

May 2025 — Shanghai Jiao Tong University  
Expanding the Boundaries of Dark Matter Halos

# The infall region of galaxy clusters as a complementary probe to cluster abundance

Based on work in:

1. Mpetha et al. (2024), MNRAS, 532, 2, arxiv:2407.01661
2. Mpetha et al. (2025), arxiv:2501.09147

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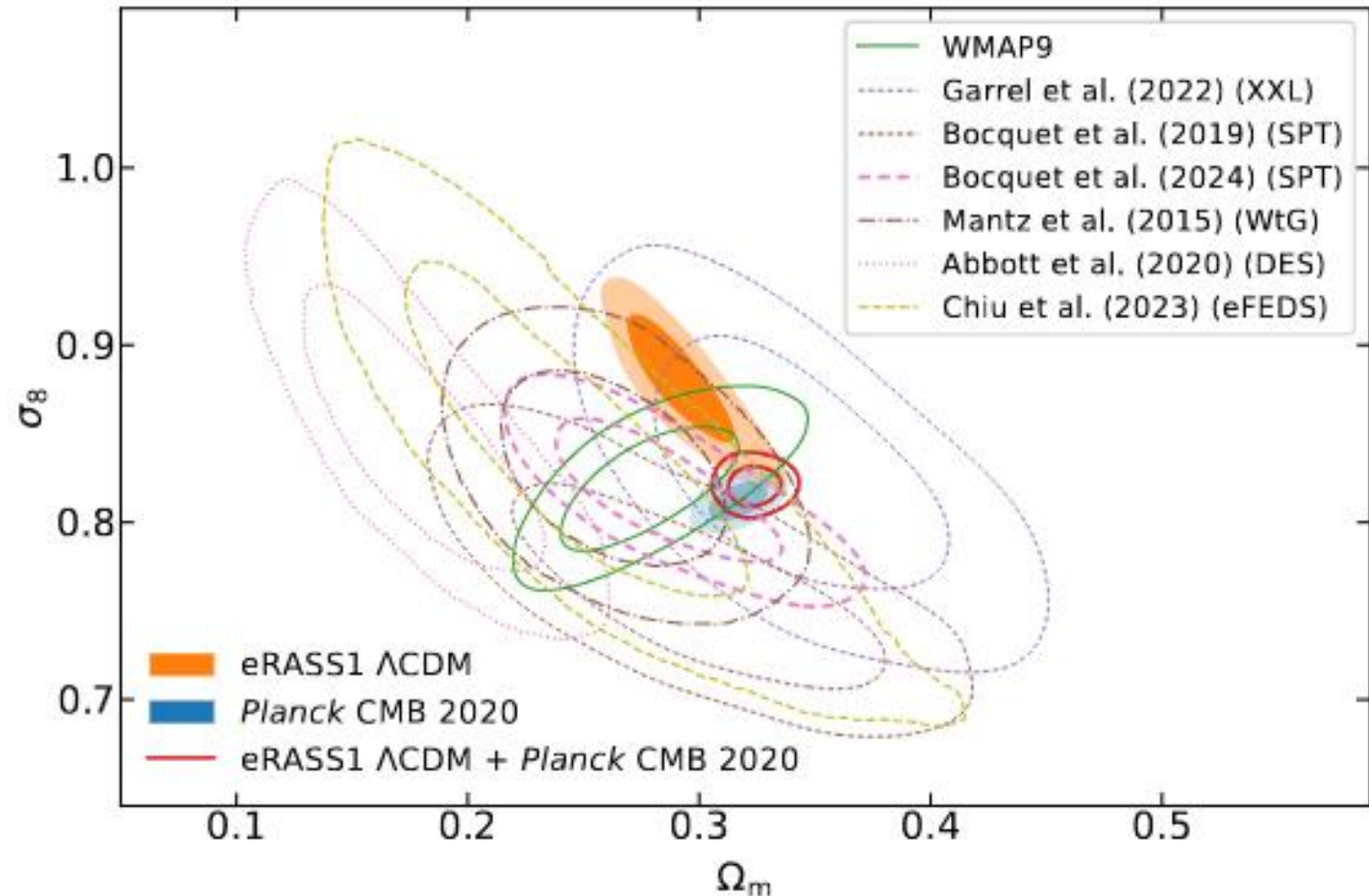


UNIONS

# Motivation

- Galaxy clusters are an excellent test-bed for cosmology
- Their abundance constrains the amount of matter in the Universe,  $\Omega_m$ , and the amplitude of density fluctuations,  $\sigma_8$
- Can we use other cluster properties to do better

