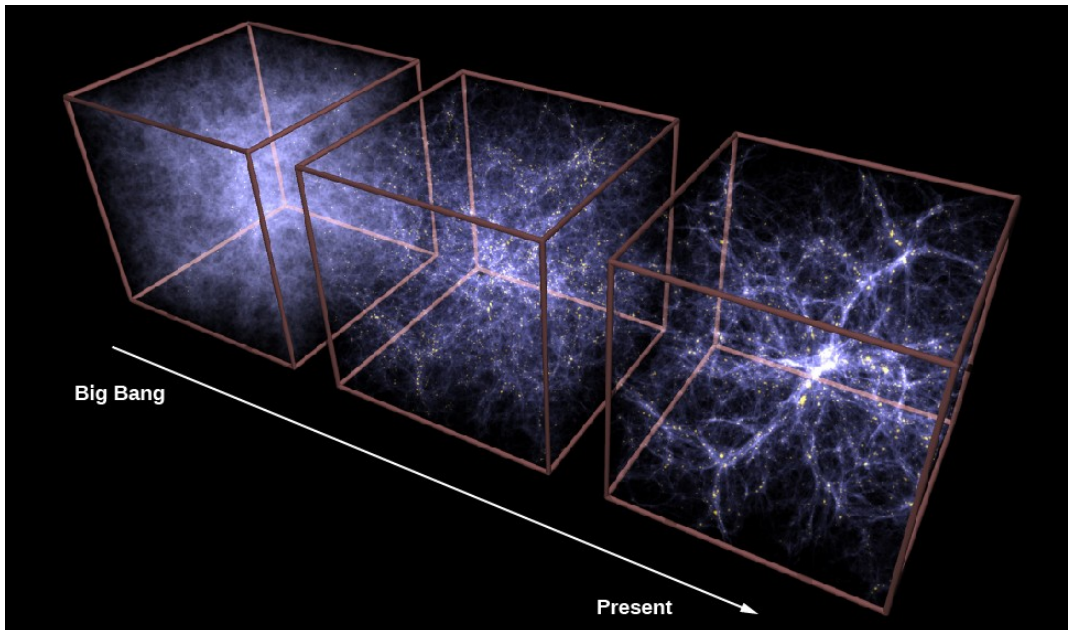
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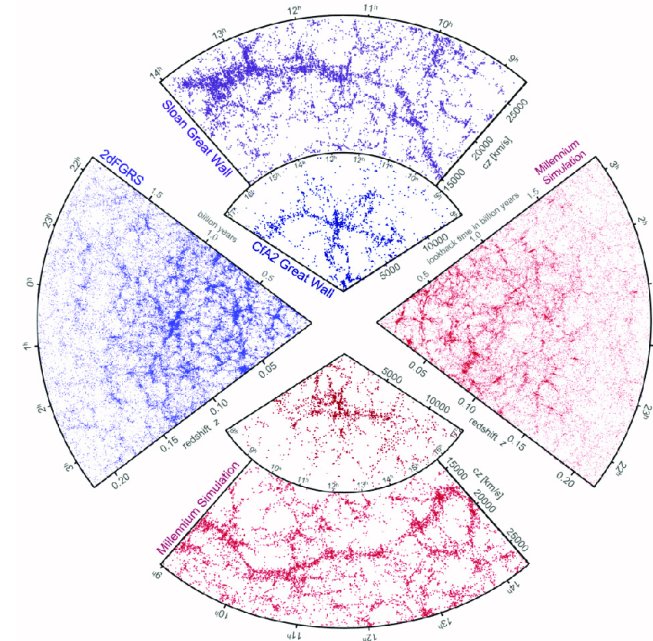


Opportunity to reconstruct the underlying cosmic density field

Nbody simulations



Mock galaxy survey

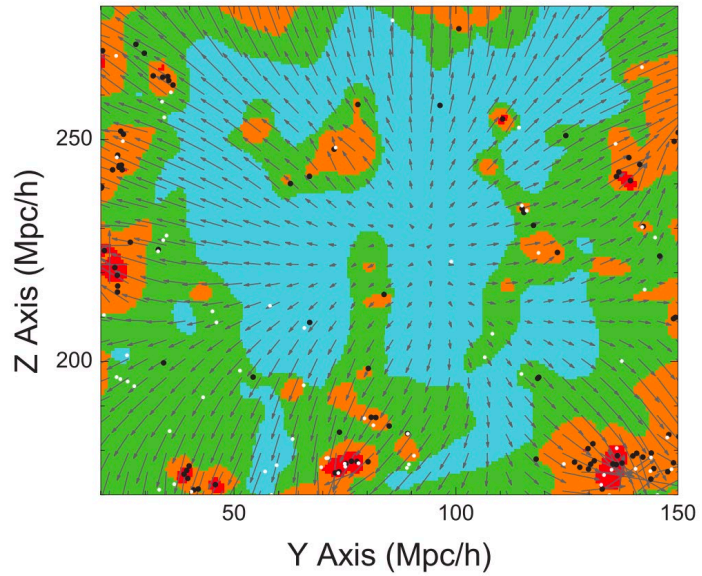




Reconstructing the mass distribution of the Universe can provide

US

- Velocity & Tidal field (Wang et al. 2012)

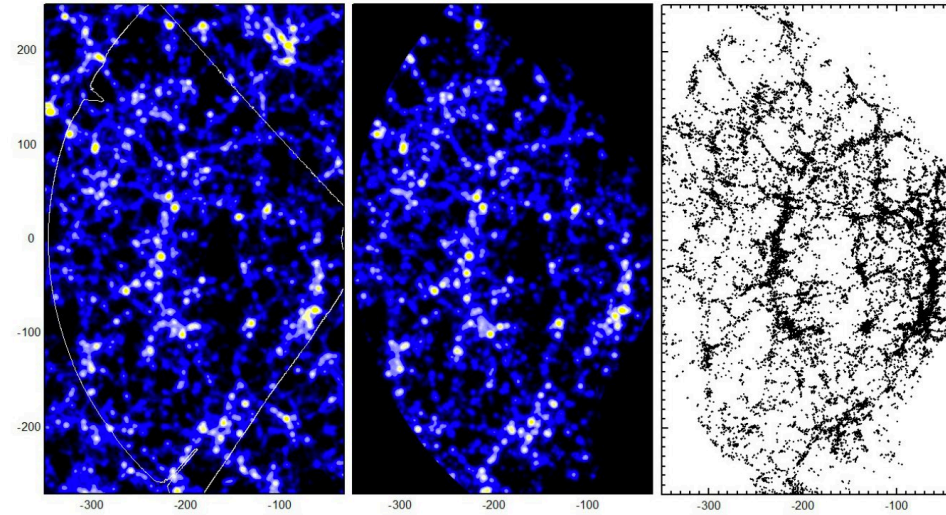
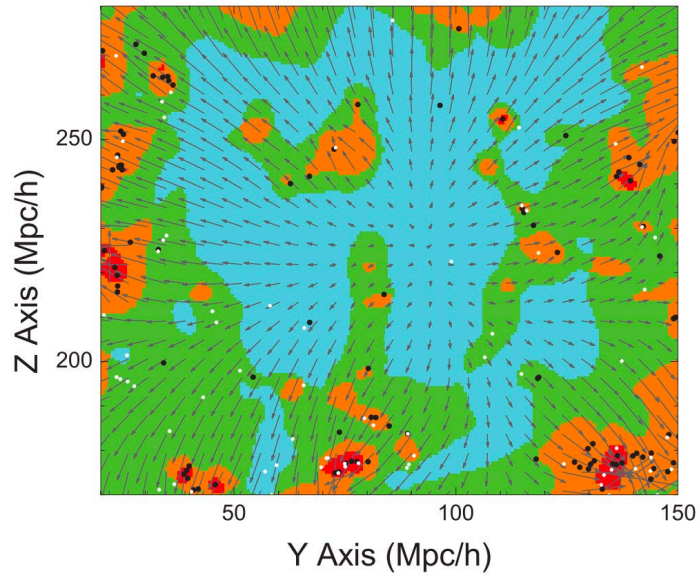




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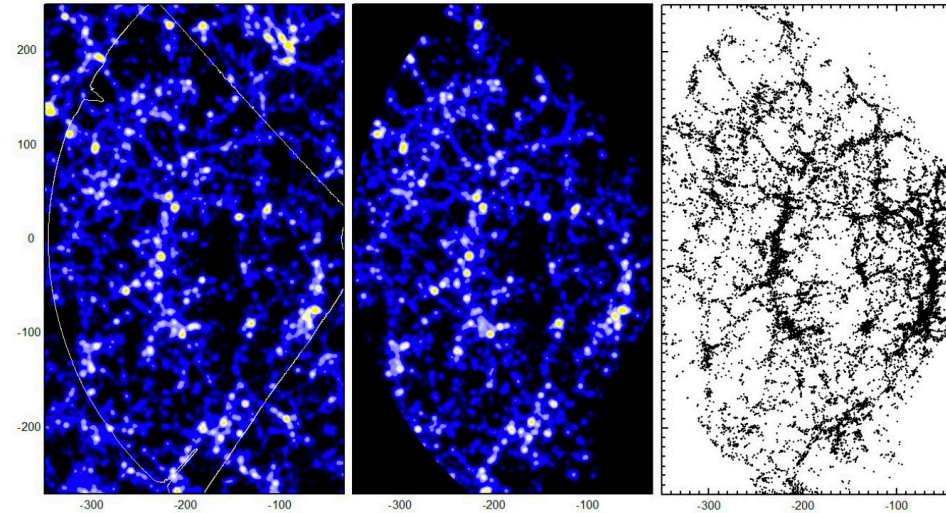
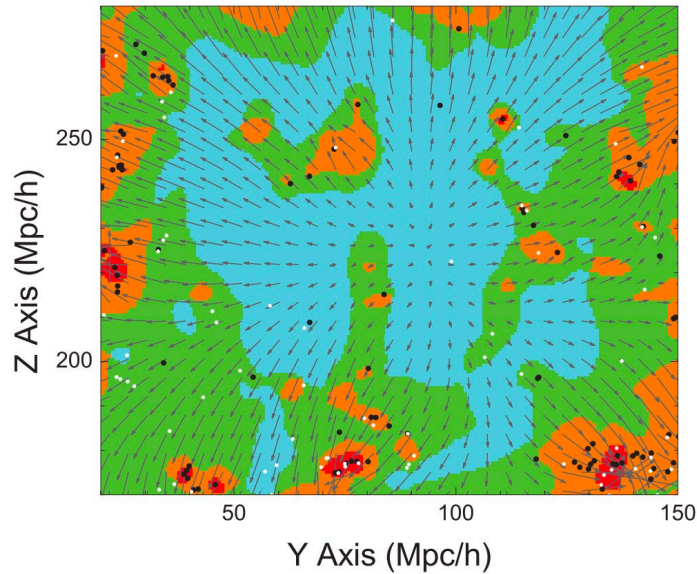




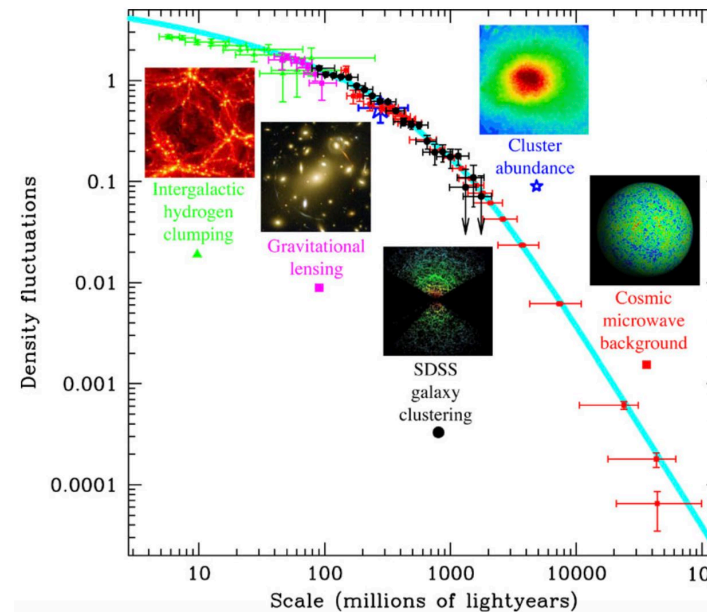
Reconstructing the mass distribution of the Universe can provide

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- Real-space dark matter power spectrum (Tegmark et al. 2004)

