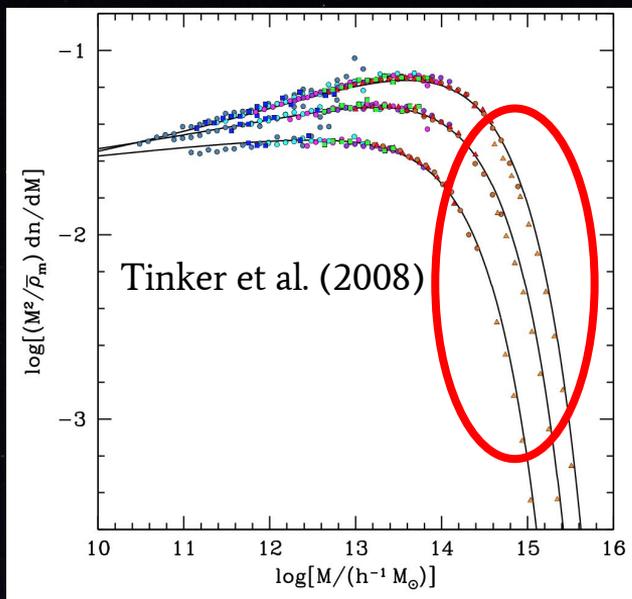


# Splashback Radius as a Probe of Cosmology and Astrophysics

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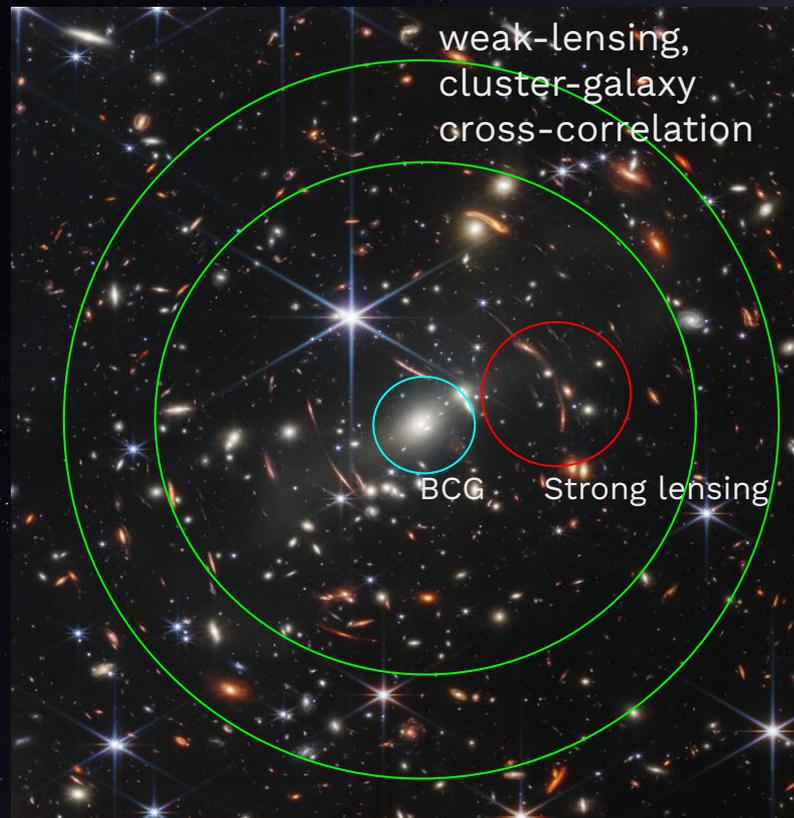
Tae-hyeon Shin  
Halo Boundary Workshop  
Shanghai, China  
May 26, 2025

# THE GALAXY CLUSTERS



Galaxy clusters live in the **high-mass tail** of the halo mass function  $\Rightarrow$  very sensitive to the **growth of the structure** ( $\Omega_m$  and  $\sigma_8$ )

Thus, it is important to accurately define/measure the **mass** of the cluster

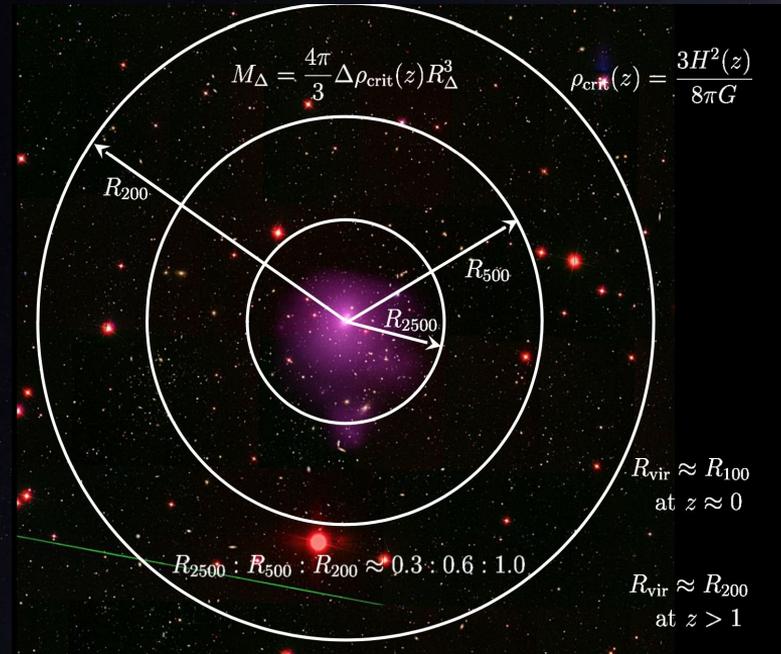


# THE BOUNDARY OF HALOS

$R_\Delta$ : boundary based on the overdensity level

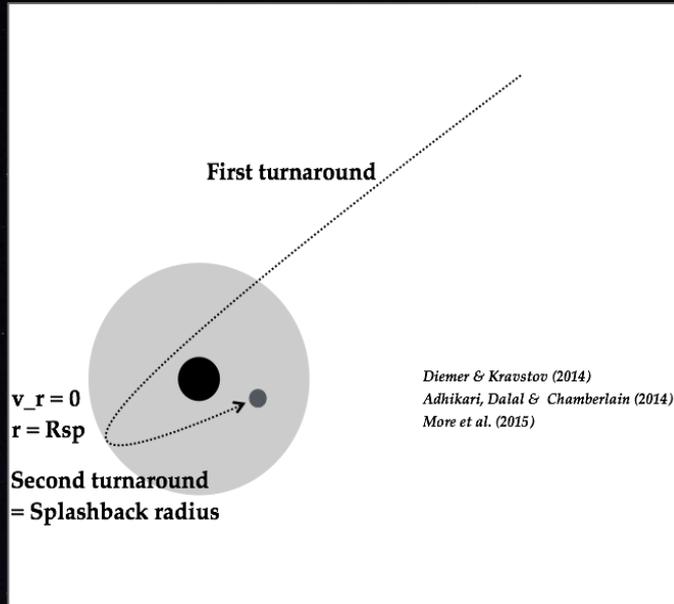
- **Pseudo-evolution** (Diemer+13):  
change in the background density
- Halos **continuously accrete** matter:  
no radius within which the particles  
are fully virialized

Then, how can we find a **physical boundary**  
of halos?