SRG/eROSITA All Sky Survey (eRASS) cosmological constraints

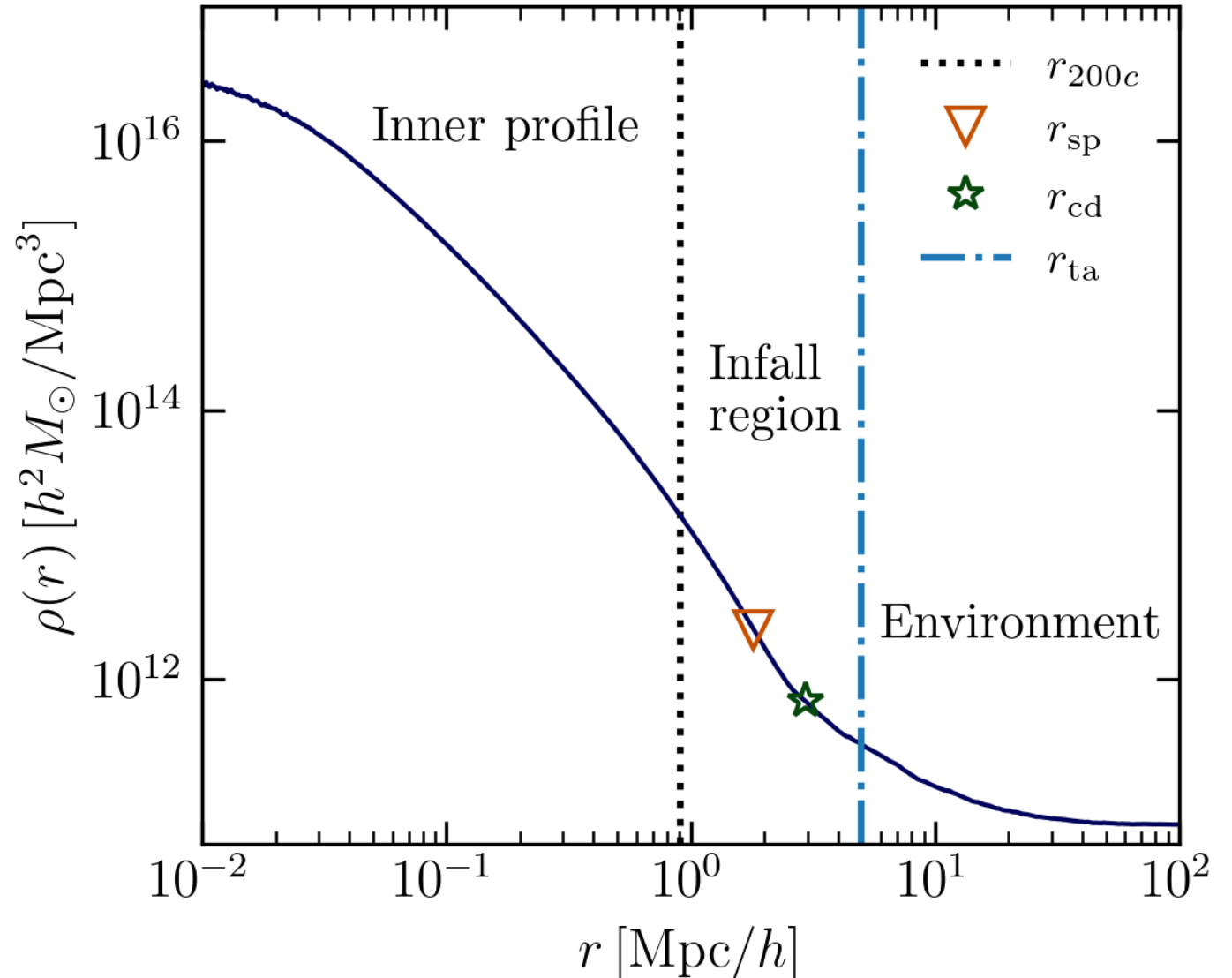


Ghirardini et al. 2024

# Infall region

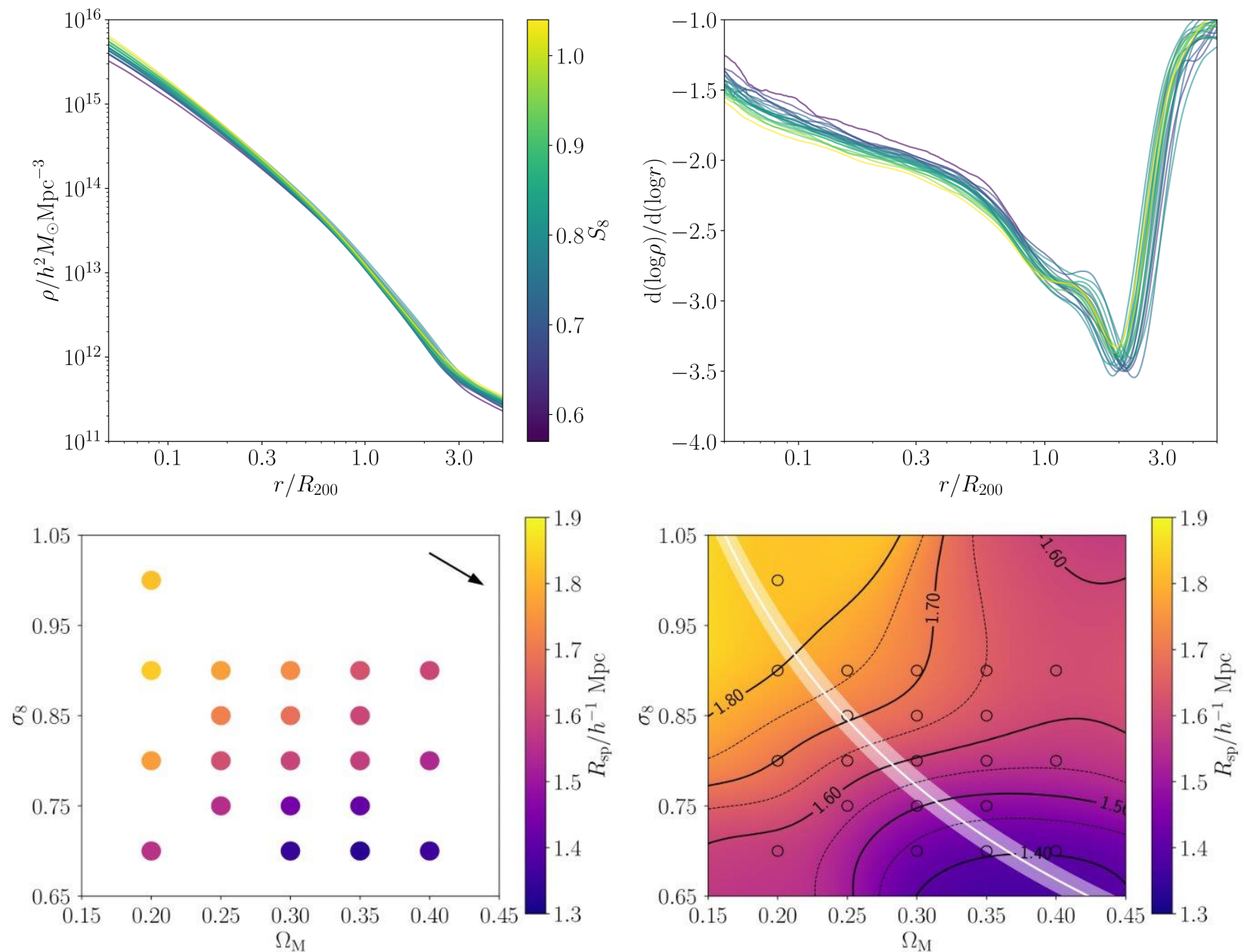
- Boundary between halo and environment
- Suite of 21 cosmological simulations with different  $\Omega_m$  and  $\sigma_8$  (Amoura et al. in prep)
- Shape of infall region depends on cosmology (Diemer et al 2017, Haggard et al 2024, Mpetha et al. 2024)