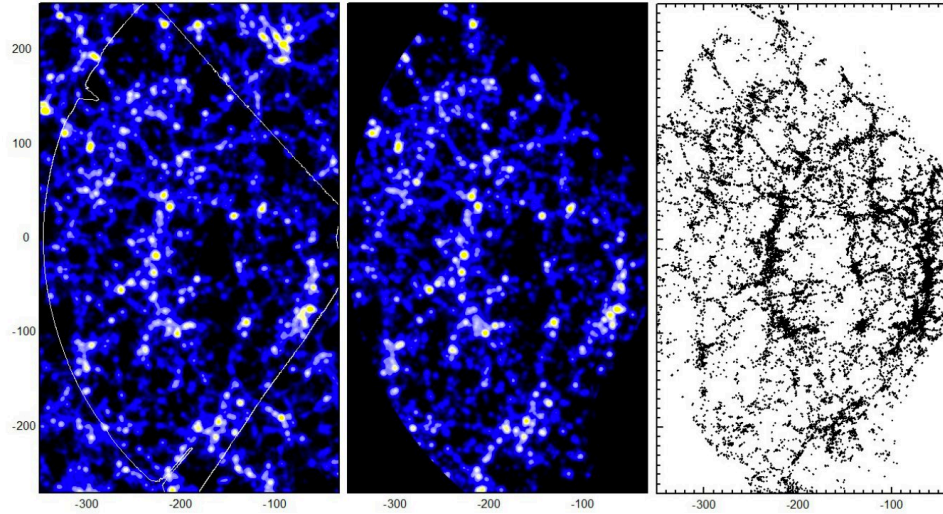
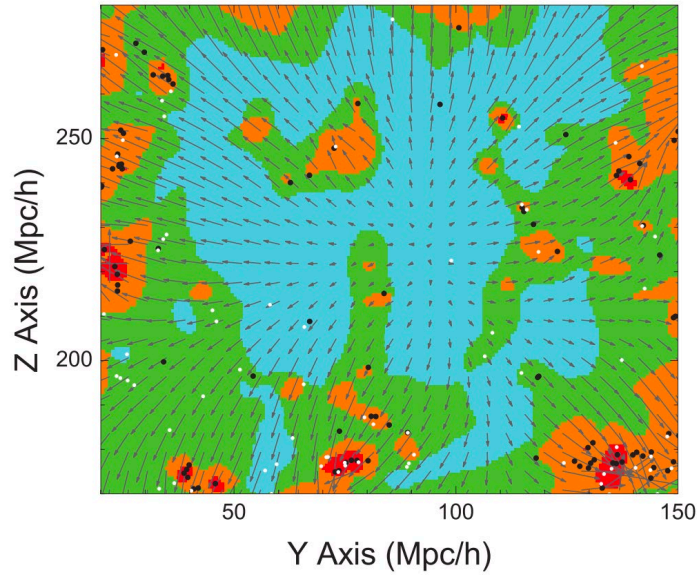




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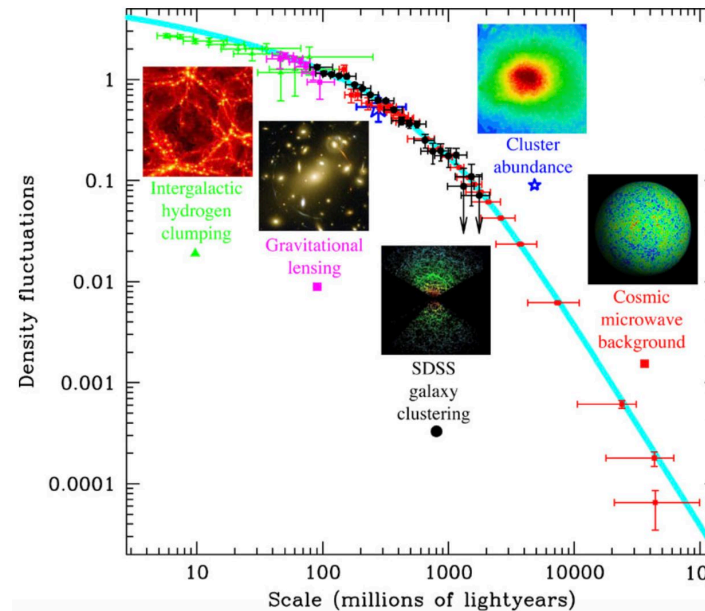
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Galaxy formation

- Real-space dark matter power spectrum (Tegmark et al. 2004)



Cosmology



The challenge in reconstructing the density field

1) Galaxies bias:

- Biased tracers of the underlying mass distribution
- Exact form of the bias is complicated.
- Linear bias form used to reconstructing velocity field
- Linear bias: only valid for small density fluctuations
motivated more by simplicity than by physical principles

$$\mathbf{v}(\mathbf{k}) = H a f(\Omega) \frac{i\mathbf{k}}{k^2} \frac{\delta_h(\mathbf{k})}{b_{hm}}.$$

$$\delta_h(\mathbf{x}) = b_1 \delta(\mathbf{x}) + \frac{1}{2} b_2 [\delta(\mathbf{x})^2 - \sigma_2] + \frac{1}{2} b_{s2} [s(\mathbf{x})^2 - \langle s^2 \rangle] \\ + \text{higher order terms}.$$



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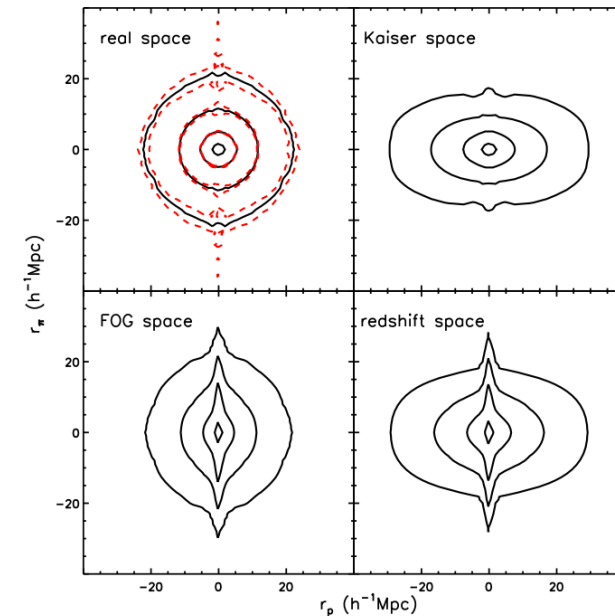
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2) Redshift space distortions

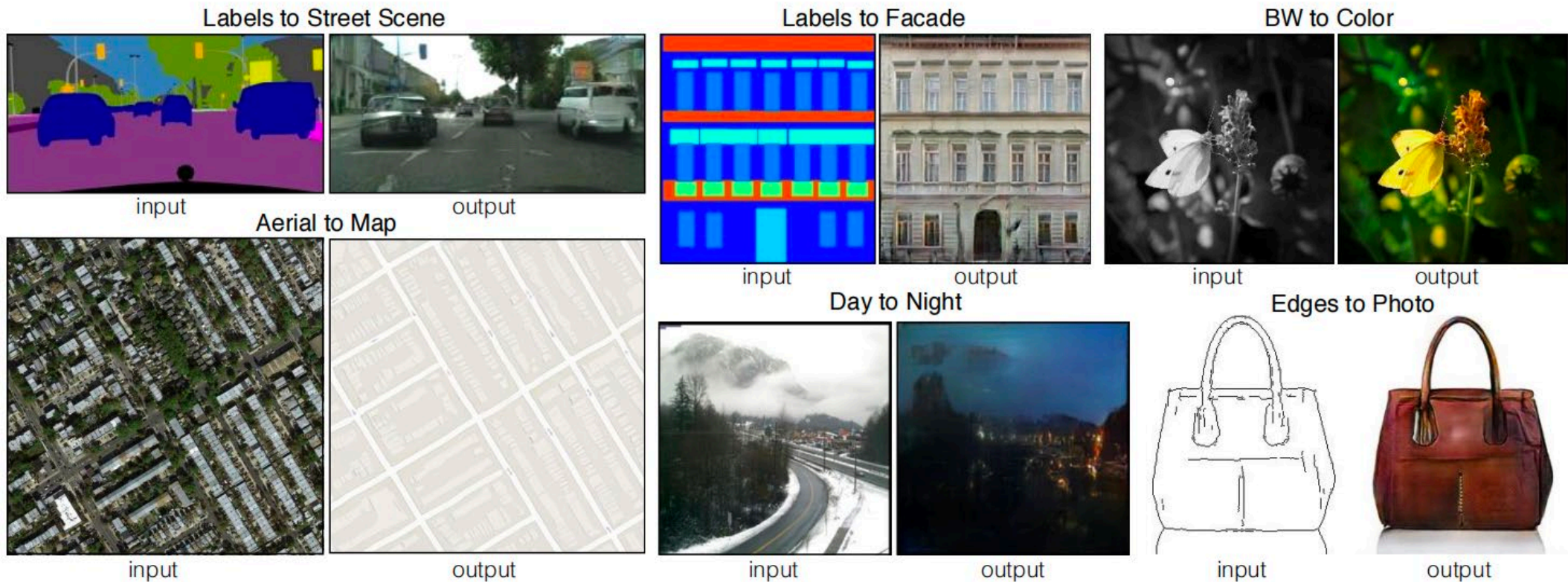
- Kaiser effect and FOG effect
- Causing modeling the bias parameters more complicated
- Iteration to make the RSD correction
- Linear theory limited in the high-density regions





Deeping learning method: UNet model

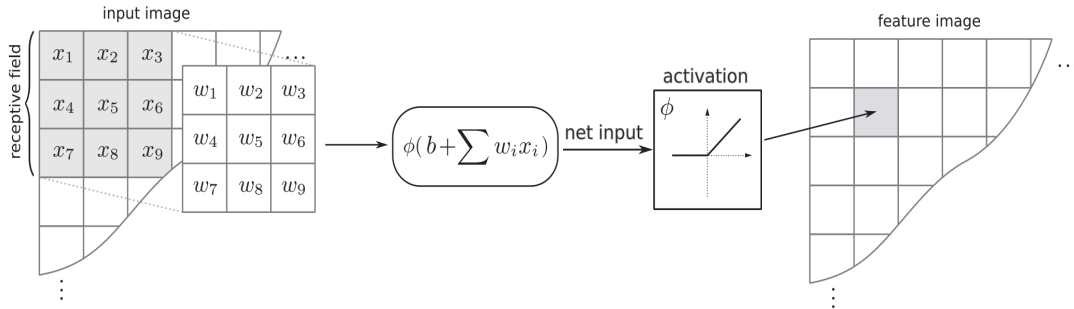
- Provides a general model for image-to-image translation
- Apply to a wide variety of image generation tasks, including translating photography from day to night and product sketches to photographs



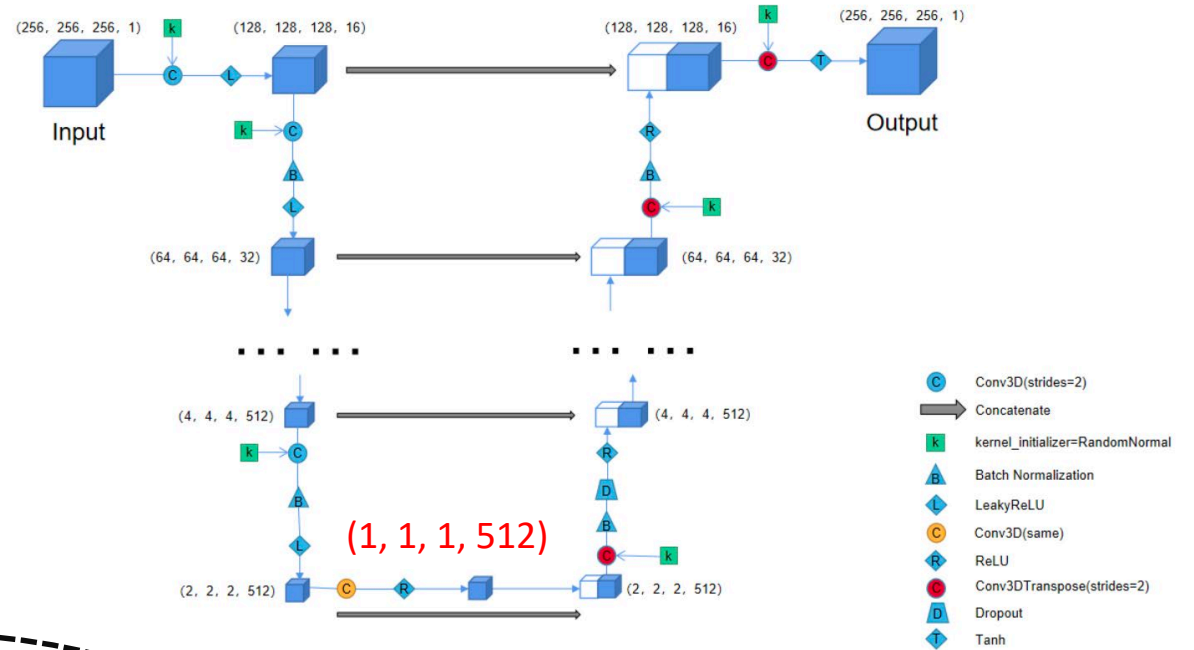


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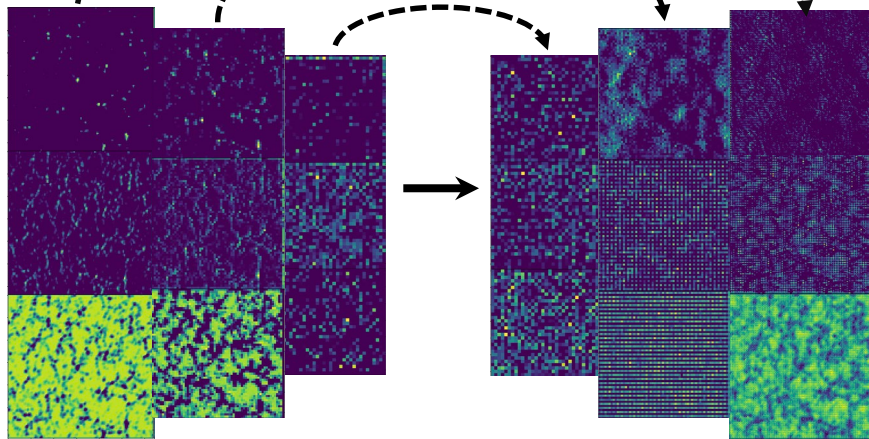
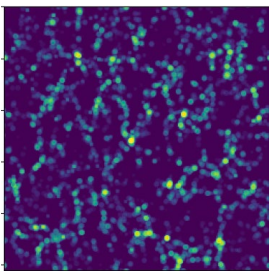
Convolutional neural network (CNN) :



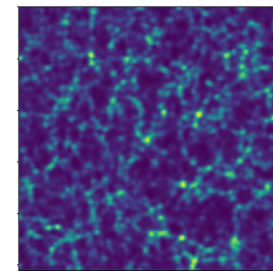
Encoder-decoder with skip connections:



Halo field



Dark matter field





Generating training and testing data

1) Evolve the particles:

- `cola_halo` code: COmoving Lagrangian Acceleration (COLA) fast simulation
- Generate 30 simulations: **15 training, 5 validation, and 10 testing samples**
- Planck2018 cosmology, $\Omega_m = 0.3111$, $\Omega_\Lambda = 0.6889$, $h = 0.6766$, $\sigma_8 = 0.812$.
- 512^3 particles, $500\text{Mpc}/h$
- Add RSD along the z-axis for halos. Keep real space for dark matter.