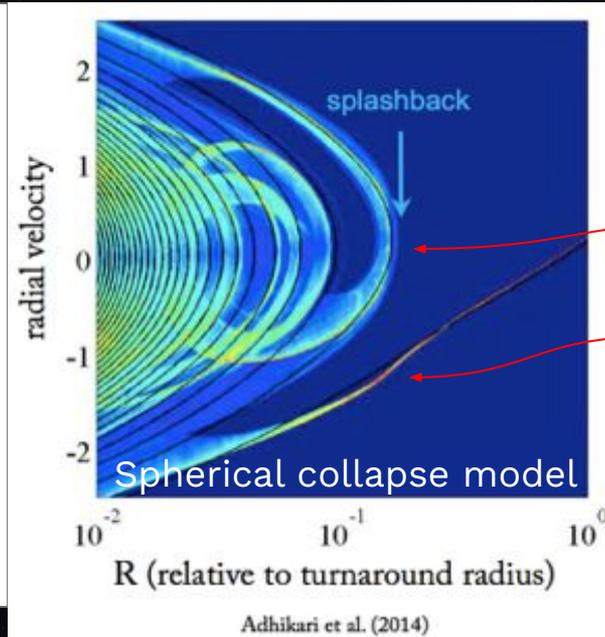


Credit: Andrey Kravtsov

# THE BOUNDARY OF HALOS



Credit: Chihway Chang



+Gunn & Gott 1972  
Fillmore & Goldreich 1984  
Bertschinger 1985

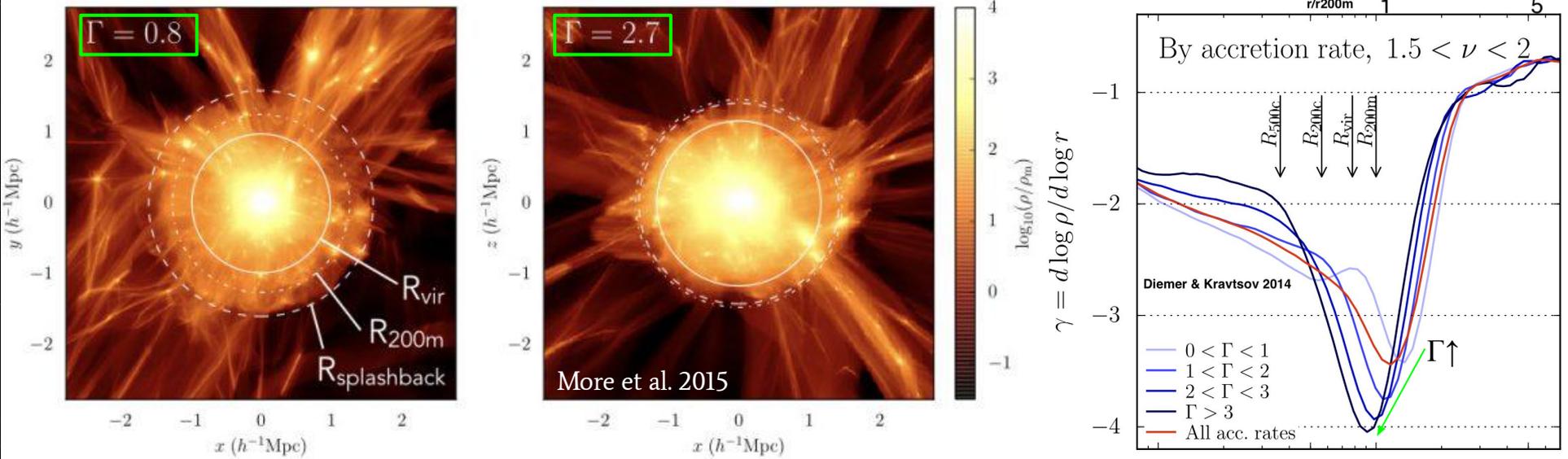
Splashback radius demarcates the **boundary** between the **multistreaming** region (1-halo) and the **infall** stream (2-halo)

Infalling particles form a sharp **physical** boundary around the **first apocenters** ⇒ splashback radius

# SPLASHBACK & MASS ACCRETION

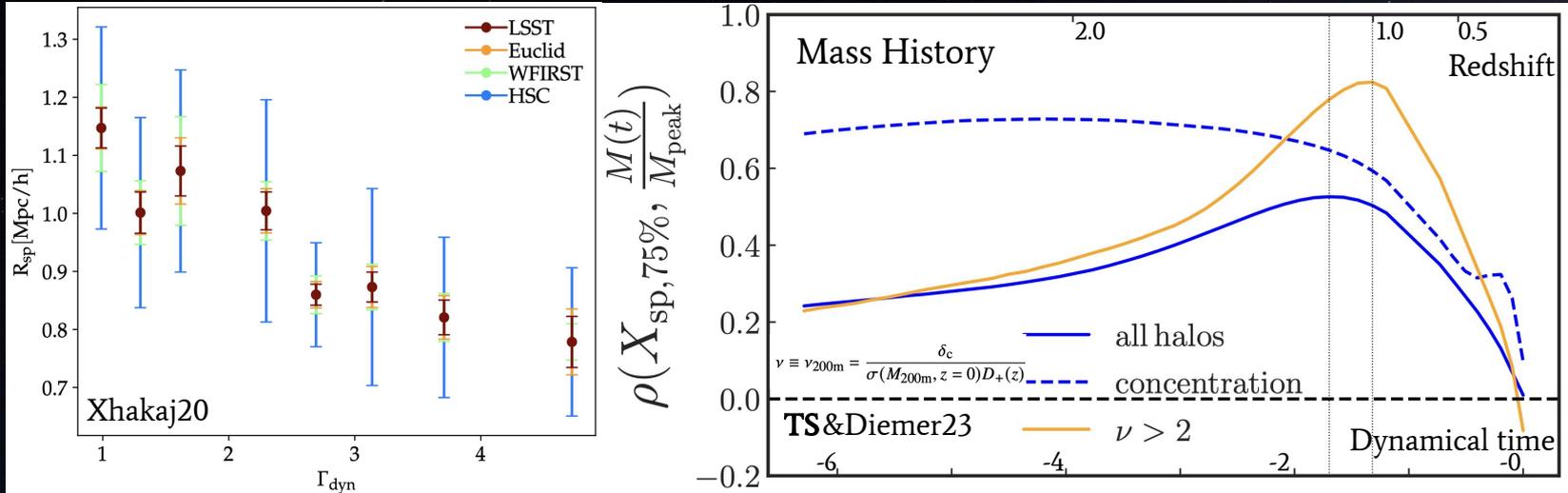
- Halos exhibit a **sharp decline in density profile** around the first orbital apocenters of accreting particles
- Splashback radius,  $r_{sp}$ , represents the location of **the steepest logarithmic slope** and it majorly depends on the **recent mass accretion rates** of halos, given the mass