Density profile of (stacked) dark matter halo



# Infall region

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Hagggar, Amoura, Mpetha et al. 2024

$$S_8 = \sigma_8 \sqrt{\Omega_m/0.3}$$



# Weak lensing profiles of galaxy clusters

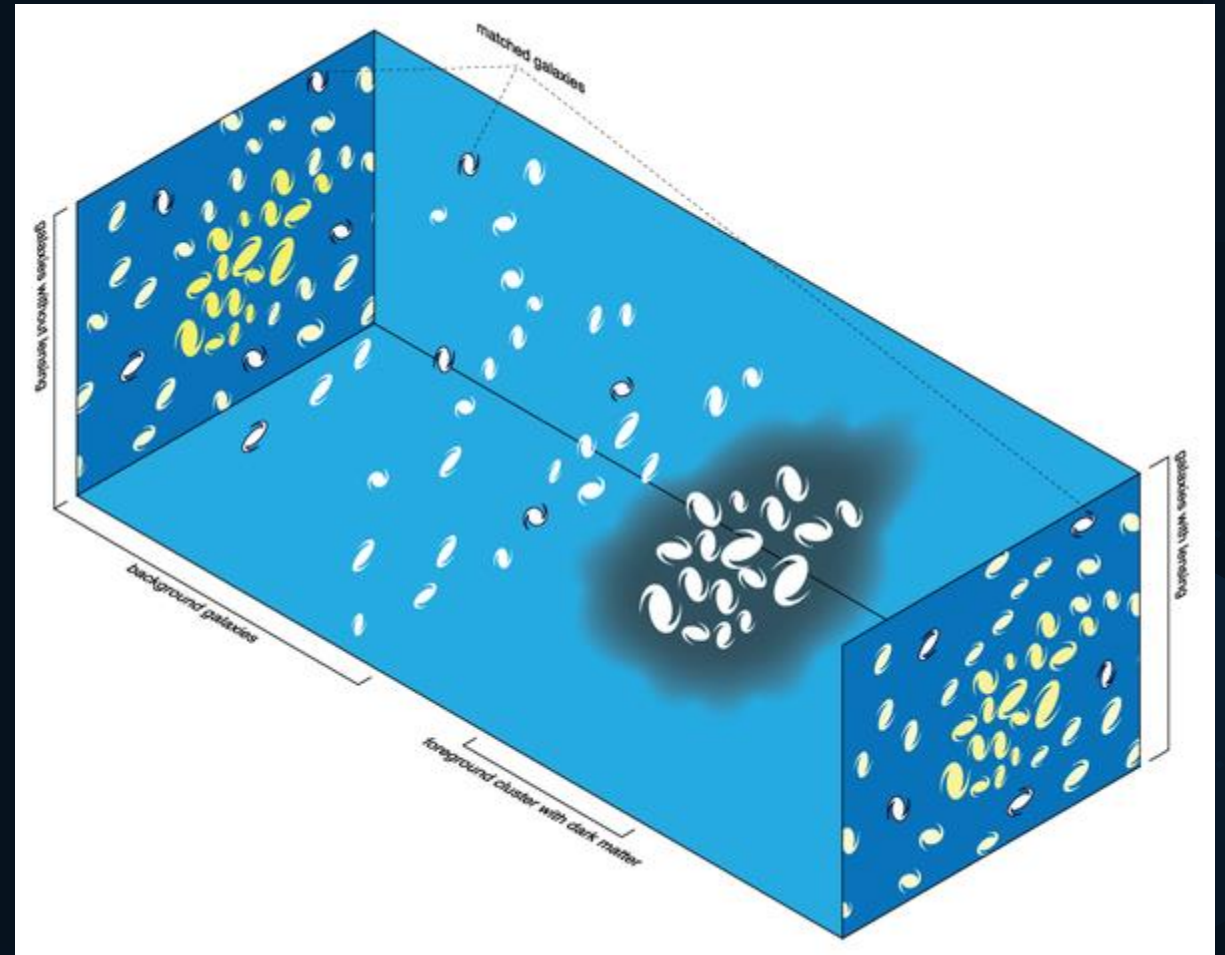
- Measure distortion of shape of background galaxies: **radial lensing profile**

$$\Delta\Sigma(r) = \gamma_t(r)\Sigma_{\text{crit}}$$

- Better tracer of total mass distribution compared to galaxy number density – compare to DM simulations