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2) Construct the density fields:

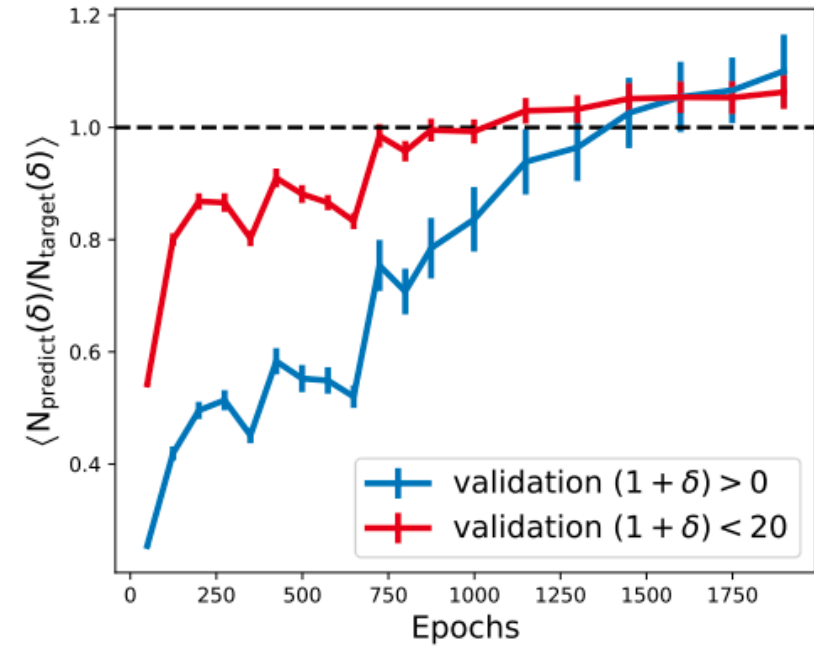
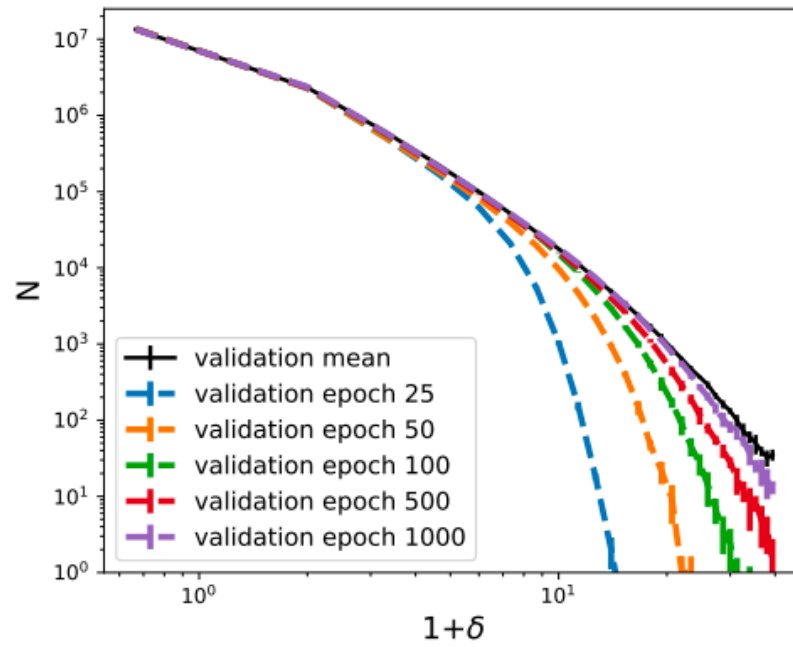
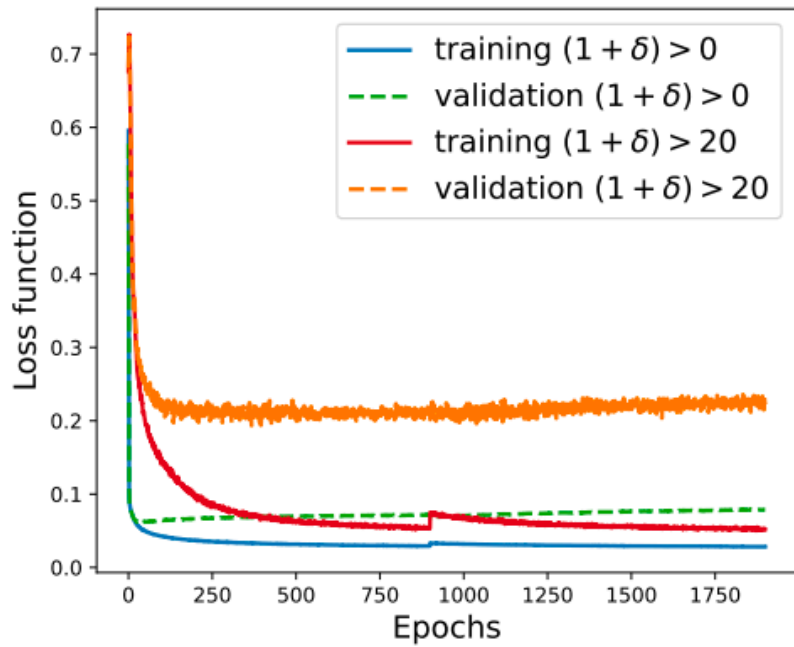
- CIC scheme, 256^3 voxels, Top-hat smoothing with $R_s = 5 h^{-1}\text{Mpc}$
- Halo mass weighting
- Rescaled the overdensity values to lie in the interval $[-1, 1]$

$$s(x) = 2x/(x + a) - 1, \quad a=5$$



Training process

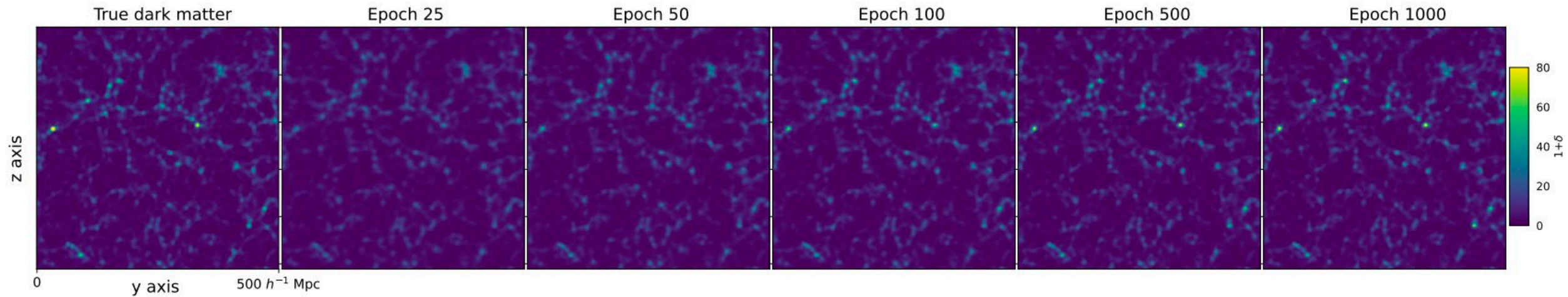
- Run 1000 epochs: check both training and validating samples
- The differences between the prediction and the target keep less until epoch around epoch 600
- The performance would not be improved after epoch 600
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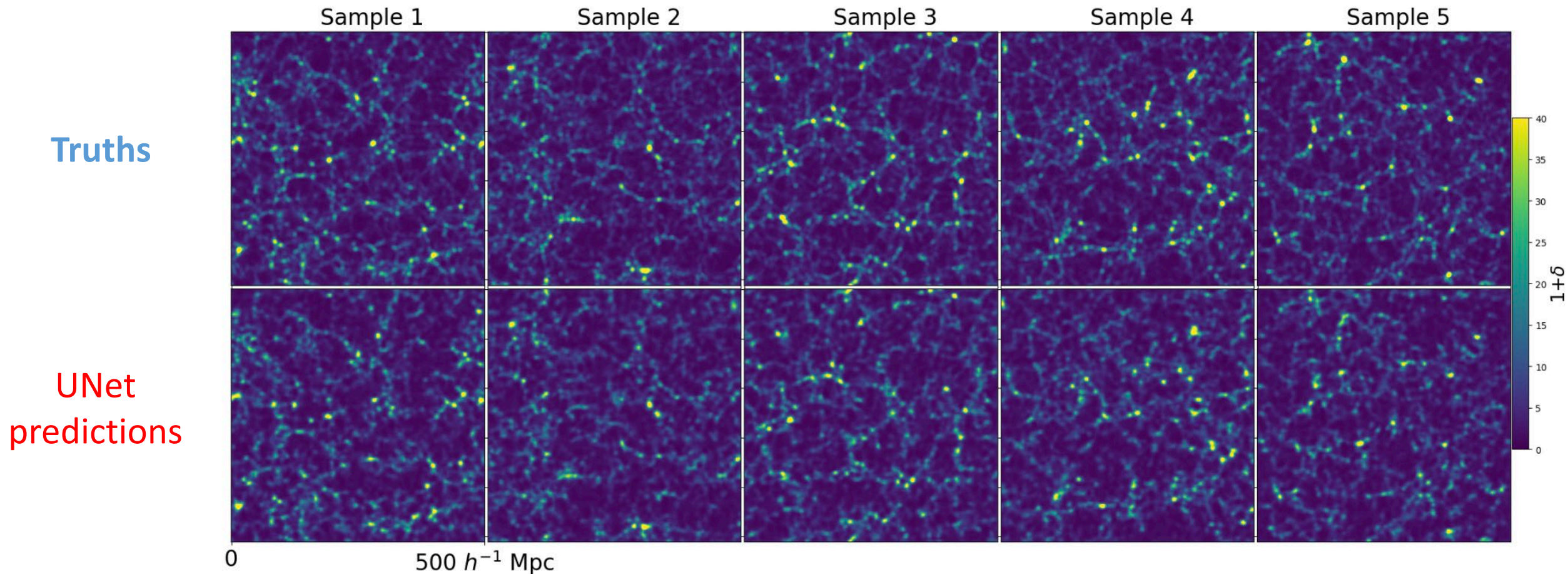




Testing: COLA samples

1) Comparisons of the projected density

- 5 samples randomly selected from the 10 COLA test samples in a slice of $500 \times 500 \times 9.76 h^{-1} \text{Mpc}$
- The reconstruction exhibit recognizable, large-scale structures including clusters, filaments, and voids
- The reconstruction is generally very successful over the different scales
- Differ slightly from the target at regions around clusters.