+Shi16a,b  
Sugiura20, 23

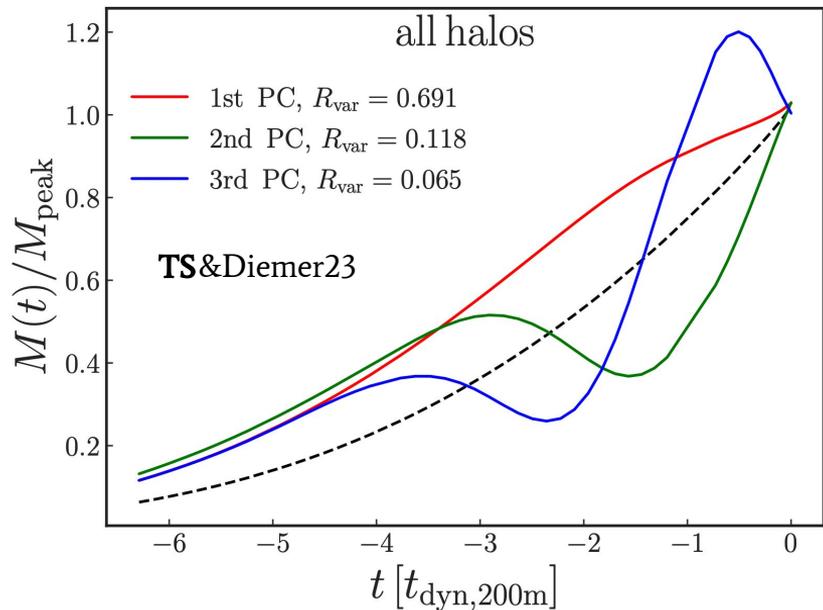


# SPLASHBACK & MASS ACCRETION

- Splashback radius is the most sensitive to the mass accretion over the recent **1 dynamical time** ( $2R_{200m}/V_{200m}$ ),  $\Gamma_{200m}$ , while concentration retains information of **earlier times** (TS&Diemer 2023)
- With the statistical power of **LSST** and **Euclid**, we can **directly constrain the mass accretion rate** of halos using splashback radius (Xhakaj+2020), therefore infer **cosmology**



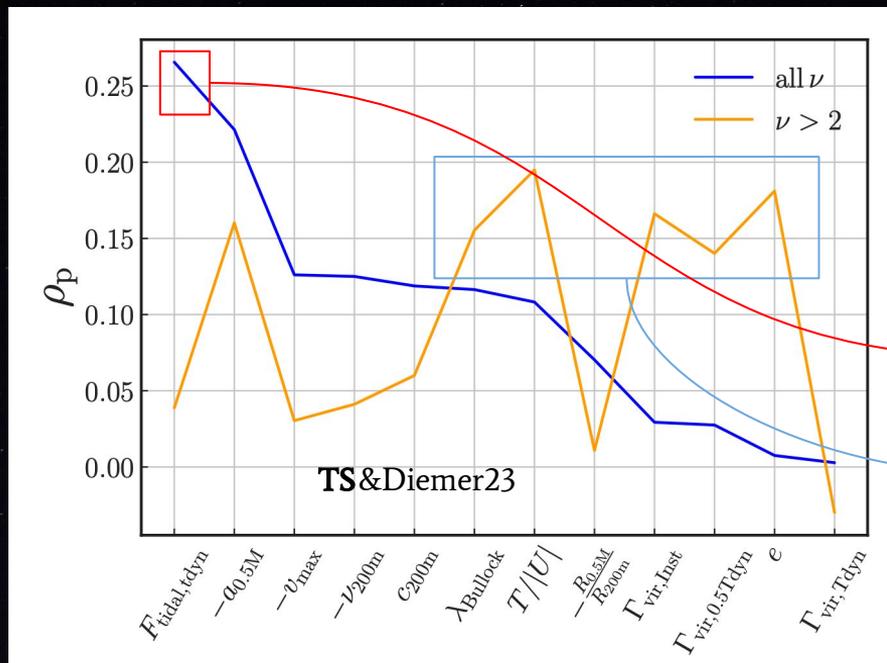
# SPLASHBACK & MA HISTORY



**Figure B1.** The first three principal components (red, green, blue) of the fractional mass history  $M(t)/M_{\text{peak}}$  (black dashed).  $R_{\text{var}}$  represents the explained variance ratio of each component.

- ~70% of the variation in the individual mass accretion history can be summarized with **one** principal function, which shows a high correlation (~0.76) to splashback radius for cluster-sized halos  
⇒ splashback for MAH
- It is driven by the high correlation (-0.89) between the principal function and  $\Gamma_{200\text{m}}$ .

# SPLASHBACK & OTHER PROPERTIES



Partial correlation between  $R_{\text{sp}}$  and other halo properties, w.r.t.  $\Gamma_{200m}$

- Compared with the recent mass accretion rate ( $\Gamma_{200m}$ ), other halo properties show subordinate levels of correlation to  $R_{\text{sp}}$
- For low-mass halos (blue, typically galaxy-sized) the effect of tidal force is not negligible, while for group- and cluster-sized halos there are hints that recent mergers may perturb the splashback radius

# CONSTRAINING $R_{SP}$ FROM DATA

WL, cluster-galaxy correlation

$$\rho(r) = \rho^{\text{coll}}(r) + \rho^{\text{infall}}(r)$$

$$\rho^{\text{coll}}(r) = \rho^{\text{Ein}}(r) f_{\text{trans}}(r)$$

$$\rho^{\text{Ein}}(r) = \rho_s \exp\left(-\frac{2}{\alpha} \left[\left(\frac{r}{r_s}\right)^\alpha - 1\right]\right)$$

$$f_{\text{trans}}(r) = \left[1 + \left(\frac{r}{r_t}\right)^\beta\right]^{-\gamma/\beta}$$

$$\rho^{\text{infall}}(r) = \rho_0 \left(\frac{r}{r_0}\right)^{-s_e} \quad \text{Truncation of the Einasto profile}$$

OR

$$\rho(r) = \rho_m \left( \delta_1 \left[ \frac{\delta_1}{\delta_{\text{max}}} + \left(\frac{r}{R}\right)^s \right]^{-1} + 1 \right) \quad \text{Diemer\&Kravtsov14}$$

Limiting central amplitude

The model used so far



$$\rho_{\text{orb}} = \rho_s e^{S(r)} \quad \gamma \equiv \frac{d \ln \rho}{d \ln r} = r \frac{dS}{dr} \quad S(r) = \int \frac{\gamma(r)}{r} dr$$

Orbiting (1-halo) term

$$\gamma(r) = -2 \left[ \left(\frac{r}{r_s}\right)^\alpha - \left(\frac{r}{r_t}\right)^\beta \right]$$

Halos have **two** different characteristic radii (c.f. NFW profile has only 1)

Scale radius    Truncation radius

$$S(r) = -\frac{2}{\alpha} \left[ \left(\frac{r}{r_s}\right)^\alpha - 1 \right] - \frac{1}{\beta} \left[ \left(\frac{r}{r_t}\right)^\beta - \left(\frac{r_s}{r_t}\right)^\beta \right]$$

**NEW MODEL (Diemer22)**

Einasto

Truncation

$$\rho(r) = \rho_m \left( \delta_1 \left[ \left(\frac{\delta_1}{\delta_{\text{max}}}\right)^{\frac{1}{\zeta}} + \left(\frac{r}{R}\right)^{\frac{s}{\zeta}} \right]^{-\zeta} + 1 \right)$$

transition smoothness parameter (set to 0.5)

Setting the maximum amplitude at the center

$$\rho(r) = \rho_m \left( \frac{\delta_1}{\sqrt{(\delta_1/\delta_{\text{max}})^2 + (r/R)^{2s}}} + 1 \right)$$

Infalling (2-halo) term

# CLUSTER-GALAXY CROSS-CORRELATION

The two-point correlation function measures the **excessive probability** of finding two galaxies being separated by a distance of  $R$

$$dP(R) = n_1 n_2 (1 + \omega(R)) dA_1 dA_2$$

$$\omega(r) = \frac{[DD(r) - DR(r) - RD(r) + RR(r)]}{[RR(r)]}$$

(Landy-Szalay estimator)