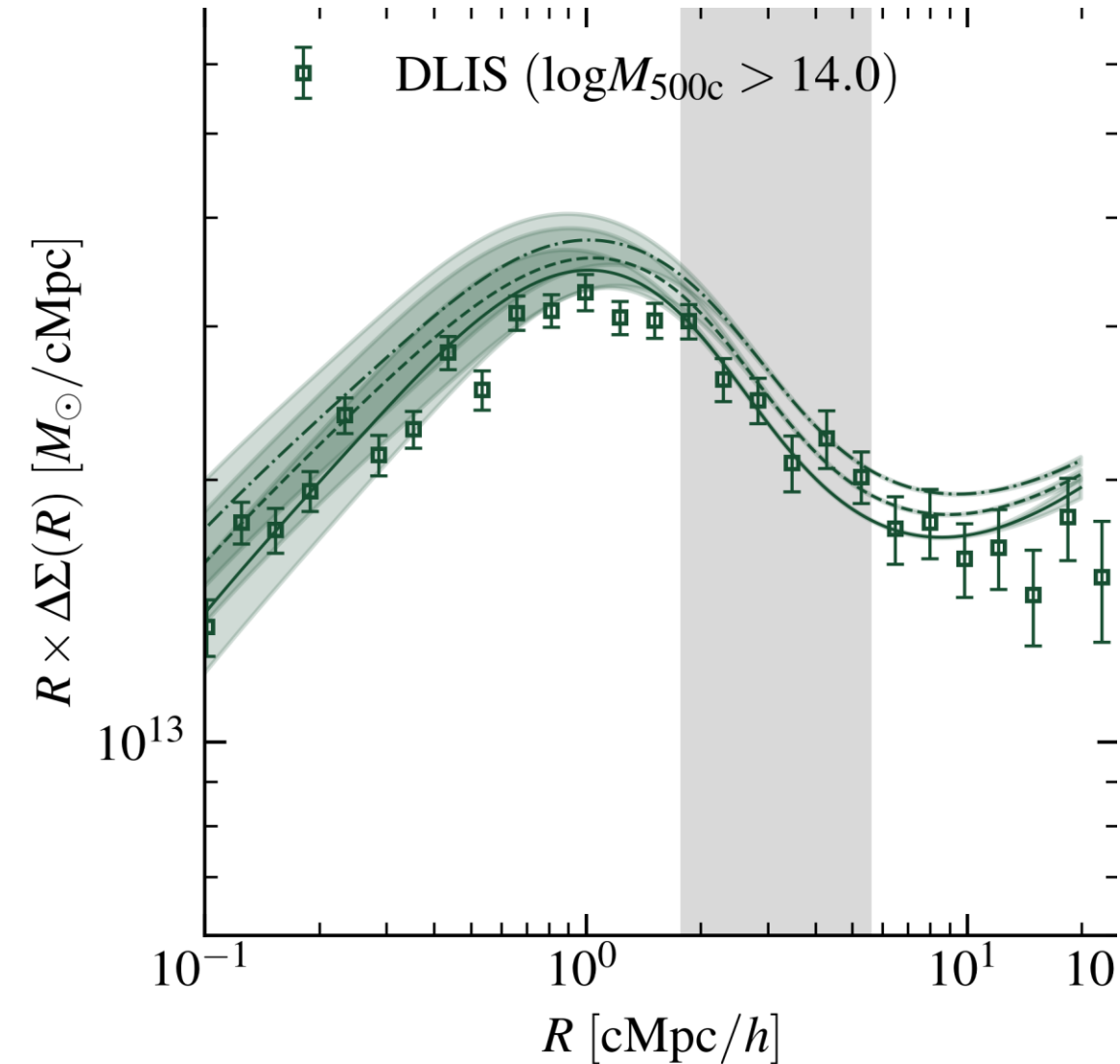
$$\Delta\Sigma(r) = \bar{\Sigma}(R) - \Sigma(R)$$

$$\Sigma(R) = 2 \int_R^\infty \frac{\rho(r)r}{\sqrt{r^2 - R^2}} dr$$



Credit: Michael Sachs

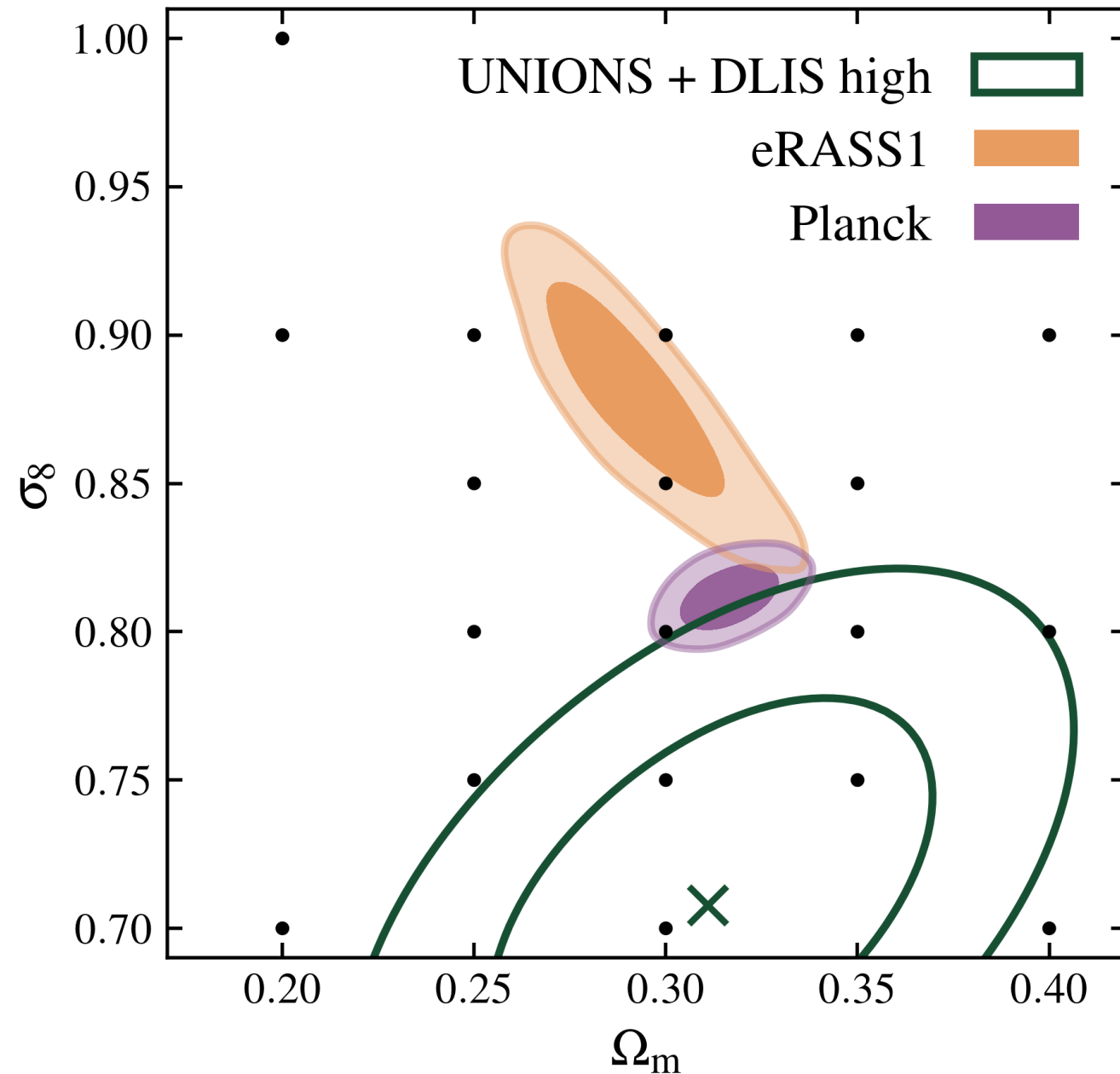
# Comparing Lensing Profiles to Simulations