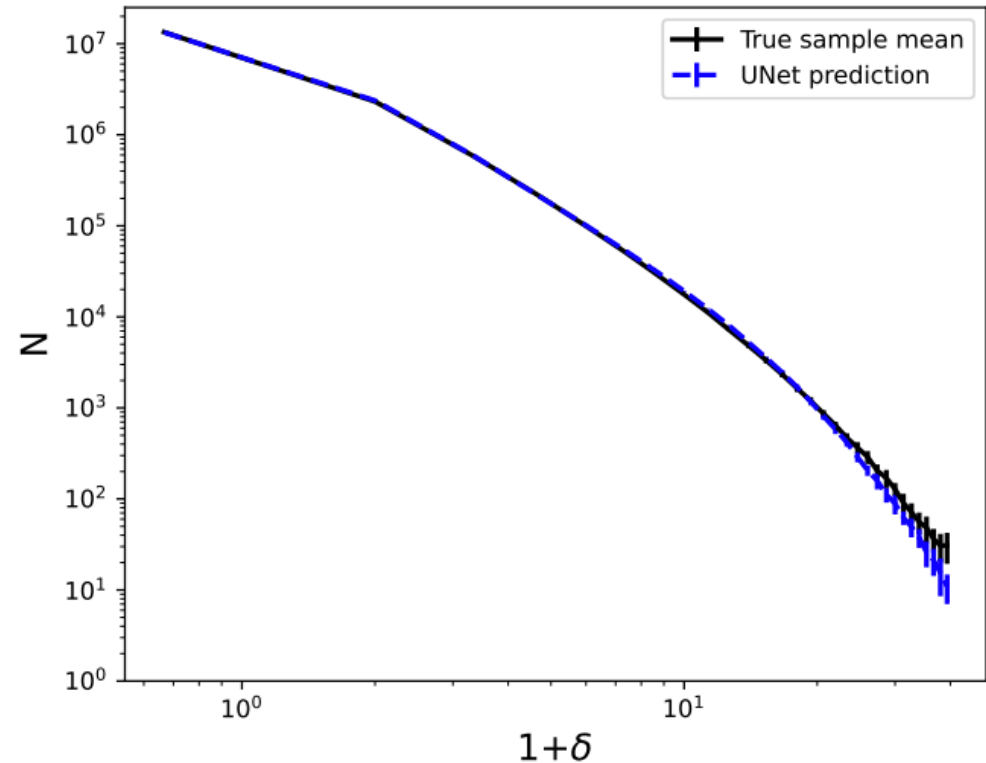
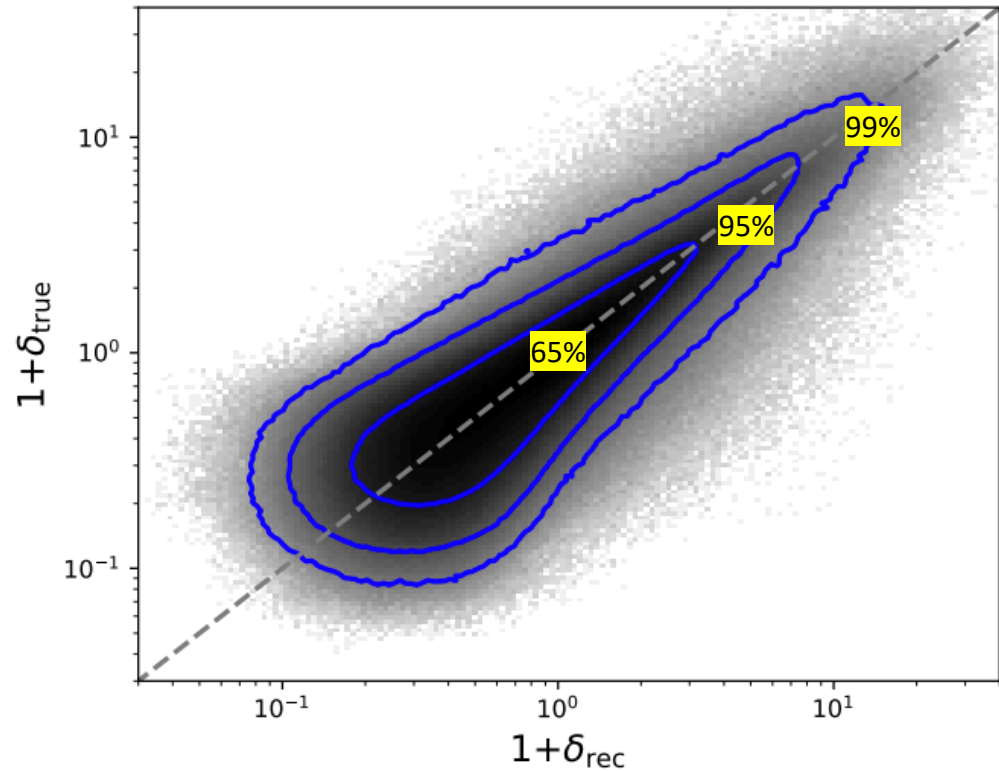




Testing: COLA samples

2) Density-density relation (left panel) and histogram distribution (right panel)

- No significant bias between δ_{rec} and δ_{true}
- 99.98% grids keeps accuracy $\Delta\delta/\delta < 5\%$
- Reason: small number of massive halos in current training volume

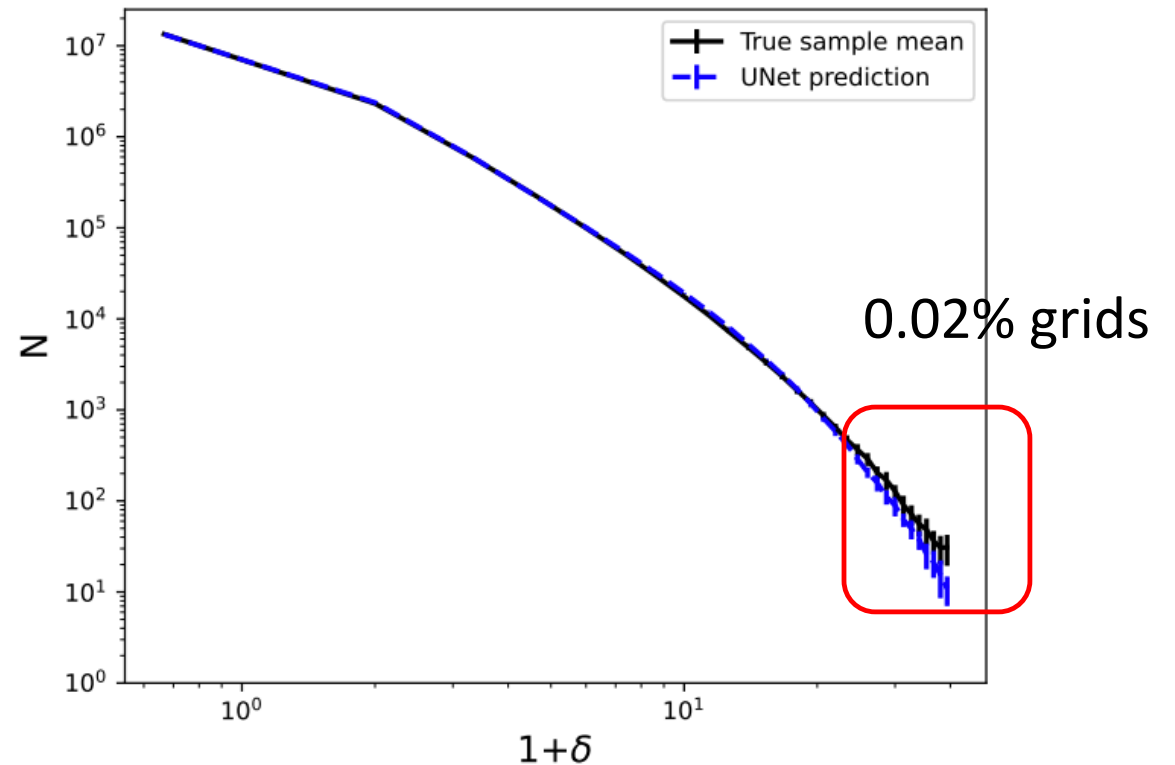
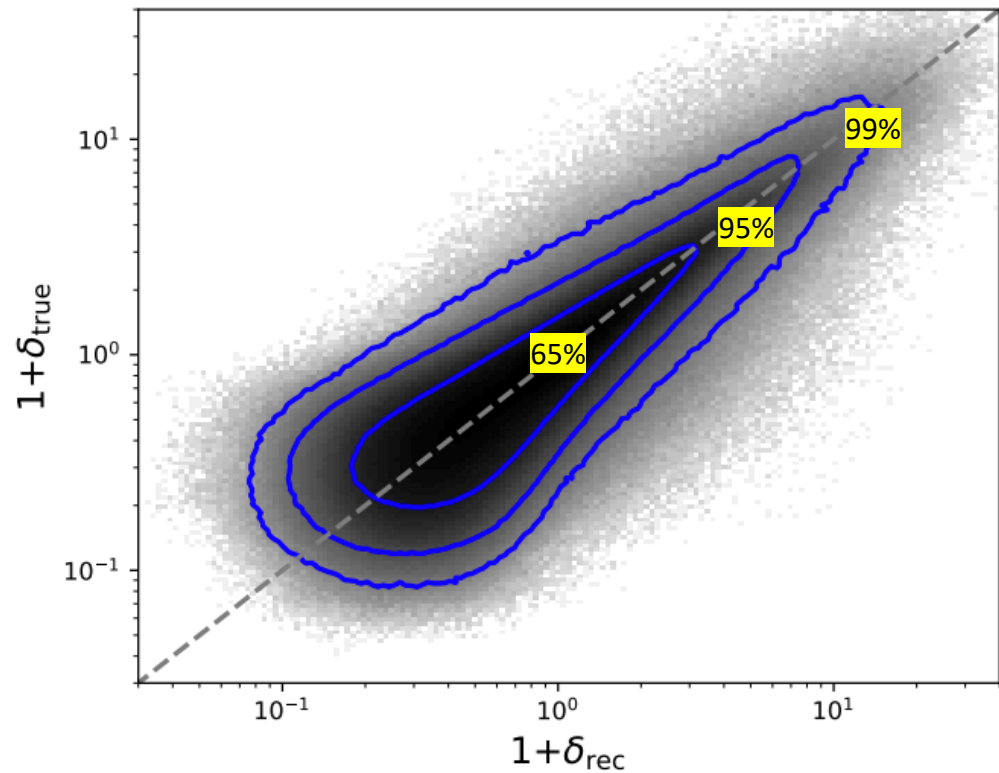




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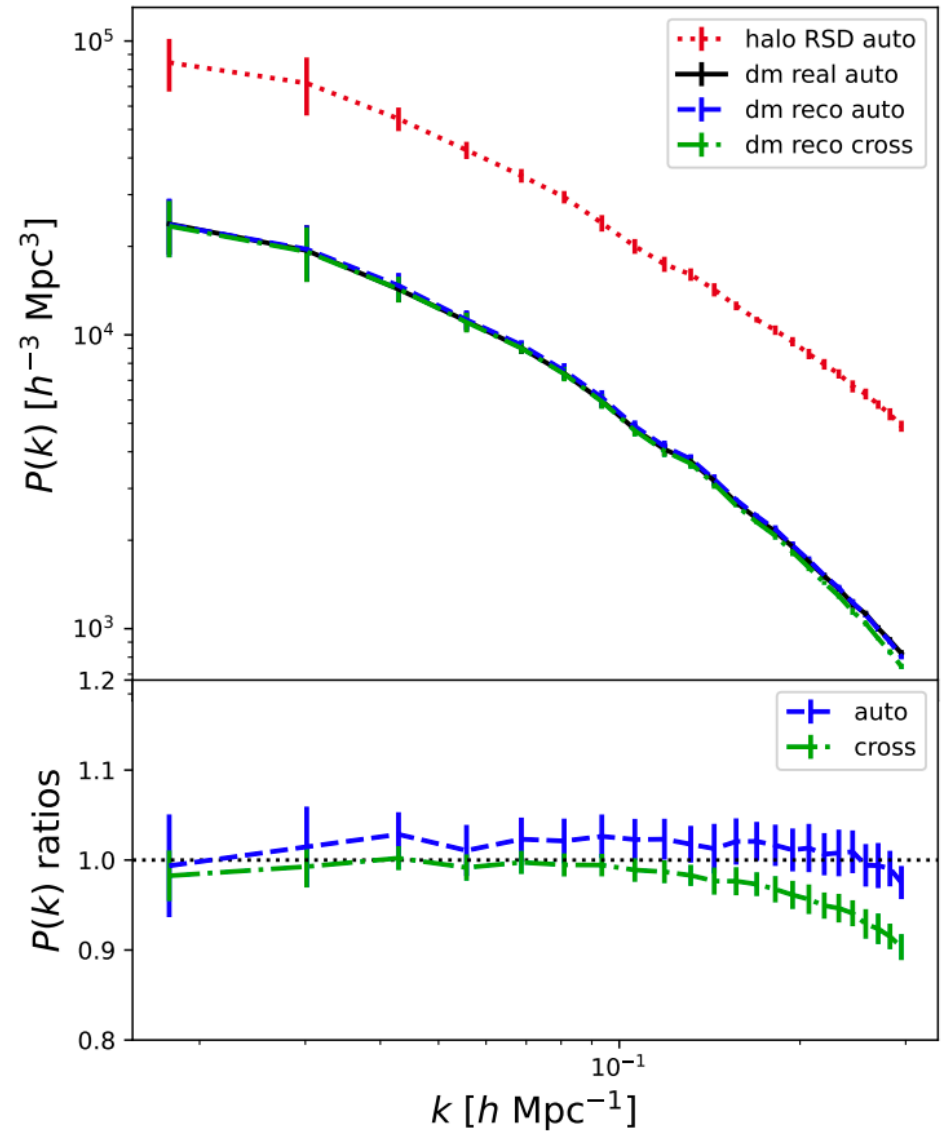
3) Monopole power spectrum

- Cross-correlation:

$P(k)$ ratios is 0.99 ± 0.01 , $k < 0.1 h \text{ Mpc}^{-1}$

1% reduction at $k = 0.1 h \text{ Mpc}^{-1}$

10% reduction at $k = 0.3 h \text{ Mpc}^{-1}$

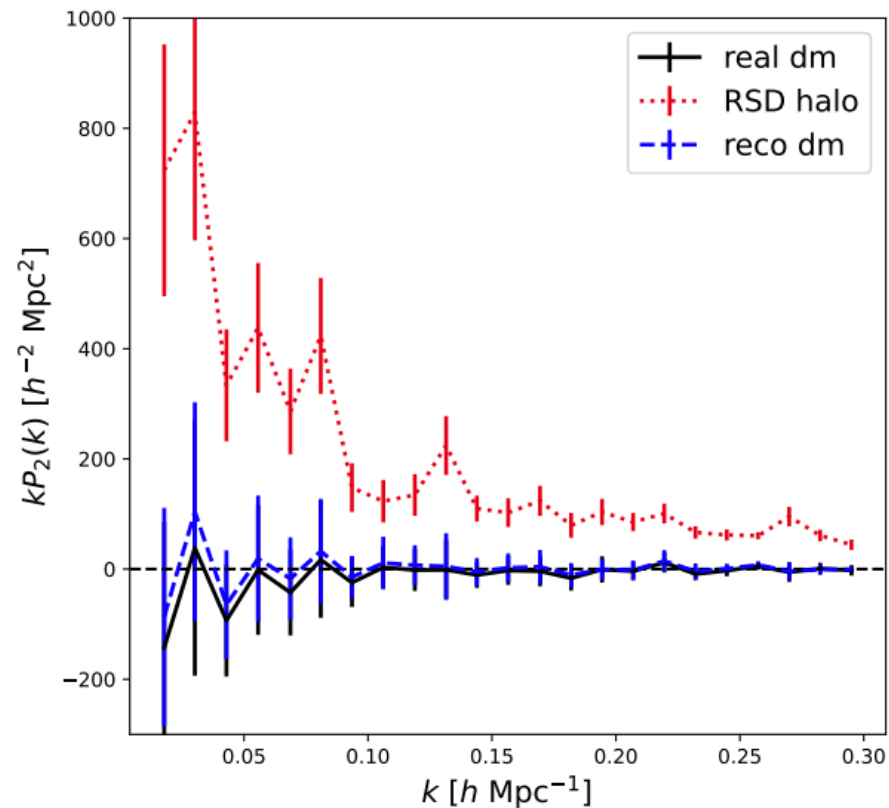
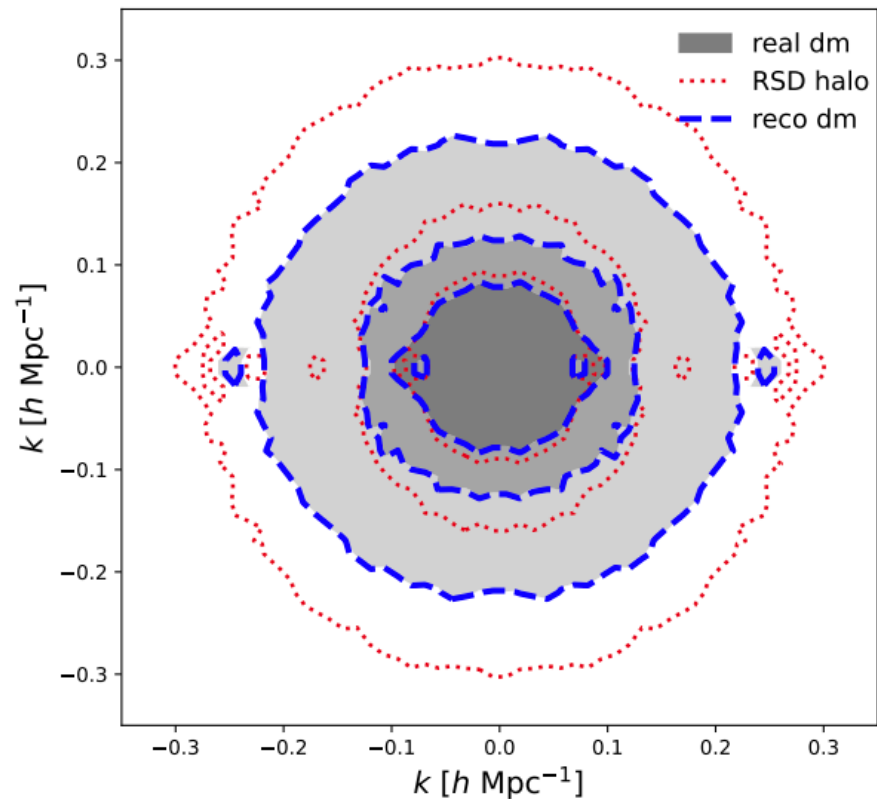




Testing: COLA samples

4) 2D power spectrum

- UNet-reconstructed $P(k_{\perp}, k_{\parallel})$ is clearly more isotropic and perfectly round.
- Quadrupole $P_2(k)$ is very close to zero.
- The correction for the RSDs is overall very successful.



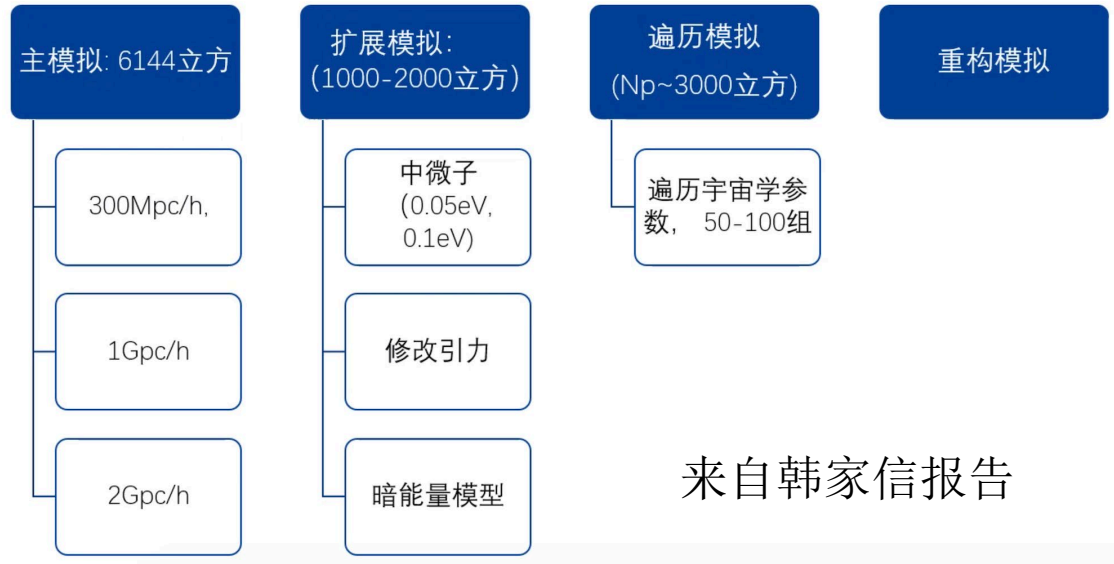
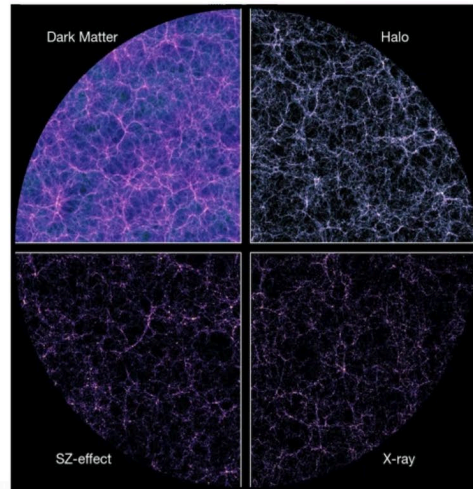


Application to Jiutian

Simulation for CSST

- 标准宇宙学模型 (Planck2018)
- 分层互补, 匹配分辨率和尺度需求
- 6144^3 粒子, 纯暗物质
- 已完成1Gpc/h
 - L-GADGET3 (李明)
 - 1万核, 28天 (14天模拟+14天后处理)
~700万核时, 22TB+内存
 - 6.8TB/snapshot, 共900TB+
(Millennium: 2160^3 , 500Mpc/h, $m_p=8 \times 10^8$, 34万核时, 25TB数据)
 - 完成初步测试和半解析星系建模