Thus, the mean-subtracted galaxy surface density around the clusters can be expressed as,

$$\Sigma_g(R) - \langle \Sigma_g \rangle = \langle \Sigma_g \rangle \omega(R)$$

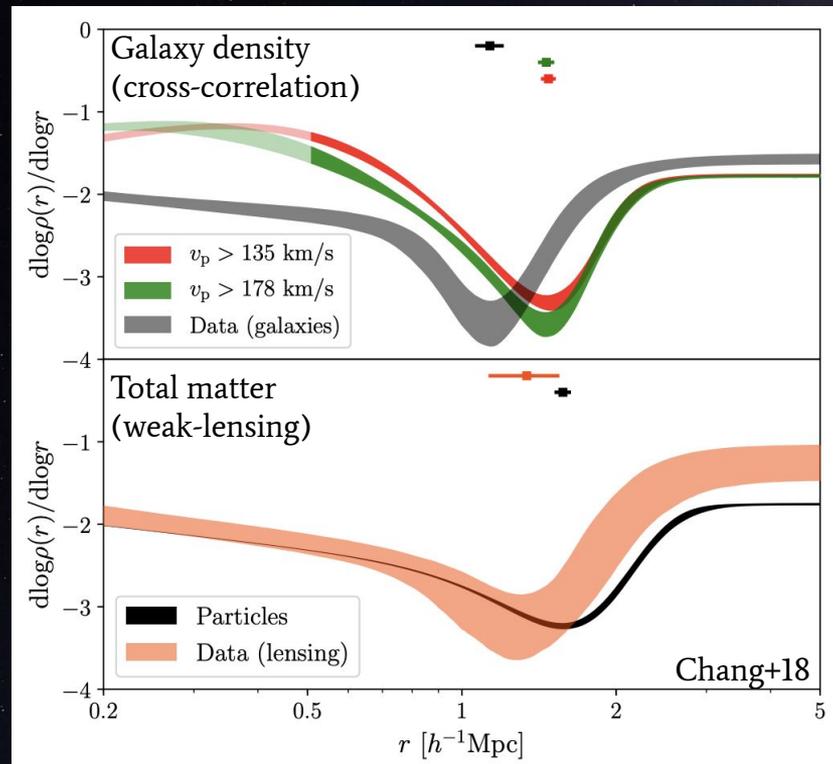
Correlation function picks up the galaxies that are correlated with the clusters: **avoiding the photo-z uncertainties of the galaxies**

# $R_{SP}$ FROM OPTICAL CLUSTERS

**Optically selected** clusters from the Sloan Digital Sky Survey (SDSS) and the Dark Energy Survey (DES) shows **~20% smaller** splashback radius in galaxy density profile than those from simulations (More+16, Baxter+17, Chang+18)

A large fraction of this discrepancy is attributed to the **projection effect** in the optical cluster **selection** (Busch&White17, Zu+17) and cluster LOS orientation (TS+19)

Optical clusters from the Hyper Suprime-Cam (HSC) survey showed splashback feature that is more consistent to theory (different algorithm)



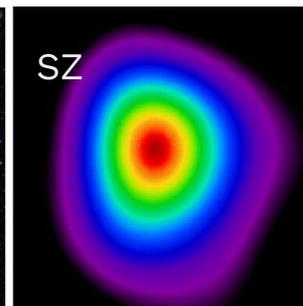
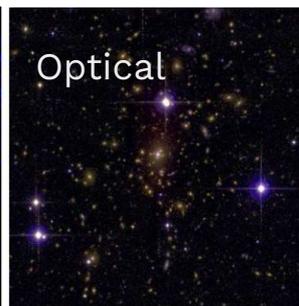
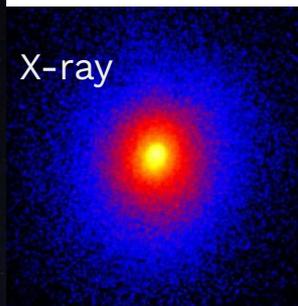
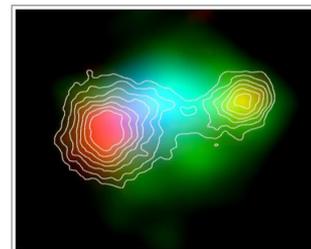
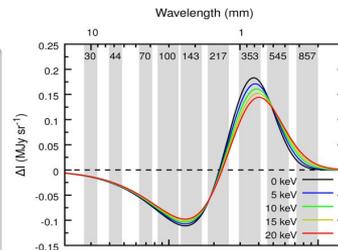
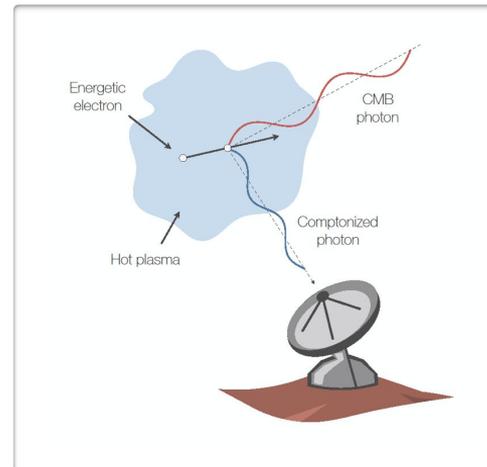
# $R_{SP}$ FROM SZ CLUSTERS

Sunyaev-Zel'dovich effect: CMB photons scattered off the hot gas within the clusters

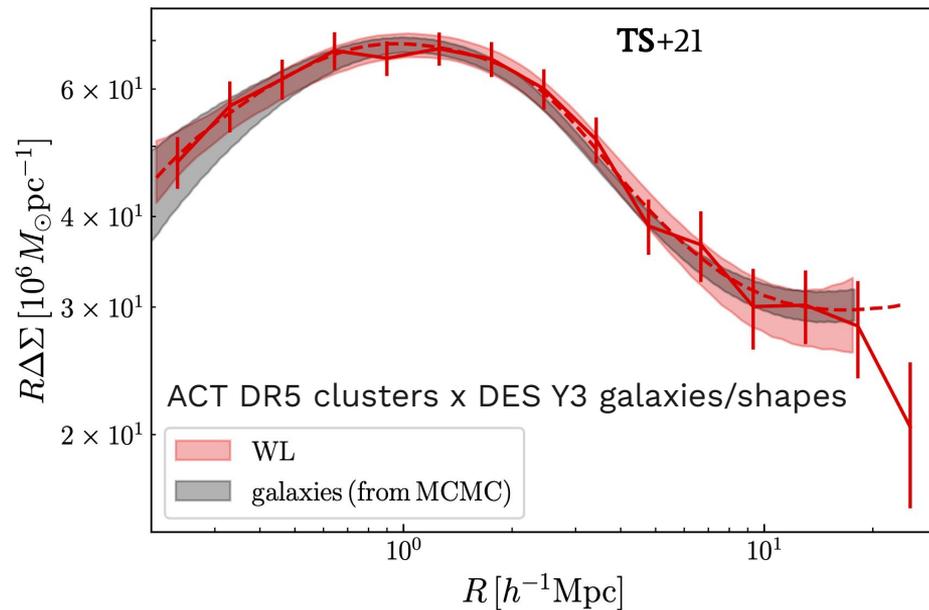
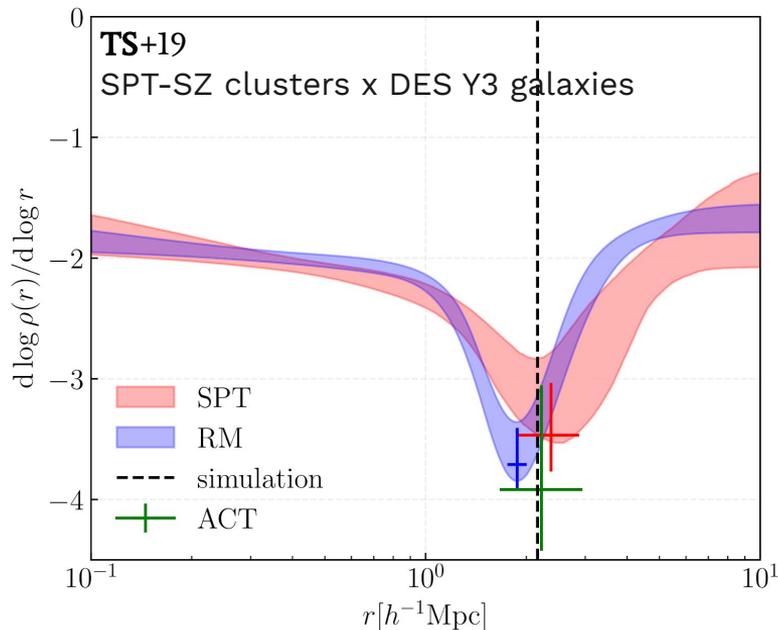
⇒ energy transferred to higher frequencies