- UNIONS weak lensing catalogue v1.3 (unmasked, no photo-z's): 3,200  $\text{deg}^2$  with 8.5 sources  $\text{deg}^{-2}$  (Guinot et al. 2022)
- Publicly available lens catalogue: DESI Legacy Imaging Survey (DLIS, Wen & Han 2024)
- Figure compares simulation profiles (matched redshift range) to observed profiles ( $\Omega_m=0.3$ ) - Include observational effects in simulation profiles (mis-centering, Eddington bias)
- Which simulation best matches the data?

# Results

- Compare DLIS profiles to simulations to find best-fitting cosmology
- Leads to  $\Omega_m = 0.31 \pm 0.04$ ,  $\sigma_8 = 0.71 \pm 0.04$
- Complementary degeneracy direction
- With improved lensing and cluster catalogues will be a competitive probe



Mpetha et al. 2025

# Considerations

Key advantages to this approach include:

- Complementary degeneracy
- Compared to inner-region, less sensitive to baryons and mis-centering
- Extracting features also possible (and informative)

BUT complete and pure cluster catalogue is important to:

- Mitigate dynamical selection effects
- Provide accurate observed mass estimate for profile comparison





# Conclusions + Future Work

- The infall region will help to break the large degeneracy in cluster abundance studies using only cluster information