边长(Mpc/h)	粒子质量(M_{\odot}/h)
300	10^7
1000	3.6×10^8
2000	2.8×10^9



来自韩家信报告



Application to Jiutian

主模拟：九天

盒子大小：1000Mpc/h

粒子数：6144³

计算：1万核，28天

内存：22TB+

存储：900TB+



Application to Jiutian

训练数据: COLA

盒子大小: 500Mpc/h

粒子数: 512^3

计算: 28核, 0.5小时

内存: <3GB

存储: 10GB

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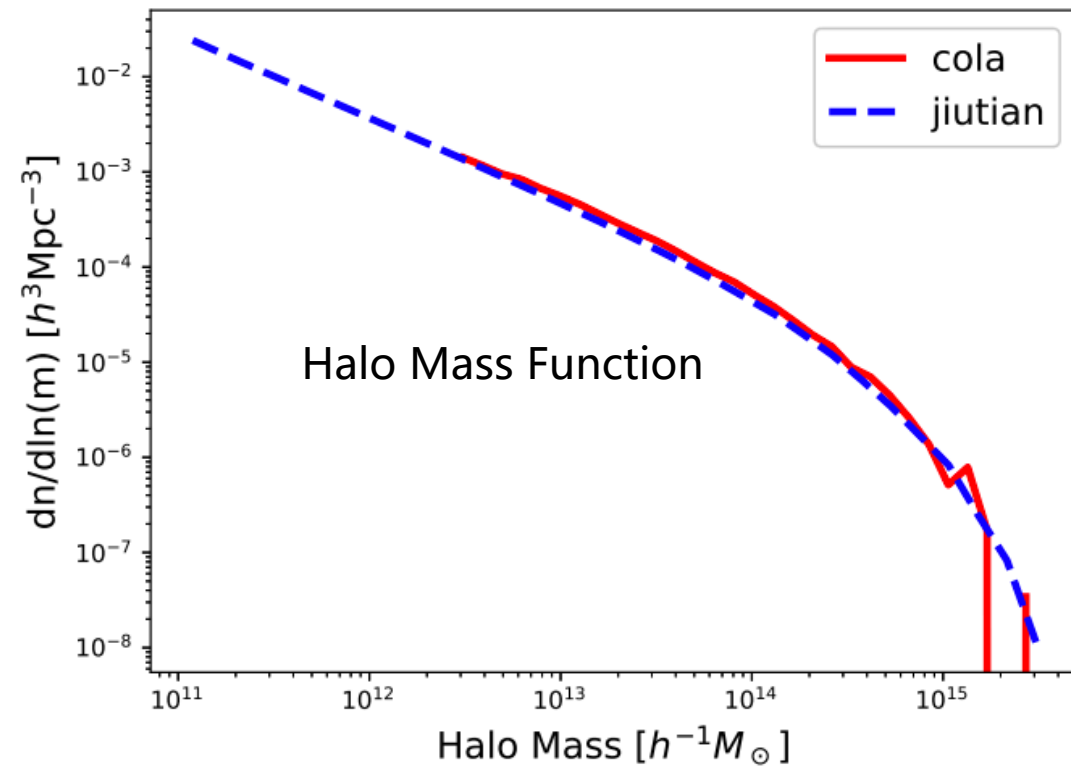
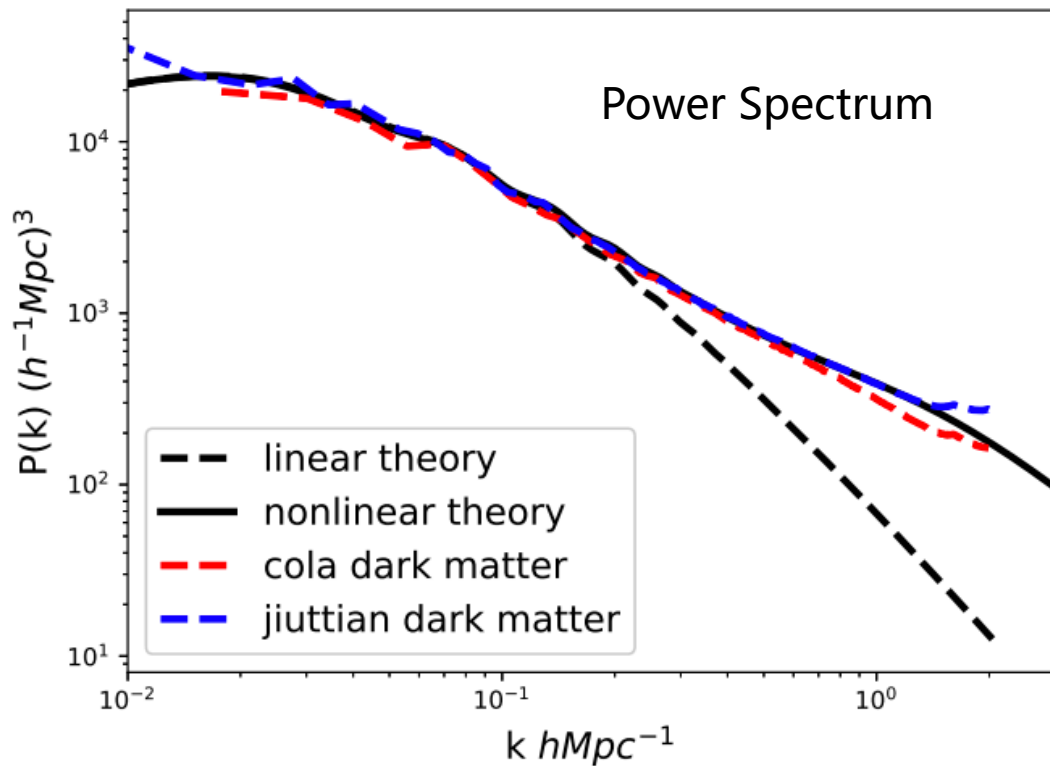
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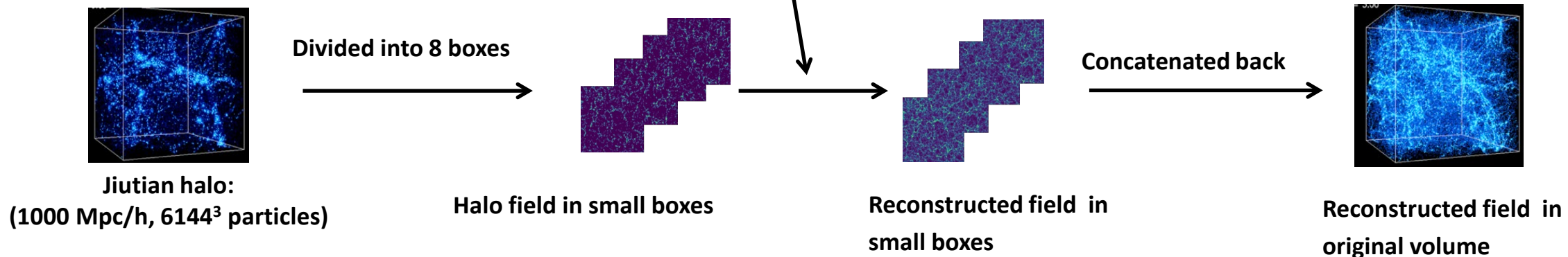
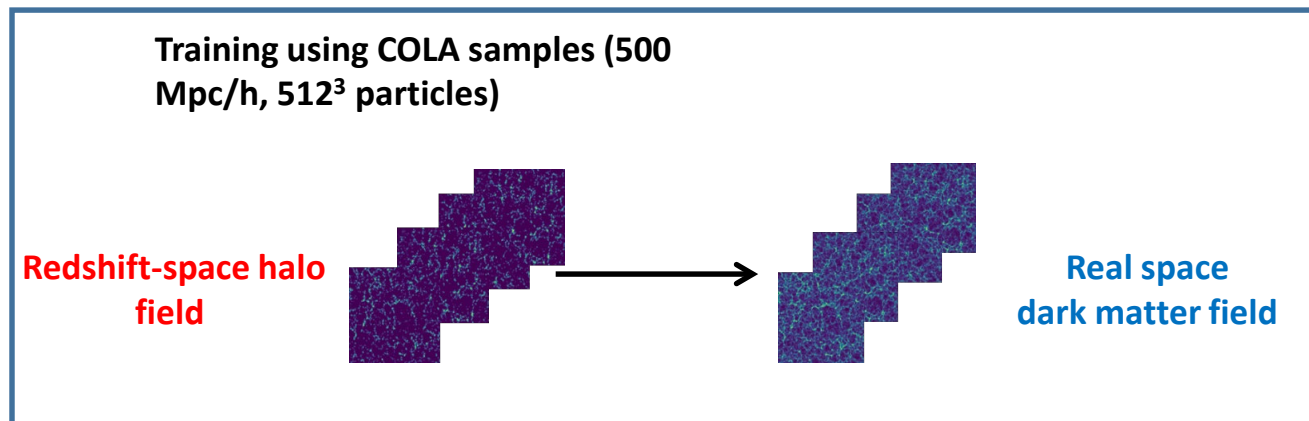
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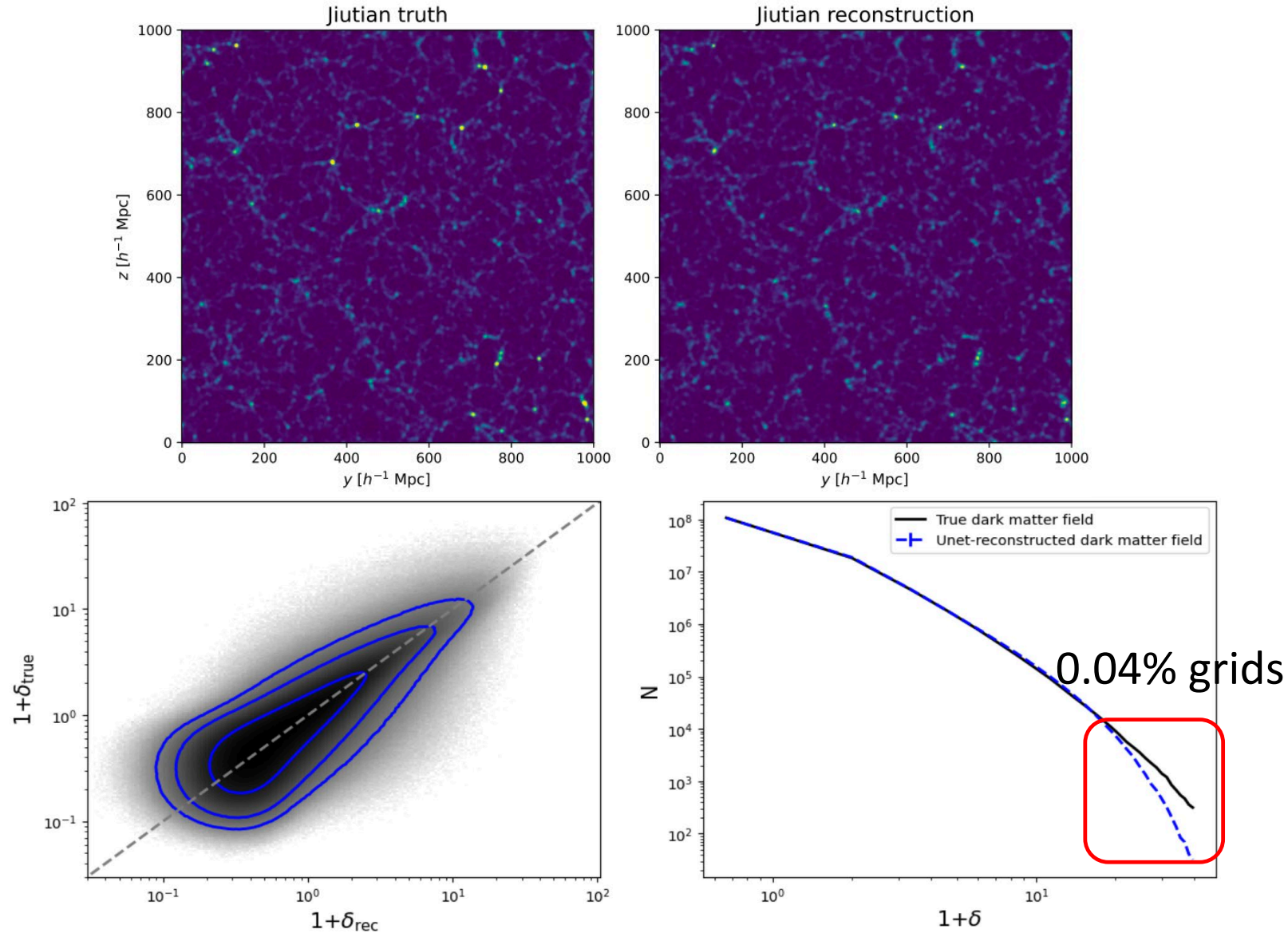
Application to Jiutian





Results: Jiutian simulation

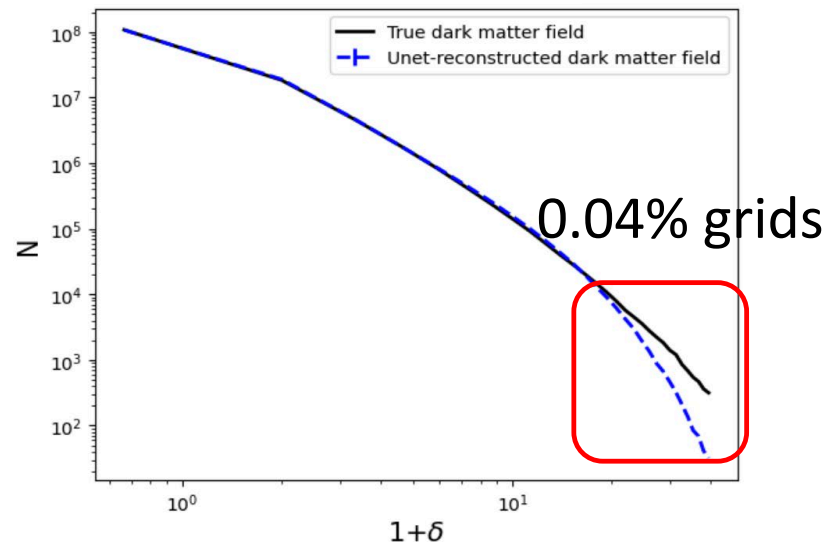
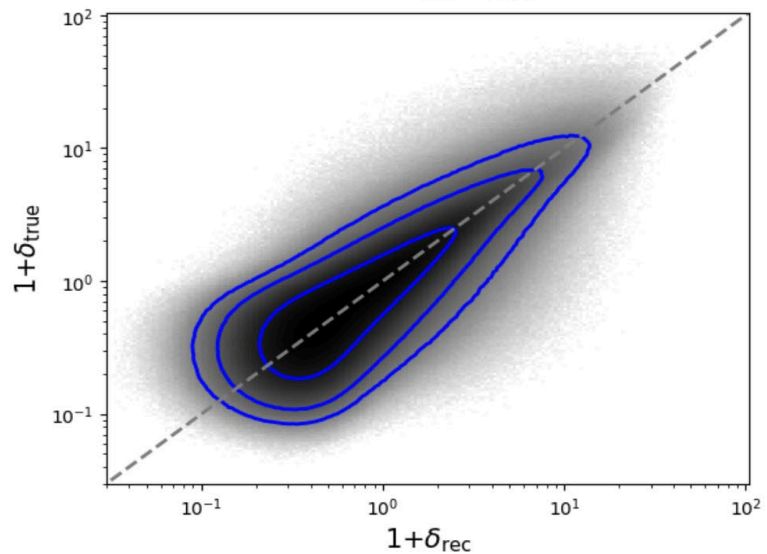
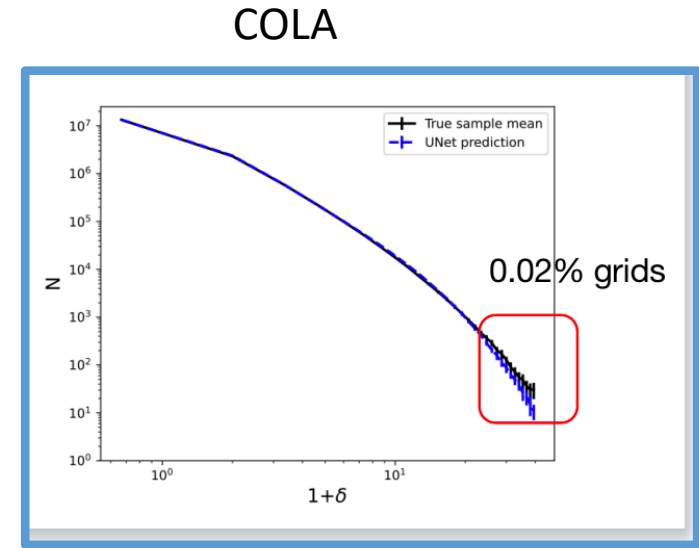
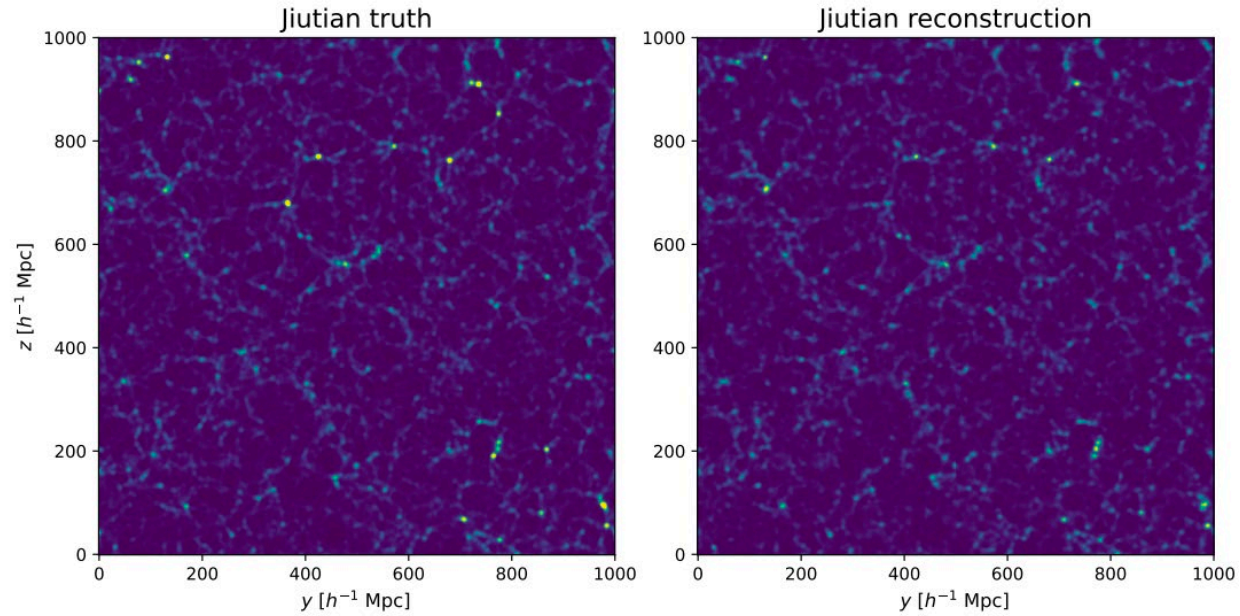
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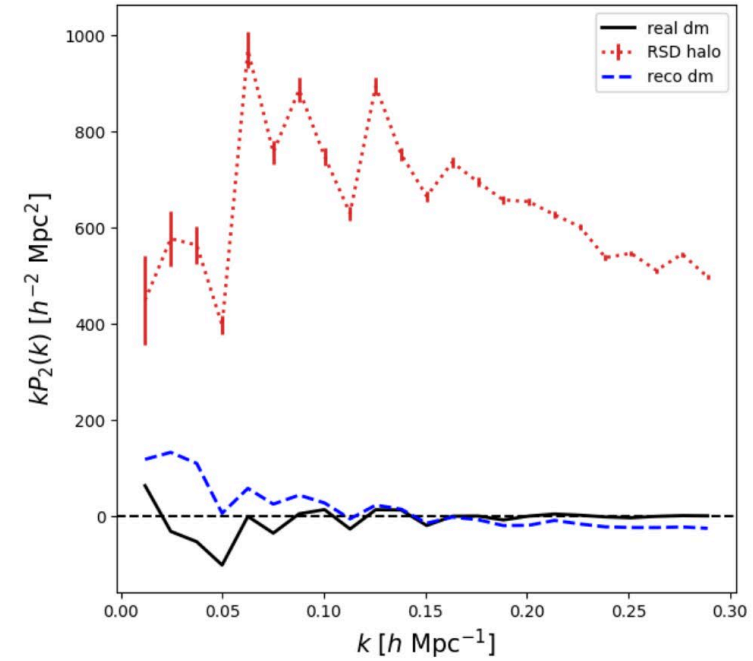
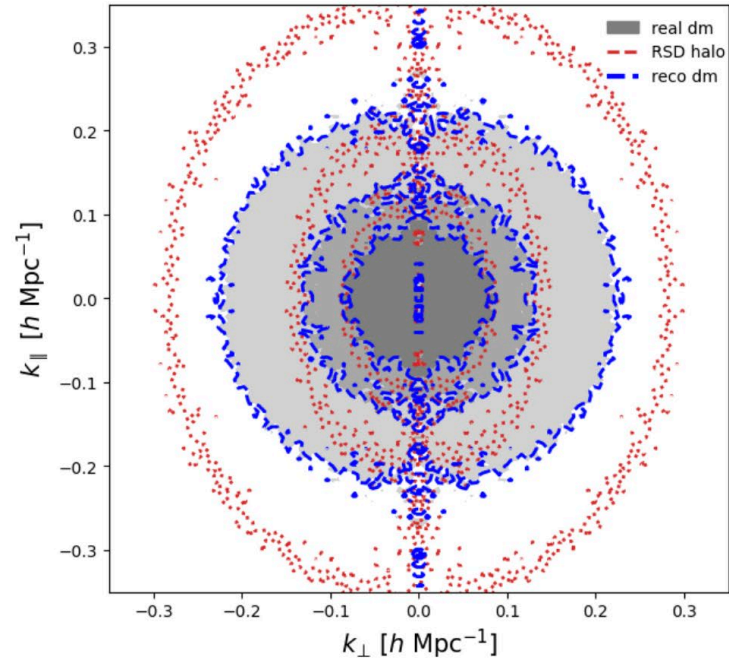
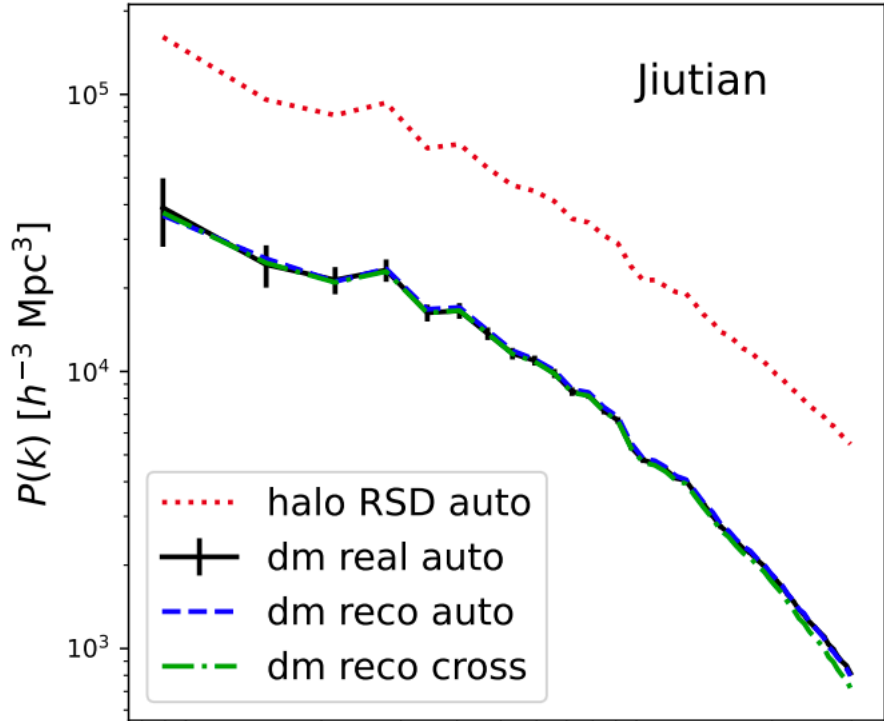
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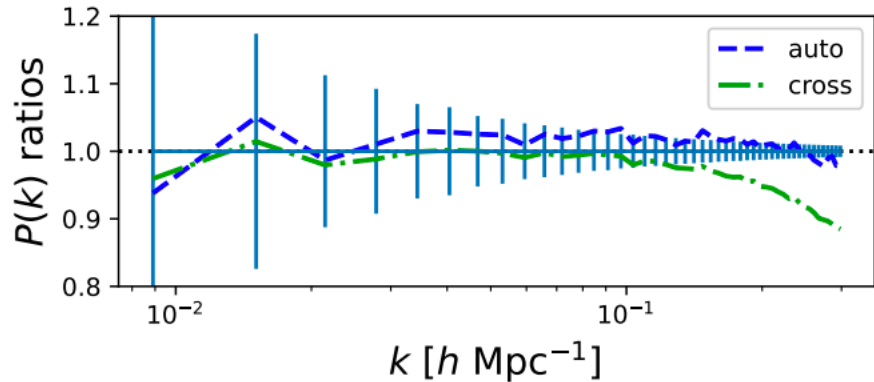