## SZ-selected clusters

- Selection is nearly **independent** of the observables in the optical survey
- The SZ signal is expected to correlate **more tightly with cluster mass** than optical richness
- **Less affected** by projection effects
- **More massive & higher redshift** clusters

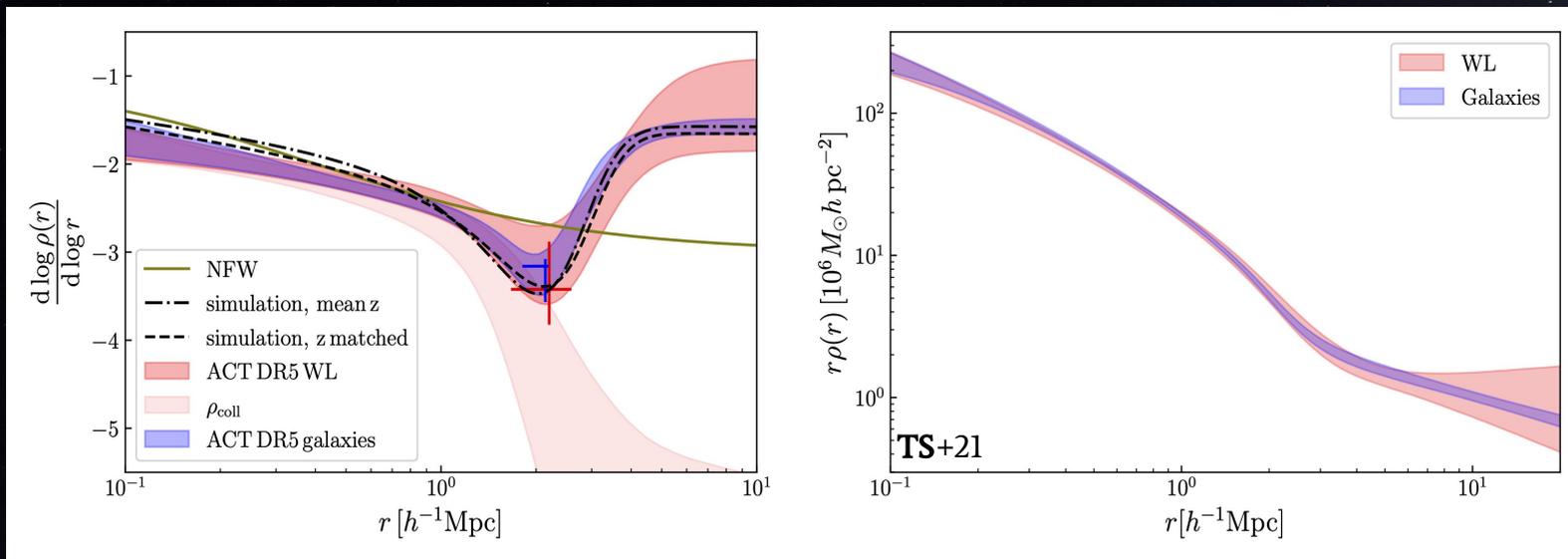


# $R_{SP}$ FROM SZ CLUSTERS



The location of splashback radius for the SZ clusters agrees with that from the theory (N-body simulation)

# $R_{SP}$ FROM SZ CLUSTERS



Furthermore, in massive SZ clusters ( $M_{500c} \sim 3e14 M_{\text{sun}}/h$ ), the galaxy density profile and the total matter profile are surprisingly similar in shape  
 $\Rightarrow$  Gravity being the dominant factor in shaping massive halos

# Assembly bias with $R_{SP}$ of X-ray clusters

<Cluster sample>

X-ray clusters from eROSITA survey (eRASS1)

$Z = [0.1, 0.5]$

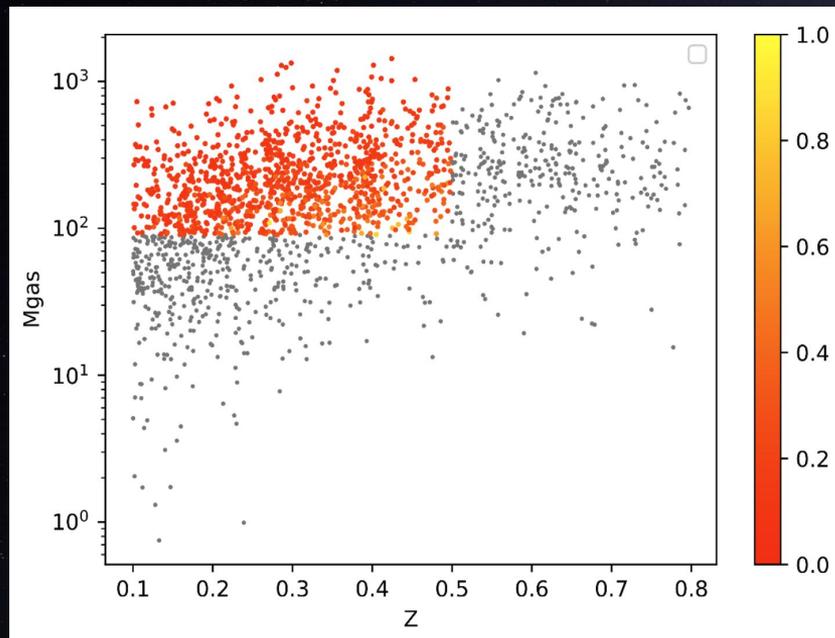
$M_{\text{gas},500c} > 9e12 M_{\text{sun}}$