## Next Steps:

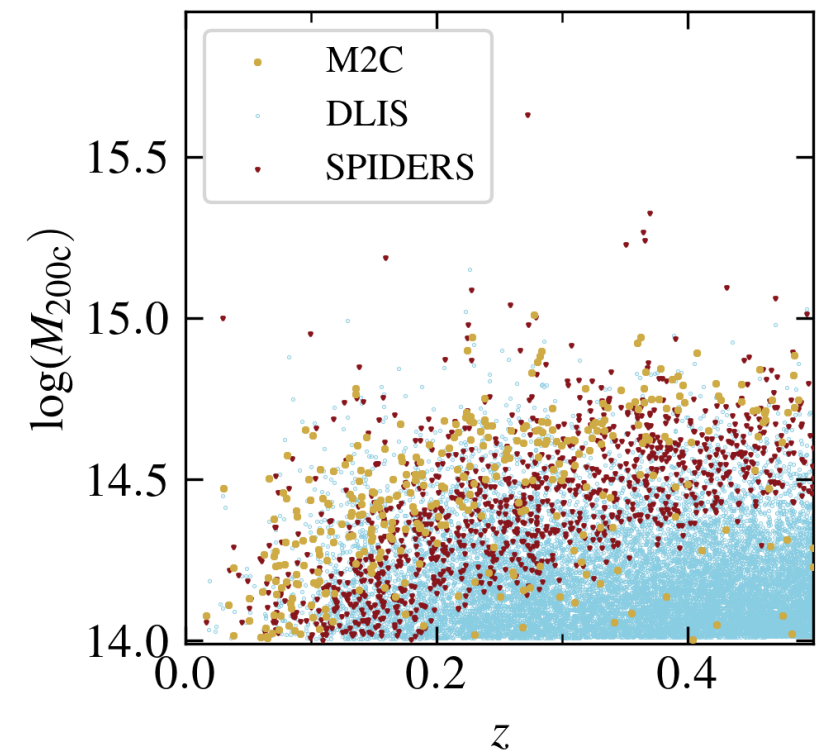
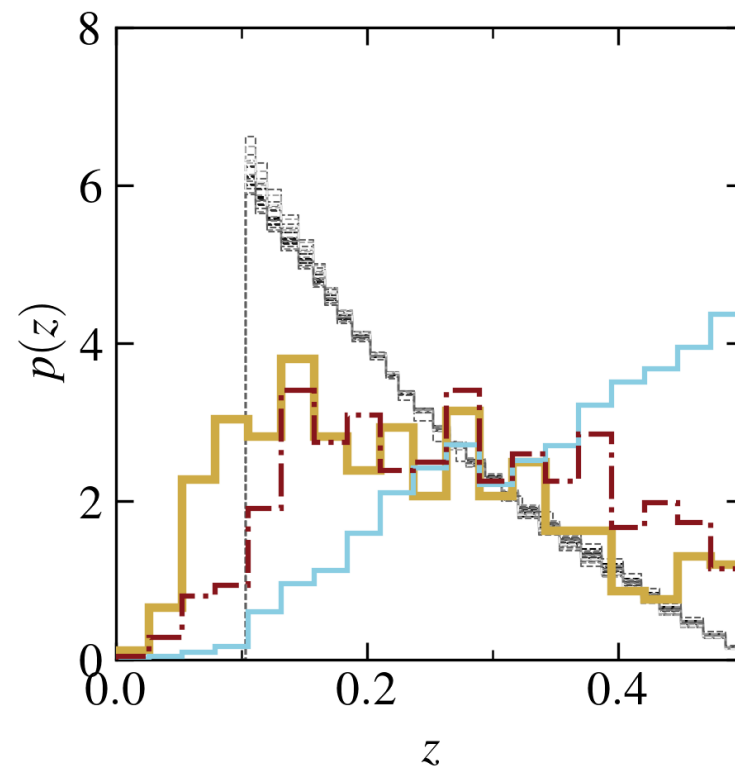
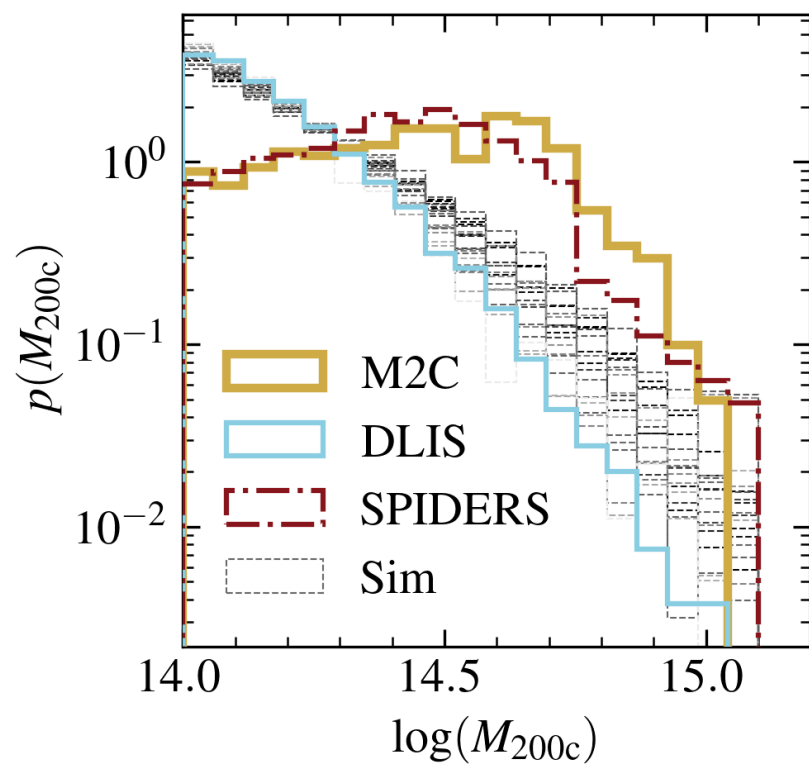
- Use AbacusSummit (finer grid of cosmologies, more parameters, more halos)
- Use spec-z clusters (DESI) with new lensing surveys (UNIONS/Euclid/Roman)