Results: Jiutian simulation

- Reconstructing dark matter density field based on UNet



The real-space $P(k)$ is also recovered accurately, with only small reduction of the cross-correlation power spectrum at 1% and 10% levels at $k = 0.1$ and $0.3 h \text{ Mpc}^{-1}$, respectively.





Application to ELUCID simulation

Check the impact of cosmology

- COLA and Jiutian simulations :

Planck2018 cosmology

$$\Omega_m = 0.3111, \Omega_\Lambda = 0.6889, h = 0.6766, \Omega_b = 0.049, \sigma_8 = 0.817.$$



Application to ELUCID simulation

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Planck2018 cosmology

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- ELUCID simulation (500Mpc/h, 3072³ particles):

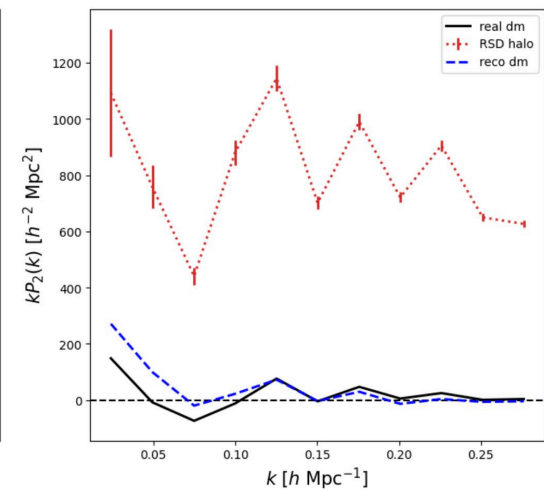
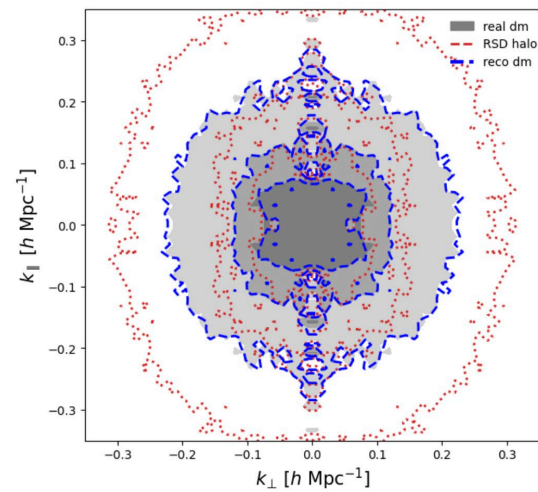
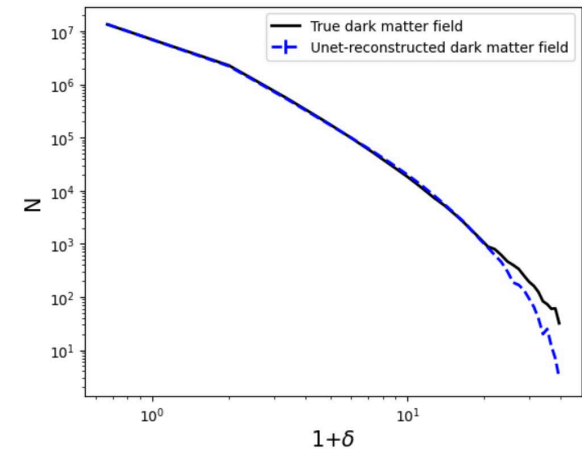
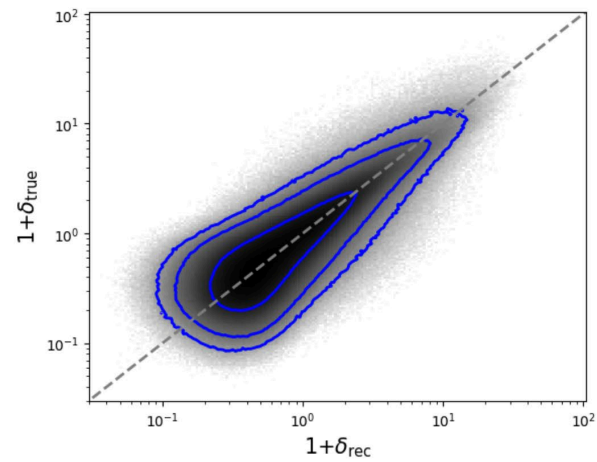
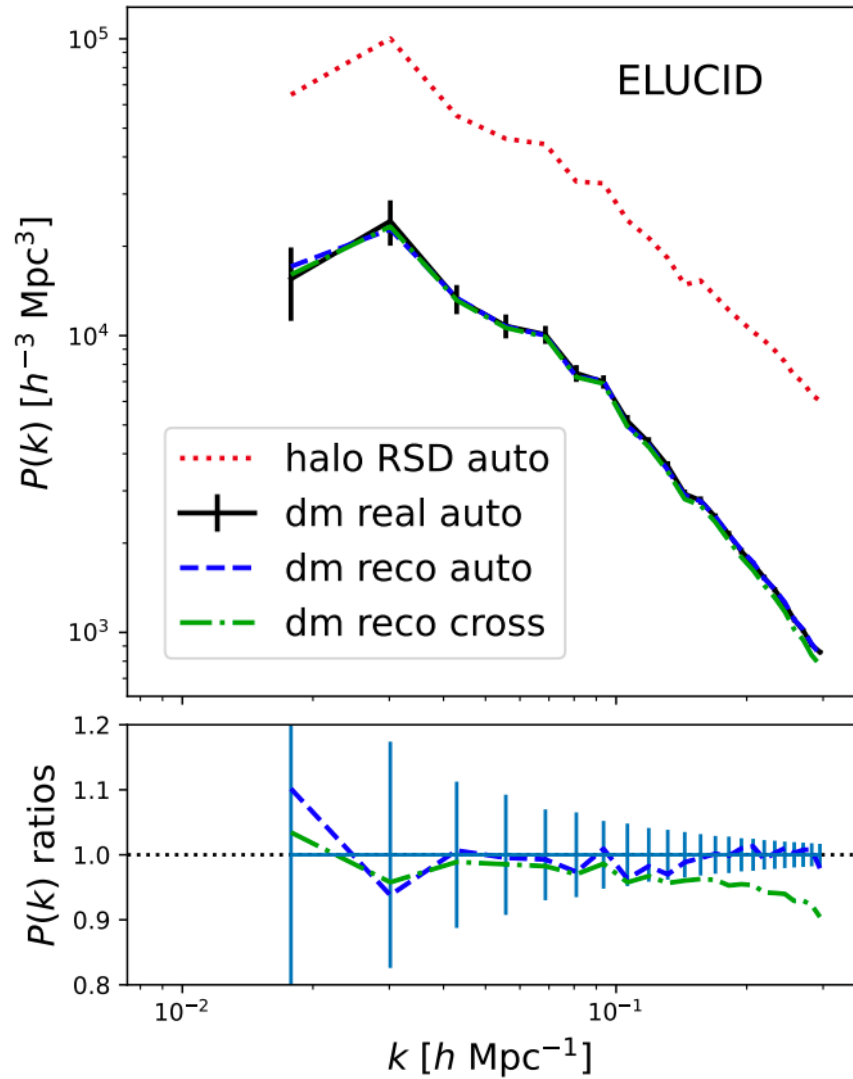
WMAP5 cosmology

$$\Omega_m = 0.258, \Omega_\Lambda = 0.742, \Omega_b = 0.044, h = 0.72, \sigma_8 = 0.80$$



Results: ELUCID simulation

- No large distinction of the results between the WMAP5 and Planck18 cosmology





Testing: velocity field reconstruction

- Reconstruct velocity field

VS.