<Galaxy sample>

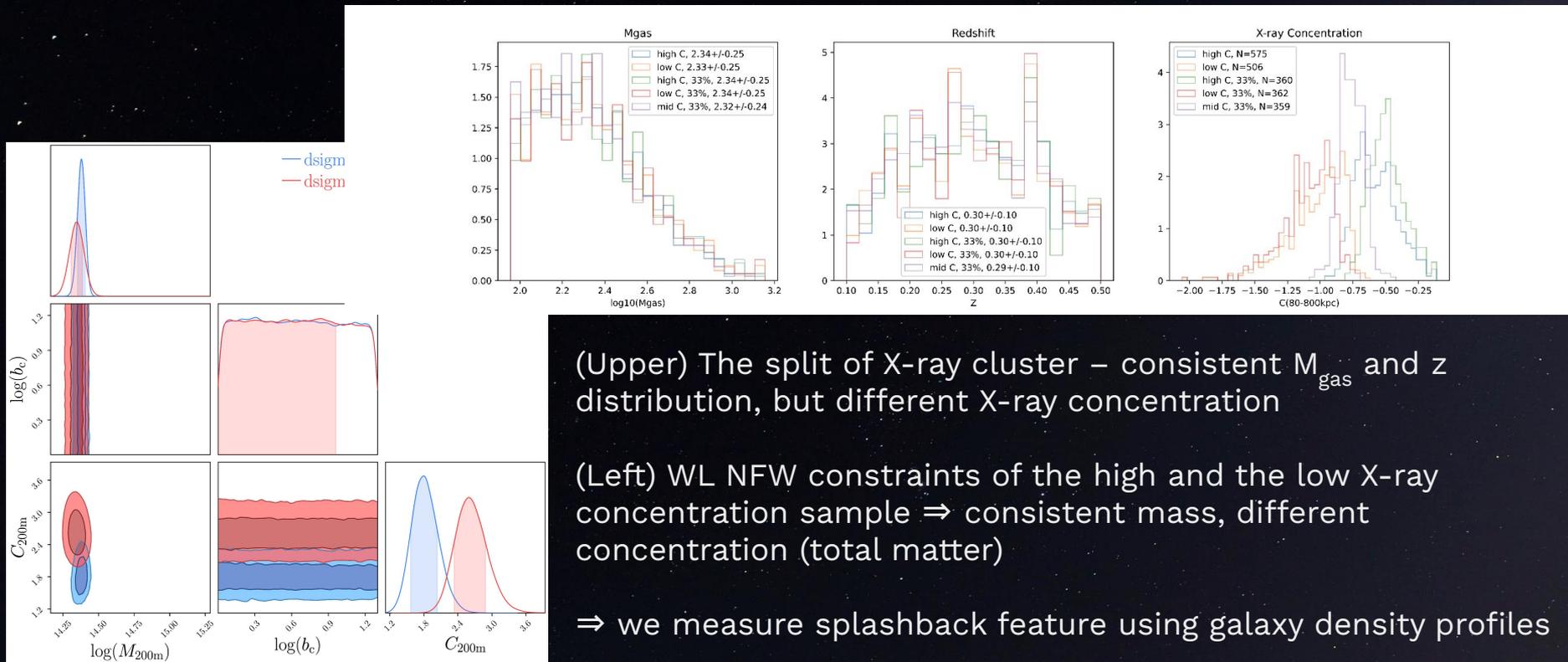
Dark Energy Survey Year-3

⇒ To detect dependence of the splashback feature on secondary halo properties other than the halo mass (assembly bias)

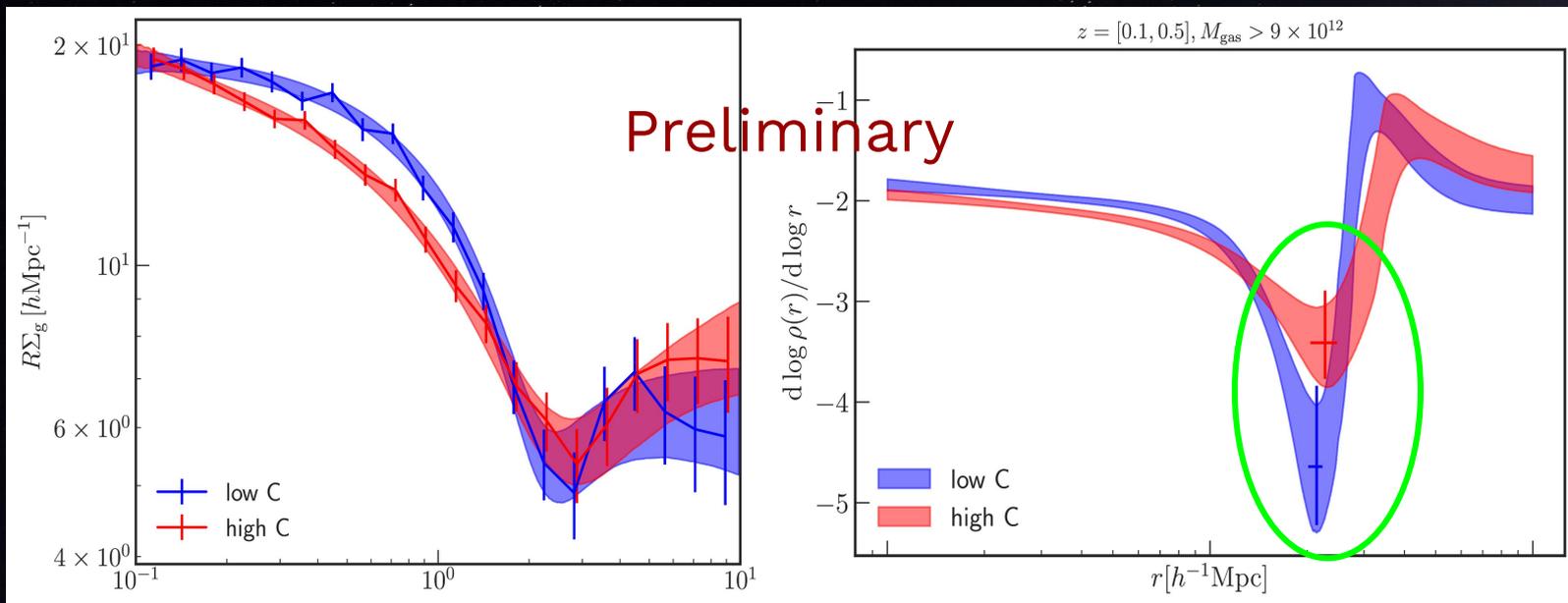
We split the clusters into the low and high **X-ray concentration** sample



# Assembly bias with $R_{SP}$ of X-ray clusters



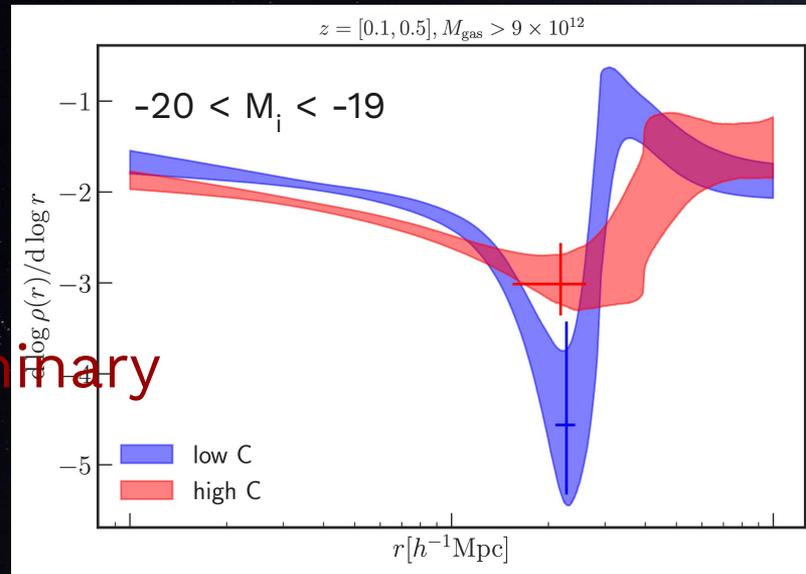
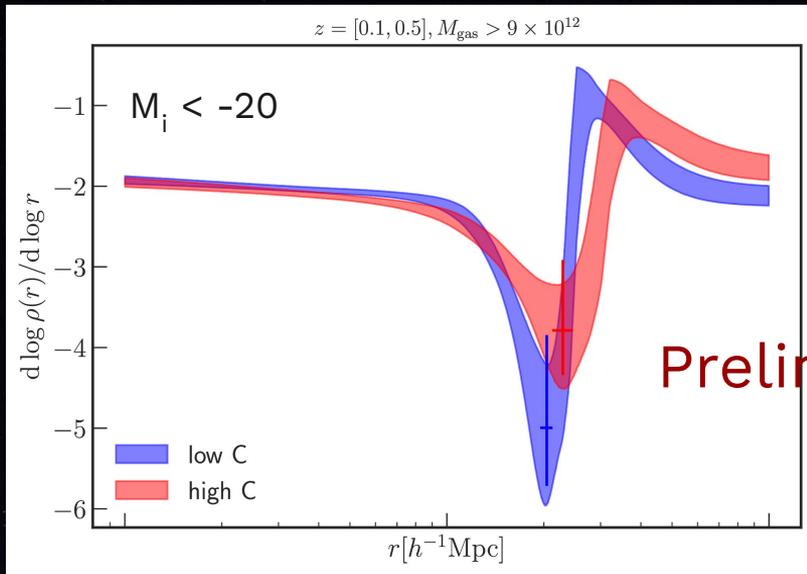
# Assembly bias with $R_{SP}$ of X-ray clusters