Thanks for listening

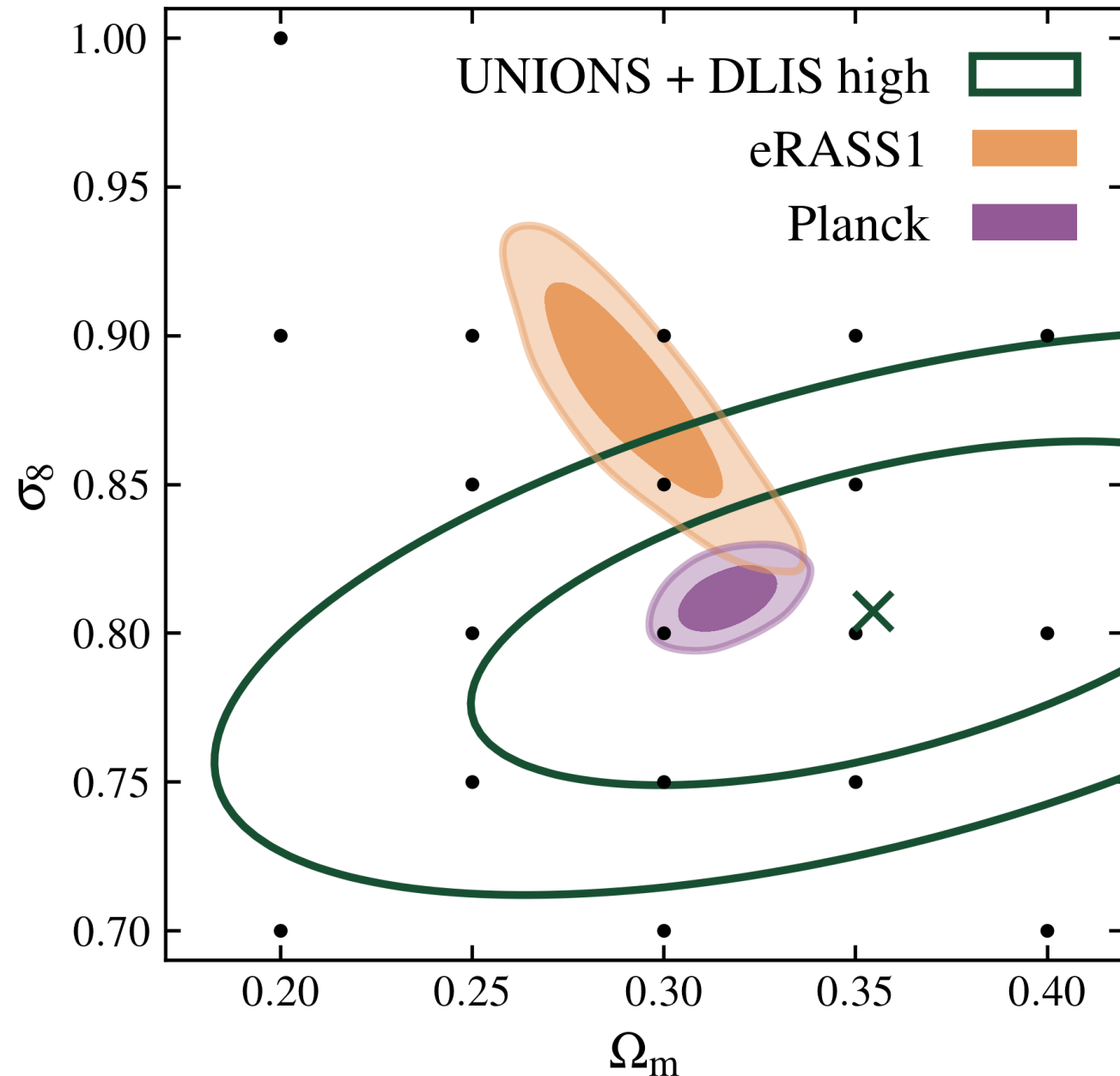
# Backup Slides

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# Redshift weighting (in progress)

- Simulated and observed lenses have a different redshift distribution
- How do results change if we weight the stacking of simulation profiles based on the snapshot redshift, to represent the observed redshift distribution





# Density Profile Model Fit

Diemer 2023 density profile model

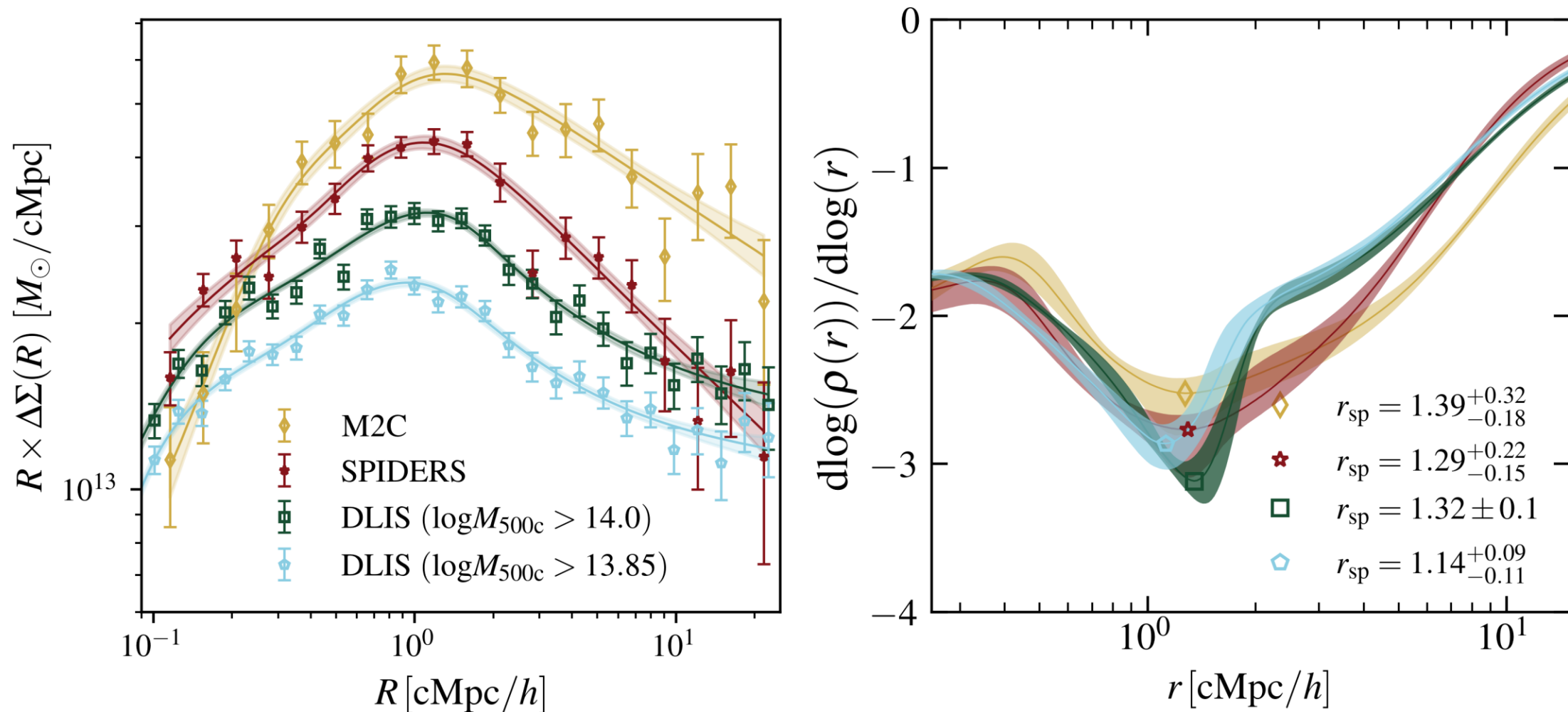
$$\rho(r) = \rho_{\text{orbit}} + \rho_{\text{infall}}$$