Halo density field $\delta_h(k)$ with a bias b_{hm}

$$v(k) = H a f(\Omega) \frac{ik}{k^2} \frac{\delta_h(k)}{b_{hm}}$$

(Wang et al 2012,
Shi et al 2016)



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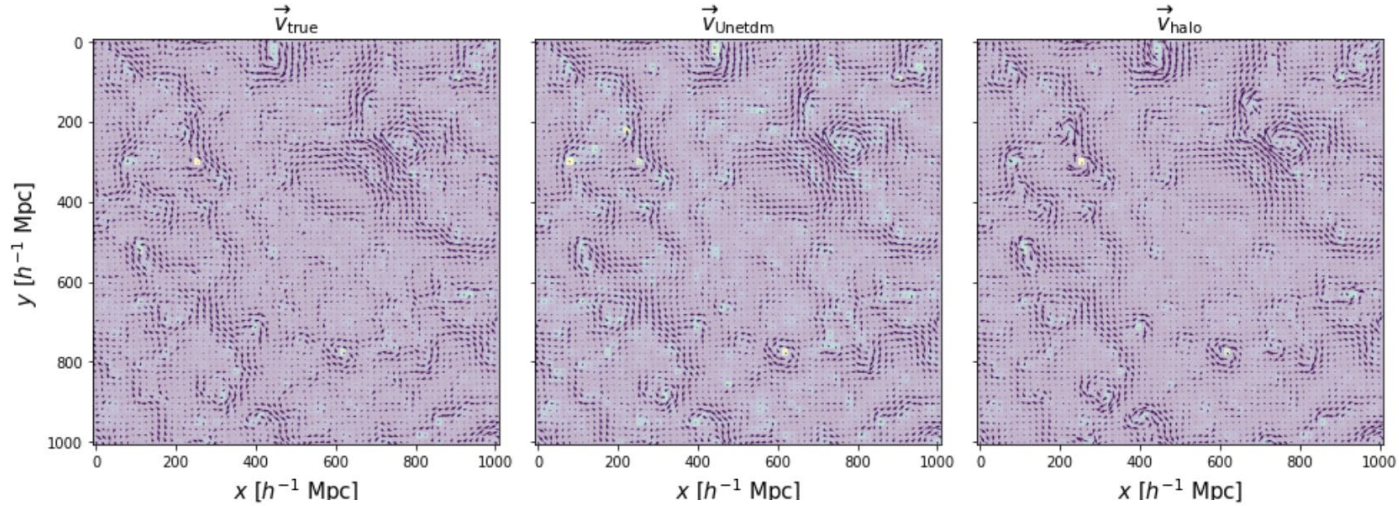
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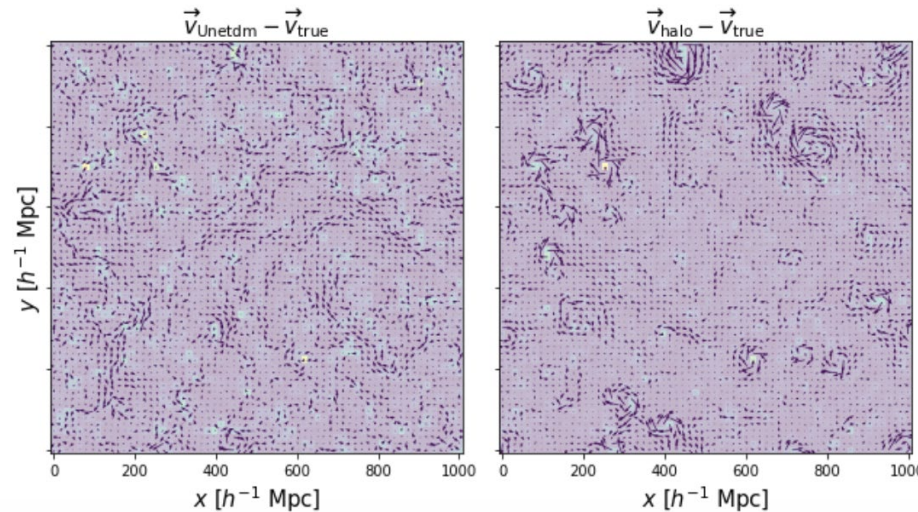
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Velocity field



Velocity difference field

UNet dark matter



Halo-based with linear bias



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$$v(k) = H a f(\Omega) \frac{ik}{k^2} \frac{\delta_h(k)}{b_{hm}}$$

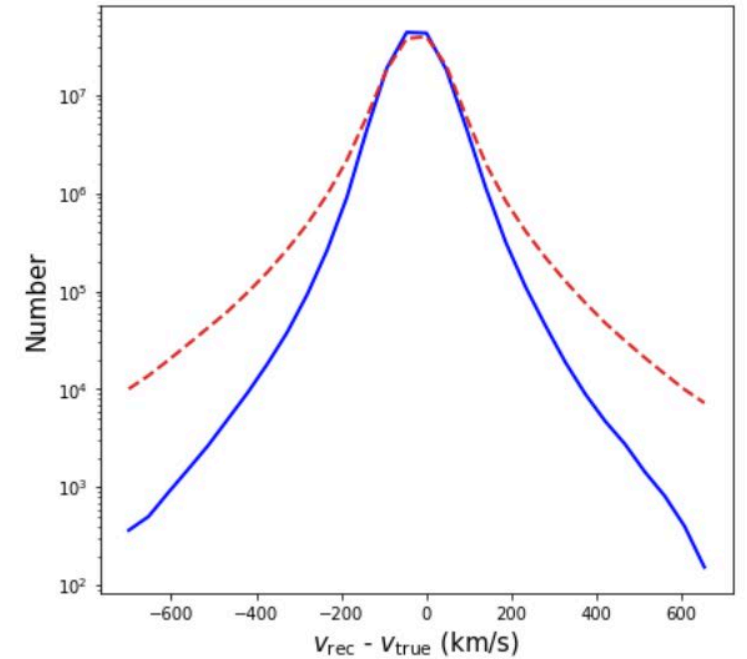
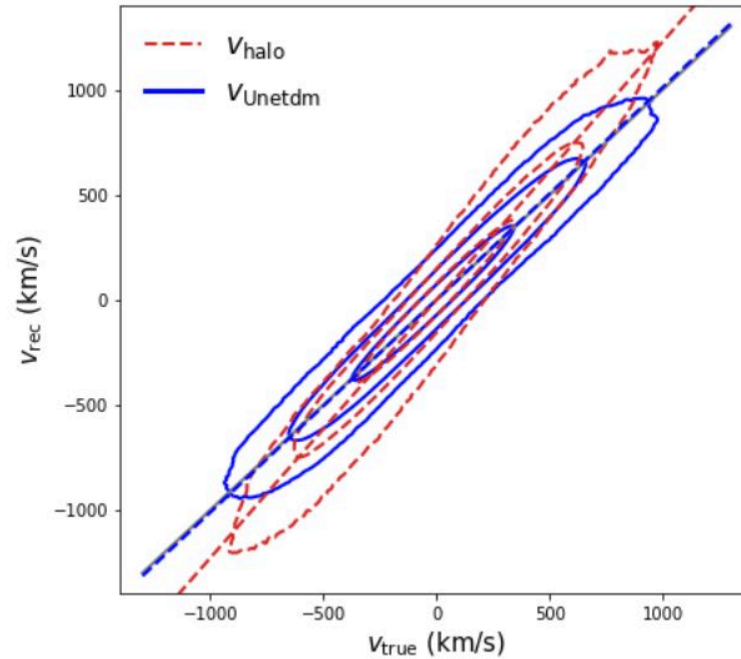
(Wang et al 2012, Shi et al 2016)

Slope Scatter

Halo : 1.15 78.2 km/s

UNet : 1.01 57.0 km/s

- Unbiased relation
- 21.1% scatter error reduction

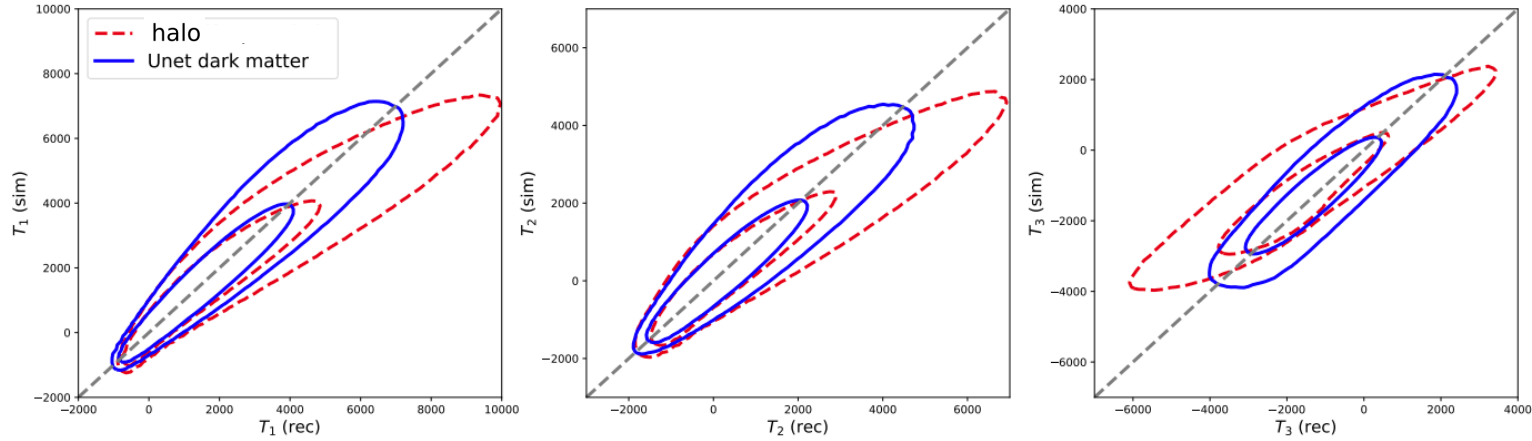


The three contours encompass 67%, 95%, and 99% of the grid cells

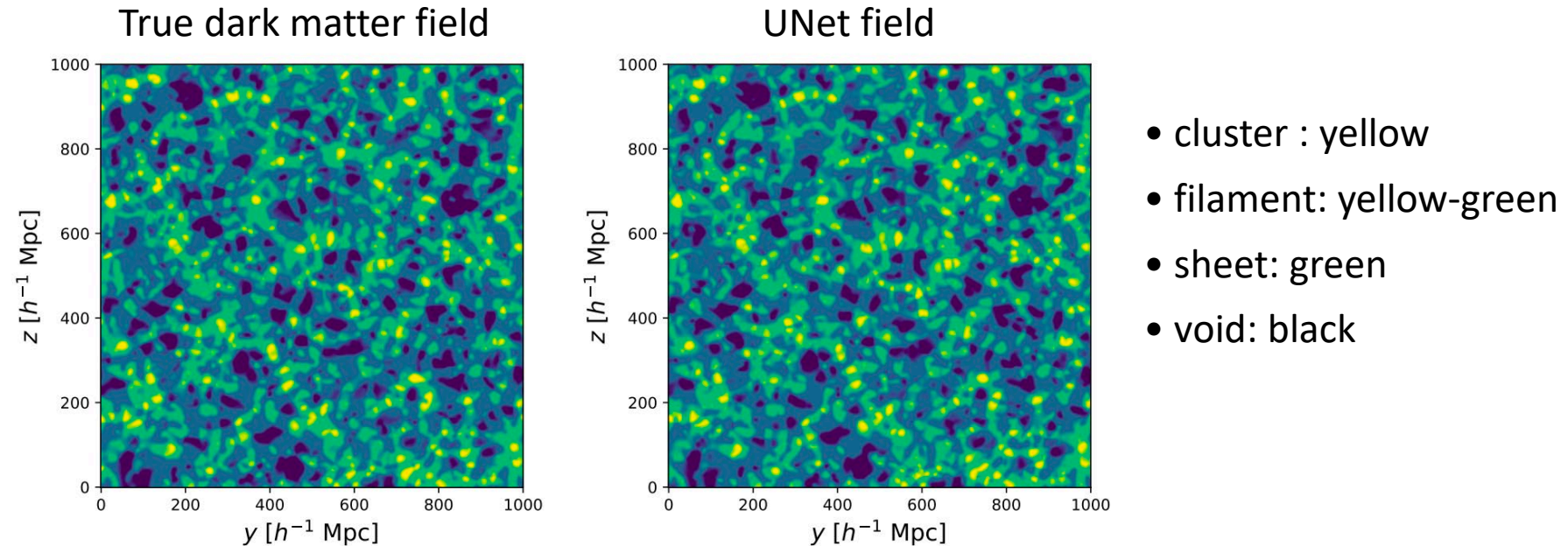


Testing: tidal field reconstruction

- Reconstruct tidal field:



- Classification of the large-scale structure:





Summary & Conclusions

1) Method: Reconstruct the cosmic density field from the redshift-space halo field based on U-net

2) Testing:

- Three simulations: COLA, Jiutian and ELUCID
- Statistics: projected density, density-density relation, histogram, 1D & 2D $P(k)$
- Fields: density, velocity and tidal fields

3) Conclusions:

- Accurate reconstruction with only 1% and 10% reduction of the cross $P(k)$ at $k = 0.1$ and $0.3 h \text{ Mpc}^{-1}$
- RSD corrected successfully
- Low-resolution-COLA-trained network generalizes to the typical high-resolution N-body simulation
- U-net-based field outperforms the traditional method in accurately recovering the velocity & tidal field



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