Absolute magnitude  $M_i < -19$

Higher concentration  $\Leftrightarrow$  lower mass accretion (older)  $\Leftrightarrow$  larger/shallower splashback radius  
 $\Rightarrow$  consistent with the theoretical expectation (Diemer14, Adhikari14, More15 etc.)

# Assembly bias with $R_{SP}$ of X-ray clusters

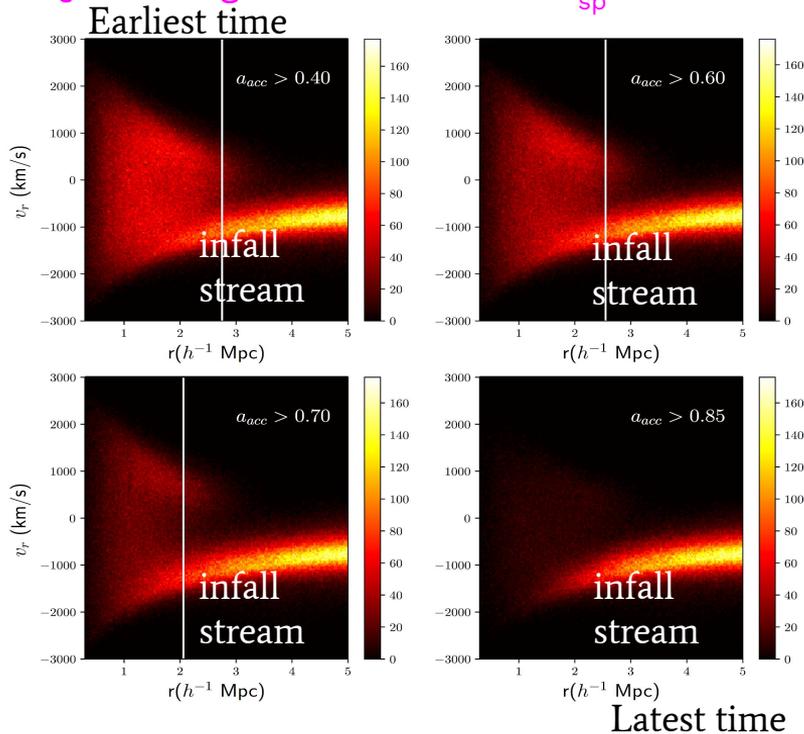


Preliminary

The low and the high magnitude galaxy profiles have qualitatively similar trend in halo concentration with each other, but show a visible trend especially for the high concentration halos  $\Rightarrow$  analysis ongoing to characterize this assembly bias signal as a function of halo and galaxy properties

# $R_{sp}$ AS A QUENCHING CLOCK

SF Quenching  $\Leftrightarrow$  Infall time  $\Leftrightarrow R_{sp}$  Adhikari&TS+21



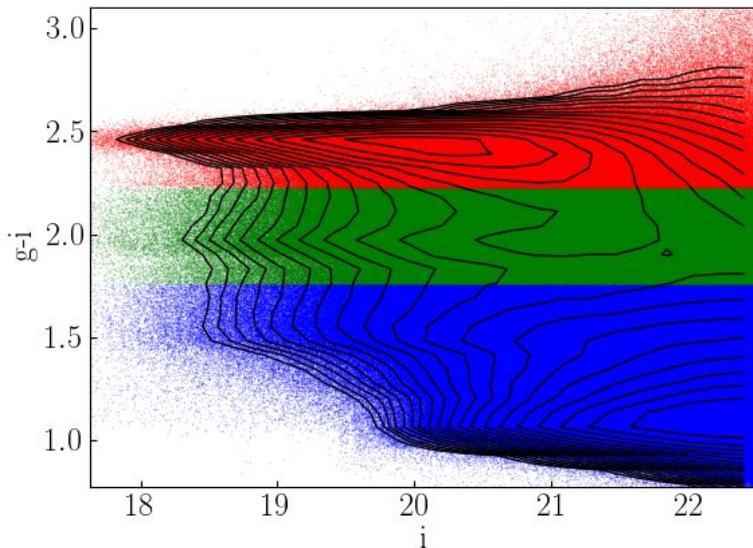
$\Leftarrow$  Subhalos accreted to a cluster at different times in simulation

Galaxies in **the infall stream** do **not** show any splashback feature, while those that have completed at least one crossing show a distinctive splashback feature

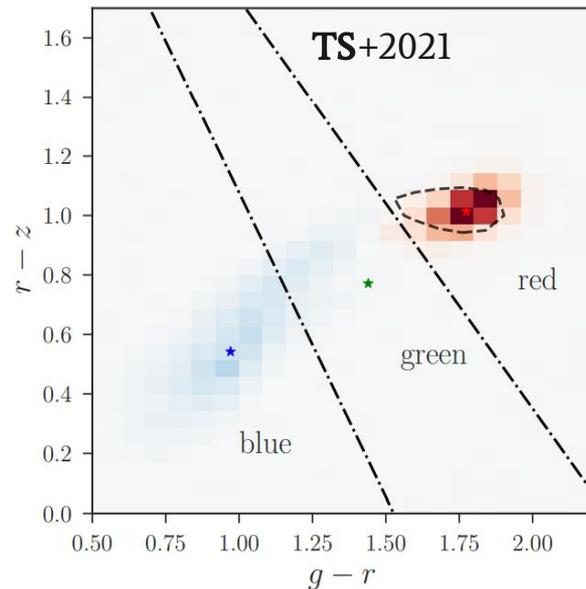
$\Rightarrow$  Can we **separate the infall population** from the observational data?