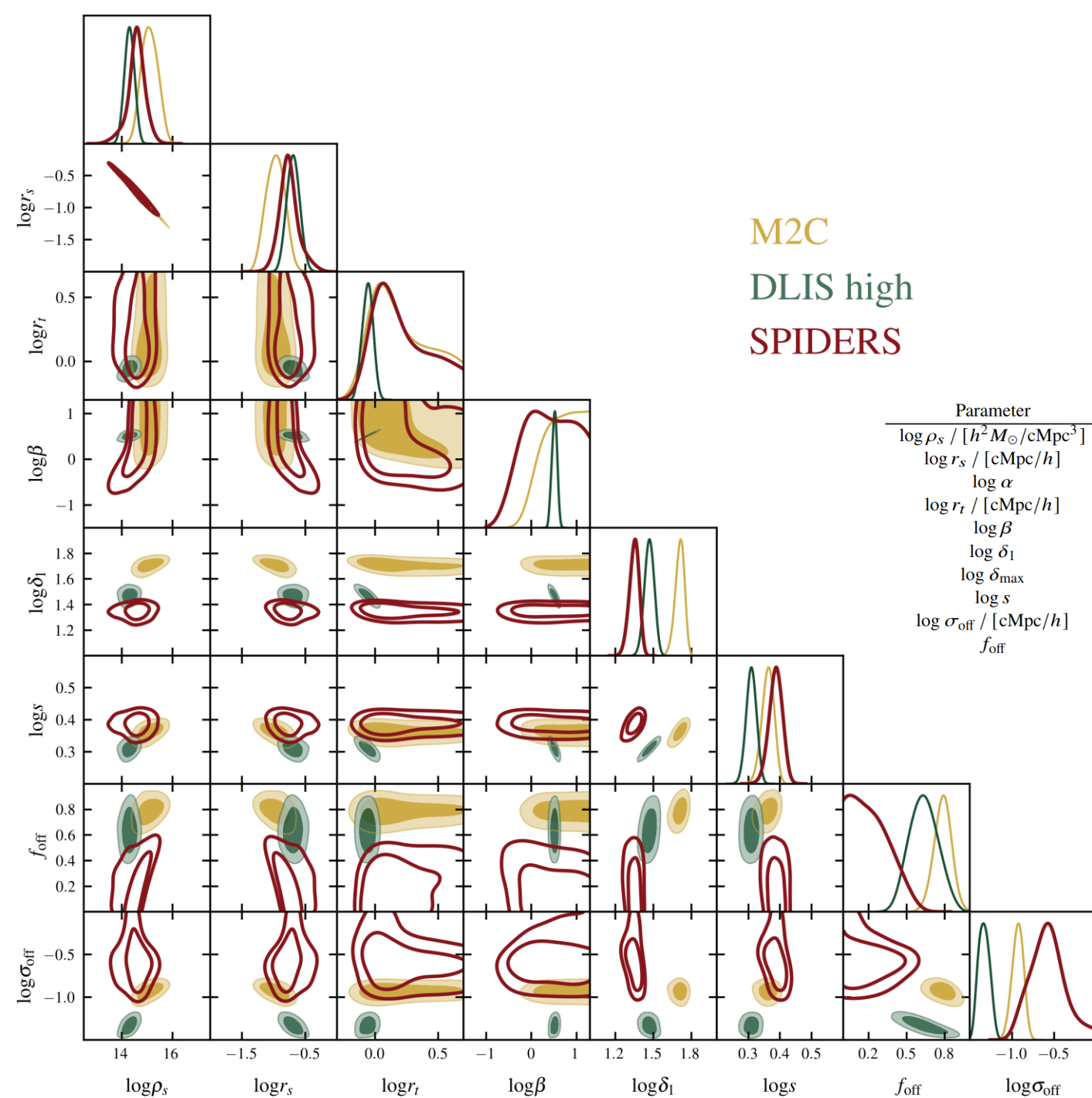
$$= \rho_s \exp \left( \left( -\frac{2}{\alpha} \right) \left[ \left( \frac{r}{r_s} \right)^\alpha - 1 \right] - \left[ \left( \frac{r}{r_t} \right)^\beta - \left( \frac{r_s}{r_t} \right)^\beta \right] \right) + \rho_m \left( 1 + \frac{\delta_1}{\sqrt{(\delta_1/\delta_{\text{max}})^2 + (r/r_{\text{pivot}})^{2s}}} \right)$$

Parameter	Fiducial value	Prior	Description	
$\log \rho_s / [h^2 M_\odot / \text{cMpc}^3]$	$\log(10^5 \rho_m)$	$\log([10^1, 10^7] \rho_m)$	Density at scale radius	Einasto
$\log r_s / [\text{cMpc}/h]$	$\log(0.07 r_{200\text{m}})$	$\log([0.01, 0.45] r_{200\text{m}})$	Scale radius	
$\log \alpha$	-1	$\log([0.03, 0.4])$	Slope of inner Einasto profile	
$\log r_t / [\text{cMpc}/h]$	$\log(r_{200\text{m}})$	$\log([0.455, 3] r_{200\text{m}})$	Truncation radius for inner Einasto profile	Truncation
$\log \beta$	0	$[-1, 1.3]$	Sharpness of truncation	
$\log \delta_1$	1	$[0, 2]$	Overdensity at the pivot radius	Infalling
$\log \delta_{\text{max}}$	2	$[0, 3 + \log(2)]$	Overdensity in the halo centre	
$\log s$	-1	$[-2, 2\log(2)]$	Slope of the infalling term	
$\log \sigma_{\text{off}} / [\text{cMpc}/h]$	-0.5	$[-2, 0]$	Amplitude of offset distribution	Mis-centering
$f_{\text{off}}$	0.3	$[0, 1]$	Fraction of lenses with offset	

# Results

- Fit profiles to find splashback radii
- Uncertainties too large for constraints





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