# $R_{SP}$ AS A QUENCHING CLOCK

TS+2019

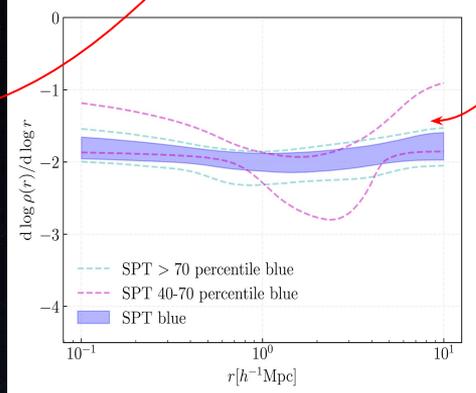
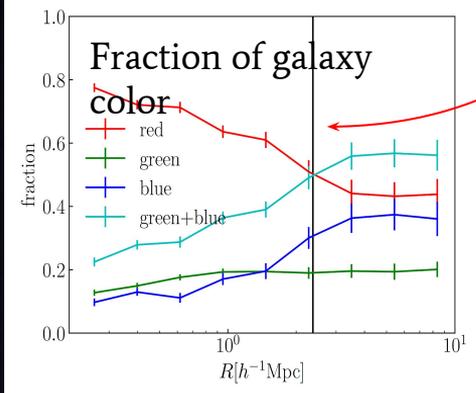
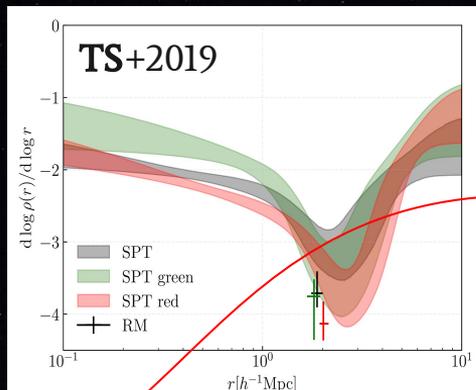
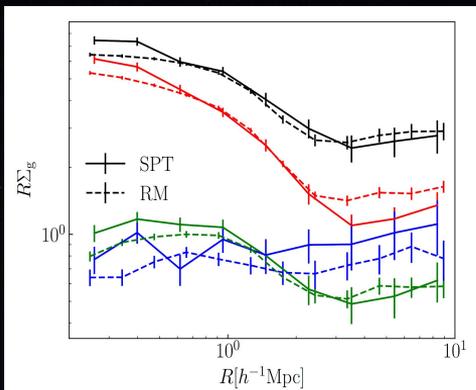


Splitting galaxies simply by color



Splitting galaxies on the color-color space (subtracting random directions from the cluster field)

# $R_{SP}$ AS A QUENCHING CLOCK

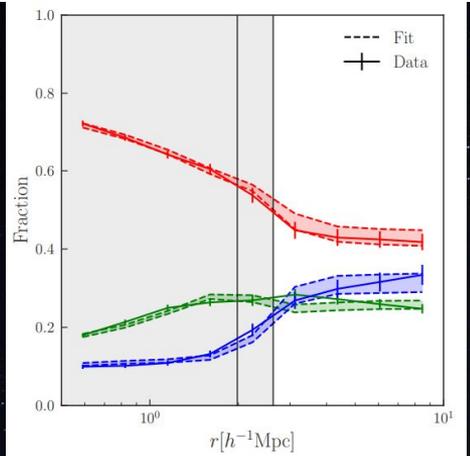
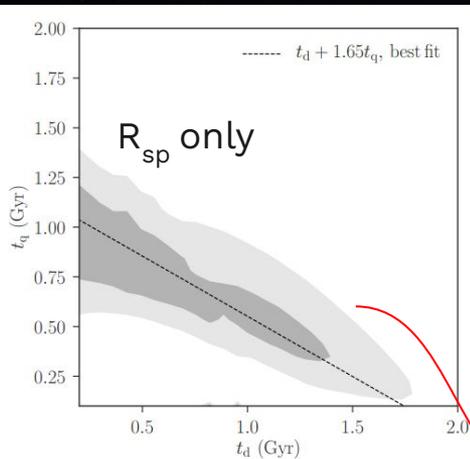
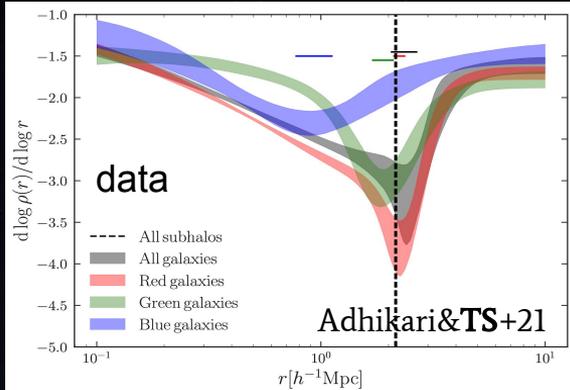
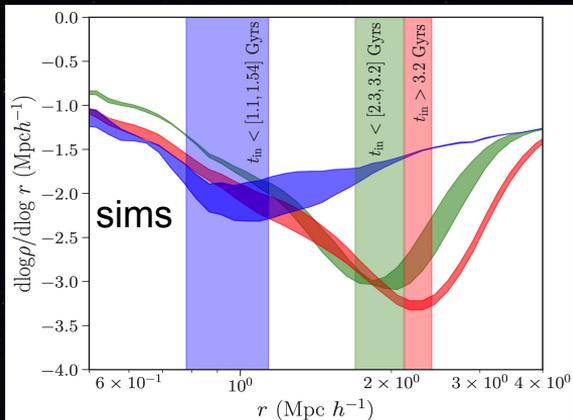


We measure profiles of galaxies split on color.

The upturn of the red fraction around  $r_{sp}$  = evidence of **quenching of galaxy star formation** inside clusters

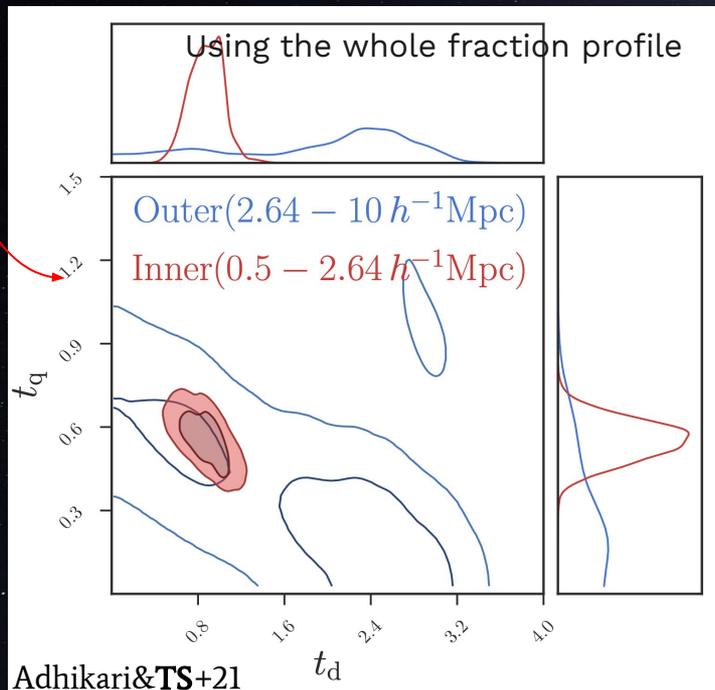
Blue galaxies are consistent to a **pure power-law** profile; indicating that they are still on their **first infall passage**  $\Rightarrow$  **qualitatively constrains maximum quenching timescale**

# $R_{SP}$ AS A QUENCHING CLOCK



Wetzel+13

$$SFR_{sat}(t) = \begin{cases} SFR_{iso}(t), & \text{if } t < t_d \\ SFR_{iso}(t) \exp\left(-\frac{t-t_d}{t_q}\right) & \text{if } t > t_d \end{cases}$$



## Constraints of Mass Accretion Rate from $R_{sp}$

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Using splashback radius calibrated against simulations to directly constrain the mass accretion rates of halos

## $R_{sp}$ as a Cosmological Probe

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Using splashback radius to constrain cosmology (especially,  $\Omega_m$ )  
⇒ supplementary to the number-count cluster cosmology

## Further Applications to Constrain Physics

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Nature of dark matter, modified gravity, galaxy star-formation quenching and etc.